

USERS' MANUAL FOR ASYMMETRIC WHEEL/RAIL CONTACT CHARACTERIZATION PROGRAM

by

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16. Abstract <p>Wheel/rail geometric constraint relationships, such as the effective conicity and gravitational stiffness, strongly influence the lateral dynamics of railway vehicles. The principal curvatures of wheel and rail profiles are important parameters in the determination of creep coefficients used in rail vehicle models. In general, these geometric constraints and profile curvatures are nonlinear functions of the wheelset lateral displacement. This report is a users' manual for a computer program written in FORTRAN IV that uses iterative procedures to determine these nonlinear functions for arbitrary wheel and rail profiles. The program computes the wheel/rail contact positions, geometric constraint functions, and profile curvatures for any given wheel profile, rail profile, rail cant angle, and rail gauge for an asymmetric wheelset on asymmetric rails. Analytical methods used and program input and output are described. Results are in the form of printout, punched cards and drum plotter plots. The users' manual includes program listings, sample deck set-ups, and sample run output.</p>			
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A. INTRODUCTION AND PURPOSE

The Asymmetric Wheel/Rail Contact Characterization Program, WHRAILA, and associated subroutines compute the wheel/rail contact positions, geometric constraint functions and profile curvatures for any given wheel profile, rail profile, rail cant angle and rail gauge for an asymmetric wheelset on asymmetric rails. The program is an extension of the WHRAIL program for symmetric wheelsets on symmetric rails developed under U.S. Department of Transportation Contract Number DOT-OS-40018 and documented in [1]. Much of the material in this manual parallels directly the description of the WHRAIL program in Appendix A of [1]. Major differences between the two programs are given in Section D. A flow chart of the WHRAILA program is shown in Figure 2.

B. PROGRAM DESCRIPTION

- 1) Usage: The program consists of a main program and sixteen subroutines. Input is coordinated by the main program, WHRAILA, and subroutine PRFLE. Printed output is from the main program, subroutine PRFLE, and subroutine DCRFCN. Punched card output is from the main program. Plotted output is from subroutines PLOT1 and PLOT2. The bulk of the communication is in COMMON storage. All floating-point computations are done in double precision.

The main program, WHRAILA, coordinates the input and calculations. Subroutine PRFLE reads in the digitized profiles and fits a series of 4th order polynomials to the data using subroutines CRVFT, ORTHLS, and COEFS. The main program prints-out and punches on cards the curve-fit results. Subroutine PLOT1 plots the profile data points and the curve-fits using subroutine GTPTS to calculate the fitted points and using the plotting routines [3] associated with the CALCOMP 936 digital drum plotter to produce the plots. Subroutine EQSOLV coordinates subroutines CHECK, FIBON, CHOOSE, and RADII to find the contact point locations. Subroutine EQSUB2, using subroutines CHOOSE and RADII, calculates values of

the constraint parameters which are plotted by subroutine PLOT2, using the CALCOMP plotter routines. The main program, WHRAILA, coordinates entry points PRFLES and PRFLEP in subroutine PRFLE and the subroutines SPLINE and SPI to find profile curvatures. The main program outputs contact point, constraint parameter, and profile curvature results on the line printer and on punched cards. Profile curvature results are printed both as a function of wheelset lateral position and as a function of position on the profile.

The user has the option to suppress punched card output and plotter output. He can use the program for either symmetric configurations of the wheelset, rails, and rail cant angles or asymmetric configurations. For an asymmetric wheelset, an option is available to adjust the left wheel profile points so that the left wheel flange top is at the same height as the right wheel flange top. The program can be optionally used to only generate wheel and rail profile principal transverse curvatures.

- 2) Subroutines Required: SUBROUTINE PRFLE (NW, XW, YW, NC, RR, XB, INC, IW), the profile fitting routine, reads in data points describing a profile, divides each profile into a series of regions, and fits a 4th order polynomial to each region. Uses subroutines CRVFT, ORTHLS, and COEFS. Contains entry points PRFLES and PRFLEP to set up arrays for the spline fit calculation of profile curvatures.

SUBROUTINE CRVFT (N, L, X, Y, W, A) finds the coefficients of the 4th order polynomial that best fits an array of data points. Uses subroutines ORTHLS and COEFS.

SUBROUTINES ORTHLS (X, Y, W, N, L, J, C, ALPHA, BETA, K, T1, T2, T3, IND1) computes parameters for a fourth order polynomial using a least-squares procedure. From the Univac MATHPAC [2].

SUBROUTINE COEFS (J, C, ALPHA, BETA, KC, A, T1, T2, T3, IND2) computes the five coefficients for a fourth order polynomial. From the Univac MATHPAC [2].

SUBROUTINE PLOT1 (ICTR, ICTL, IWG, IRG) plots the wheel and rail profiles with a symbol at every other data point and draws a line representing the curve-fit. Uses subroutine GTPTS and the CALCOMP plotter routines [3].

SUBROUTINE GTPTS (XMAX, XMIN, RR, B, NC, AXW, AR1, S1, NU) calculates an array of points on the curves fitted to a profile.

SUBROUTINE EQSOLV (NUMBR, XWINC) coordinates the search for the contact points. For symmetric wheelsets and rails, it transposes positive wheelset lateral displacement results to get values for negative wheelset displacement. Uses subroutine CHECK.

SUBROUTINE CHECK (XW, DXW, WR, XOLD) uses a Fibonacci search procedure [4] to find the contact point locations. Uses subroutines CHOOSE, RADII, and FIBON.

SUBROUTINE CHOOSE (X1, X2, X3, X4) chooses the curves which represent the wheel and rail profiles at the instantaneous points of interest.

SUBROUTINE RADII (RR, YR, RL, YL, X1, X2, X3, X4, R1, R2, R3, R4) finds the functions of four fourth order polynomials for four inputs.

SUBROUTINE FIBON (N, AX, XMAXW, XMAXR, XMINW, XMINR, SBX, NCA, NCB, BA, BB, R, Y, SIGN, X1, X2, Y1) uses the Fibonacci single direction minimization search procedure [4] to find candidate contact point locations.

SUBROUTINE EQSUB2 (NUMBR) calculates the geometric constraint relations by substituting the contact point locations into the defining equations. Uses subroutines RADII and CHOOSE.

SUBROUTINE PLOT2 (NUMBR, ICTR, ICTL) plots the results. Uses the CALCOMP plotter and associated routines[3].

SUBROUTINE SPLINE (N, X, Y, C, IPRINT) computes parameters for a cubic spline curve-fit of profile data points.

SUBROUTINE SPI (N, X, Y, S, XP, YP, D1, D2, RC, CV, IER) interpolates along the profile spline curve to find values of the profile ordinate, first and second derivatives, radius of curvature, and curvature. ENTRY point SPIC (N, X, Y, S, XP, CV) is used to just find the curvature.

SUBROUTINE DCRFCN (N, AXW, AR5, AM3, AW1, AR) performs quasilinearization using describing function techniques for a sinusoidal input for symmetrical wheelsets on symmetrical rails.

3) Description of Parameters:

Main Program WHRAILA - Input parameters

XWINC	Lateral increment of wheelset at which calculations are made, inches.
ISYM	For asymmetric wheels and/or rails ISYM = 0. (All four wheel and rail input decks required.) For symmetric case ISYM = 1. (One wheel and one rail profile input deck required.) For symmetric case, but with different rail cant ISYM = 2. (Same decks as ISYM = 1.)
IPUNCH	For punched results on cards IPUNCH = 1.
IPLLOT	To bypass CALCOMP plotting routines, IPLLOT = 0.
ICURV	To only perform profile curvature calculations, ICURV = 1 (bypass contact point and geometric constraint calculations).
IFLANG	For asymmetric wheelsets, for adjusting the left wheel profile points so that right and left wheel flange top heights coincide, set IFLANG = 1.
NUMB	Number of points to be calculated, ≤ 121 . The amplitude of wheelset lateral displacement = $(NUMB - 1) * XWINC$ inches.
INC	Number of data points per curve-fit zone, $3 \leq INC \leq M/3$, where M = number of data points.
WG	Wheel gauge measured from flangeback to flangeback, inches.
RG	Rail gauge measured from inside one rail at a point 5/8" from the top of the rail to the corresponding point on the other rail, inches.

BR	Cant of right rail, radians (positive cant to the inside).
BL	Cant of left rail, radians (positive cant to the inside).
IWHLR, IWHLL	Label for right and left wheels, alphanumeric.
DTFR, DTFL	Distances from tapeline to flangeback for right and left wheels, inches.
NWR, NWL	Number of right and left wheel profile data points, $9 \leq NW \leq 200$.
XW1,YW1,XW3,YW3	Arrays of data points for wheel profiles, dimensions NWR and NWL: XW1(I), XW3(I) = distances from tapeline for right and left wheels, positive out, inches. YW1(I), YW3(I) = right and left wheel radii at XW1(I), XW3(I), inches.
IRAILR, IRAILL	Label for right and left rails, alphanumeric
DRWR, DRWL	Distances from rail head centerline to a point on the inside of the rail 5/8" down from the top of the rail for right and left rails, inches.
NYR, NYL	Number of right and left rail profile data points, $9 \leq NW \leq 200$.
XW2,YW2,XW4,YW4	Arrays of data points for rail profiles, dimensions NYR and NYL: XW2(I), XW4(I) = distances from centerline for right and left rails, positive out, inches. YW2(I), YW4(I) = heights of right and left rails at XW2(I), XW4(I), inches.
ITWO	If the input profile data cards contain one (X,Y) data point per card, ITWO = 0. For two data points per card, ITWO = 1.
INEG	If the Y coordinates of the input profile data cards are positive, INEG = 0. If they are negative, INEG = 1.

- 4) Input Formats: Sample deck set-ups are listed in Section F. The program requires the wheel and rail profile data, rail cant, rail gauge, wheel gauge and certain program control information in the following format:

Card #	Col. #	Contents	Format
1	any	XWINC	() - unspecified, real number
2	1-3	ISYM	(2I3)
2	4-6	IPUNCH	
3	1-3	IPL0T	(2I3)
3	4-6	ICURV	
4	1-3	IFLANG	(I3)
5	1-3	NUMB	(2I3)
5	4-6	INC	
6	any	WG	() - unspecified, real numbers, in order, sepa- rated by commas or blanks
6	any	RG	
6	any	BR	
6	any	BL	
7	1-52	IWHLR (start right wheel input data)	(13A4)
8	any	DIFR	() - real
9	any	NWR	() - integer
10	any	ITWO	() - integers, in order, separated by a comma or blank
10	any	INEG	
11 to end of right wheel pro- file data (ED1)	11-25 26-40	for ITWO = 0 XW1(I), YW1(I) — or —	(10X,2D15.7)
	any	for ITWO = 1 XW1(I), YW1(I), XW1(I+1), YW1(I+1)	() - real 4D15.7 numbers, in order, sepa- rated by commas or blanks

Card #	Col. #	Contents	Format
ED1 + 1	1-52	IRAILR (start right rail input data)	(13A4)
ED1 + 2	any	DRWR	() - real
ED1 + 3	any	NYR	() - integer
ED1 + 4	any	ITWO	() - integers, in order, separated by a comma or blank
ED1 + 4	any	INEG	
ED1 + 5 to end of right rail profile data (ED2)	11-25	for ITWO = 0	(10X, 2D15.7)
	26-40	XW2(I), YW2(I)	
	any	or for ITWO = 1 XW2(I), YW2(I), XW2(I+1), YW2(I+1)	() - real 4D15.7 numbers, in order, separated by commas or blanks
<p>For asymmetric case, add the following data decks:</p> <ol style="list-style-type: none"> 1) Left wheel input data (identical format to right wheel input data starting with card #7) 2) Left rail input data (identical format to right rail input data starting with card # (ED1 + 1)) 			
END-3	1-52	ICTR (Right Rail Cant)*	(13A4)
END-2	1-52	ICTL (Left Rail Cant)*	(13A4)
END-1	1-52	IRG (Rail Gauge)*	(13A4)
END	1-52	IWG (Wheel Gauge)*	(13A4)

* Character labels appearing on CALCOMP plots.

- 5) Output: For a sample output, see Section F. The main program, WHRAILA, first prints out the selected user options followed by a printout of the profile input cards. The wheel and rail descriptions and coefficients of the polynomials used to fit the profiles are printed. Two tables are then printed that contain all the contact point, geometric constraint, and profile curvature results as a function of the wheelset lateral position. For symmetric configurations, sinusoidal describing functions of certain of the results are printed by the DCRFCN subroutine. Finally, the main program prints tables of wheel and rail profile curvatures as a function of position on the profile. If selected, the results as a function of wheelset lateral position are punched by WHRAILA. If selected, the input profiles and the contact point and geometric constraint results are plotted by subroutines PLOT1 and PLOT2.

The FORTRAN names used in the program output are the following:

AMP	Amplitude of wheelset lateral motion, inches.
ALAM	Describing function of the nondimensional difference in rolling radii, $(r_L - r_R)/2a$, as a function of nondimensional wheelset lateral position, x_W/a_W .
DELM	Describing function of one half the difference in contact angles as a function of nondimensional wheelset lateral position, x_W/a_W .
WSRL	Describing function of the wheelset roll angle as a function of nondimensional wheelset lateral position, x_W/a_W .
XW	Wheelset lateral displacement, positive to the left, inches.
X1, X3	Contact locations on the right and left wheels, positive out from tapeline, inches.
X2, X4	Contact locations on the right and left rails, positive out from centerline, inches.
RR, RL	Rolling radii, right and left wheels, inches
YR, YL	Rail head profile height, right and left rails, inches.
MR, ML	Contact angles on the right and left wheel with respect to the axle, radians.
WR	Wheelset roll angle with respect to the horizontal (positive up on left), radians.

YCG	Vertical displacement of wheelset centroid from nominal position, inches.
RR CRV	Principal rolling curvature, right wheel, 1/inches.
RL CRV	Principal rolling curvature, left wheel, 1/inches.
(RL-RR)/2A	Normalized difference in rolling radii.
(ML-MR)/2	Normalized difference in contact angles, radians.
CWR, CWL	Principal transverse curvature, right and left wheel profiles, positive for center of curvature within wheel, 1/inches.
CYR, CYL	Principal transverse curvature, right and left rail profiles, positive for center of curvature within rail, 1/inches.
XWR, XWL	Distance from the tapeline on the right and left wheels, positive out from the tapeline, inches.
XRR, XRL	Distance from the centerline on the right and left rails, positive out from the centerline, inches.

6) Summary of User Requirements and Recommendations:

All input data is on cards with the formats shown. The maximum allowable points per wheel or rail profile is 200 points. For asymmetric wheels and/or asymmetric rails, ISYM = 0, and two each wheel and two each rail input decks are required. For completely symmetric configurations, ISYM = 1, and only one wheel and one rail input deck are needed. For symmetric wheels and rails, but with different rail cant angles, ISYM = 2, with one wheel and one rail input deck required.

For punched results on cards, specify IPUNCH = 1 (otherwise, specify IPUNCH = 0). To bypass CALCOMP plotting routines, specify IPLOT = 0. To bypass all calculations except profile curvature calculations, select ICURV = 1. For asymmetric wheel profiles, to adjust left wheel data points so that right and left wheel flange top heights are identical, select IFLANG = 1 (otherwise, select IFLANG = 0).

To pick values for NUMB, the number of points to be calculated, and XWINC, the lateral increment of the wheelset at which points are calculated, note that NUMB and XWINC determine the range of the wheelset lateral positions, i.e., the maximum wheelset amplitude = (NUMB - 1)XWINC inches. If calculations are made for too large a wheelset lateral displacement, then plotted results may extend

past the borders of the graphs. The suggested value for XWINC is 0.01 inch. However, XWINC = .02 inch is completely acceptable and the WHRAILA execution time is almost cut in half. When larger values of XWINC are selected, the wheelset location at which the contact point jumps from the wheel tread to the flange is less accurately defined. Suggested values for NUMB (with XWINC = .01 inch) are (1) for wide gauge take NUMB = 121 (the maximum allowed), (2) normal gauge take NUMB = 101, and (3) narrow gauge take NUMB = 81. INC determines the data points per curve-fit zone. If INC is small then the fitted curve will fit the points more closely. If INC is larger, more numerical smoothing will be done. Take INC = 6 for a start. If the curves do not fit the profiles well enough (this is determined from the plot where the profile data points and curve-fits are plotted together) then decrease INC. The maximum number of curve-fit regions allowed is 30. The maximum number of increments of the wheelset in the positive direction is 121.

Remember to input the profile data points (wheel and rail) in a sequence that starts with the largest "X" value and moves toward the smallest. This is necessary because the program separates the profiles into zones assuming this order. A message is printed if any of the "X" coordinates are out of order. There are a few other error messages in the program which are self-explanatory. There is also a warning printed when the wheelset roll angle iteration does not converge. When IFLANG = 1, for asymmetric wheels, a message is printed noting the amount that the left wheel profile "Y" values were adjusted.

C. METHOD

The computations carried out in this program can be divided into five sections:

- (1) Mathematical Description of Rail and Wheel Profiles
- (2) Calculation of Contact Point Locations
- (3) Quantitative Description of Geometric Constraint Relations
- (4) Calculation of Wheel and Rail Profile Curvatures
- (5) Quasi-linearization

The computational procedures and mathematical representations used in these five sections, respectively, are described below. A program listing for each subroutine may be found in Section F. Additional information on the theory behind the approach and methods used in the WHRAILA programs can be found in Chapter 4 of [1].

- 1) Mathematical Description of Rail and Wheel: The inputs to the program are:
 - (a) parameters specifying the size of regions to be curve-fit and the amplitude of wheelset lateral displacement allowed
 - (b) wheel and rail gauges
 - (c) tabular wheel and rail profile data
 - (d) tapeline to flangeback distance and one-half head rail width

The rail and wheel profiles are described by fourth order polynomials fitted to sub-intervals of the profiles. The sub-intervals consist of a specified number of data points with an overlap of three data points on each adjoining interval. The tabular profile data is read into a subroutine, PRFLE, that separates the data into the regions and then calls another subroutine, CRVFT, to fit a fourth order polynomial to each region. The curve-fitting is accomplished in subroutines ORTHLS and COEFS [2] that use an orthogonal polynomial, least-squares curve-fitting approach.

The output of the profile subroutine for each profile is:

- (1) the input profile data cards, (2) a set of fourth order polynomials with each polynomial fitting a certain interval of the profile, and (3) the limits defining each interval of the profile.

- 2) Calculation of Contact Point Locations: The numerical procedure to find the contact point locations is conducted in the manner described in Chapter 4 of [1] with the following exceptions:
 - (a) To handle asymmetric wheels and rails, the contact point search is conducted both for the wheelset displaced in the positive and negative directions.
 - (b) The contact points are found for XWINC inch increments (user selectable) of the wheelset lateral position.

(c) The iterative search procedures are conducted using multiple Fibonacci minimization searches [4] rather than an exhaustive search for each contact point over the entire wheel and rail profiles.

The iteration and sweeping procedures described there are performed in subroutine CHECK. Subroutine EQSOLV increment increases the wheelset lateral displacement and calls on the CHECK subroutine to find the contact points. Several geometric relations are used in subroutine CHECK. The first is the equation describing the correspondence between points on the wheel and points on the rail. The equations that express the requirement that the wheel and rail contact at the same lateral positions are, on the right

$$a_r + x_{rR} = -x_w + (a_w + x_{wR}) \cos \phi_w - r_R \sin \phi_w \quad (1)$$

and, on the left

$$a_r + x_{rL} = x_w + (a_w + x_{wL}) \cos \phi_w + r_L \sin \phi_w \quad (2)$$

The variables in these equations are shown in Figures 1 and 2. The equations equate the lateral distance of corresponding wheel and rail points from the track centerline. They are used in subroutine CHECK and FIBON to find corresponding points on the wheel and rail to check for the minimum separation distance. Recall that the minimum separation distance indicates a contact point.

The heights that are required in calculating the minimum separation distance are computed from the following four equations, one set for the wheels and one set for the rails.

$$h_{\text{right wheel}} = -r_R \cos \phi_w - (a_w + x_{wR}) \sin \phi_w \quad (3)$$

$$h_{\text{left wheel}} = -r_L \cos \phi_w + (a_w + x_{wL}) \sin \phi_w \quad (4)$$

$$h_{\text{right rail}} = y_R + x_{rR} \sin \beta_R \quad (5)$$

$$h_{\text{left rail}} = y_L + x_{rL} \sin \beta_L \quad (6)$$

The datum used for the wheel heights is a horizontal line through the wheelset centroid. Distances above the line are positive. The datum used for rail heights is the horizontal line through the base of the rails. Rail cant is assumed to tilt only the top of the rail head about its midpoint, in accordance with the standard practice of measuring the rail gauge after the rail has been canted. The actual datums used for the wheel or rail are arbitrary, as we are only interested in the minimum separation.

Wheelset roll angle is calculated from

$$\phi_w = \frac{(y_L - y_R) + x_{r_L} \sin \beta_L - x_{r_R} \sin \beta_R + (r_L - r_R) \cos \phi_w}{(2 a_w + x_{w_R} + x_{w_L}) \cos \phi_w} \quad (7)$$

where the variables are again shown in Figures 1 and 2. Note that ϕ_w is defined in terms of itself. In the program, an iterative scheme was used to solve this equation. In case of difficulties with convergence of the contact point search, print statements have been left in the coding for debugging. The variable IPRT is set to IPRT = 0 in the beginning of the main program to suppress contact point search printout. To print information (7000 lines) during the search this variable can be set to IPRT = 1. To print values of the Fibonacci search procedure, set IPRT = 2 (produces more than 20,000 lines).

- 3) Quantitative Description of Geometric Constraint Relations: The defining equations used to calculate the geometric constraint relations are evaluated in subroutine EQSUB2. EQSUB2 calls subroutines CHOOSE and RADII to choose the applicable curve-fits and to evaluate them at the contact locations determined from the value of wheelset lateral position under consideration. The defining equations for these constraint relations follow below. See Figure 2 for an illustration of the variables appearing in the equations.

1. Rolling radii and rail heights

r_R, y_R, r_L, y_L - evaluated from curve-fits

2. Contact angles

$$\delta_R = \arctan \left[\frac{d}{dx_{wR}} (r_R) \right] \quad (8)$$

$$\delta_L = \arctan \left[\frac{d}{dx_{wL}} (r_L) \right]$$

3. Normalized difference in rolling radii

$$\Delta r = \frac{r_L - r_R}{2 a_r} \quad (9)$$

4. Normalized difference in contact angles

$$\Delta \delta = \frac{\delta_L - \delta_R}{2} \quad (10)$$

5. Roll angle

$$\phi_w = \arctan \frac{(y_L + x_{rL} \sin \beta_L + r_L \cos \phi_w) - (y_R + x_{rR} \sin \beta_R + r_R \cos \phi_w)}{(2 a_w + x_{wR} + x_{wL}) \cos \phi_w} \quad (11)$$

6. Vertical displacement of wheelset c.g.

$$y_{cg} = \left[\frac{y_L + y_R + x_{rL} \sin \beta_L + x_{rR} \sin \beta_R + (r_L + r_R) \cos \phi_w}{2} \right]_{x_w = 0} \quad (12)$$

- 4) Calculation of the Wheel and Rail Profile Curvatures: Curvature of the wheel and rail profile shapes are important parameters in the calculation of creep coefficients as a function of wheelset position. The main program, WHRAILA, coordinates the calculation of wheel and rail profile curvatures by calling subroutine SPLINE,

ENTRY points PRFLES and PRFLEP in subroutine PRFLE, and ENTRY point SPIC in subroutine SPI. The main program selects the range of profile points over which curvatures are calculated and calls the ENTRY PRFLES routine to select the data points through which a profile spline curve-fit is passed (explained below). The subroutine SPLINE is then called to fit a spline through these points. The ENTRY SPIC in subroutine SPI is called to interpolate for curvatures at the contact points found on each wheel and rail profile. The main program prints and punches on cards profile curvatures for the right wheel, right rail, left wheel, and left rail as a function of wheelset lateral position. The main program uses the ENTRY PRFLEP routine and the ENTRY SPIC routine to interpolate for profile curvature as a function of distance in 0.05 inch increments along each profile and prints the results in a table.

Curvature at any point on a wheel or rail profile is computed from a curve fitted to the profile data points. The curvature of a function y of one variable x is defined as

$$\alpha(x) = \frac{\frac{d^2y(x)}{dx^2}}{[1 + (\frac{dy(x)}{dx})^2]^{3/2}} \quad (13)$$

For any x , $\frac{d^2y}{dx^2}$ and $\frac{dy}{dx}$ can be found by interpolating on the fitted curve for second and first derivatives of $y(x)$, respectively, and $\alpha(x)$ can be found from equation (13).

Profile data points may be fitted with a single, high-order polynomial. However, the inevitable wiggles of such a polynomial fit would give inaccurate values for the first and second derivatives. A sequence of low-order polynomials for sub-intervals could be used to fit the data points. This technique, using fourth order polynomials in least-squares fits over sub-intervals, was used in PRFLE and gives good results for interpolating function values $y(x)$. However, since first and second derivatives are not required to agree as we shift from one sub-interval polynomial to the next, discontinuities in $\frac{d^2y(x)}{dx^2}$ and $\frac{dy(x)}{dx}$ and thus in $\alpha(x)$ occur at the boundary between sub-intervals.

To cope with this problem, a composite interpolation technique called the cubic spline fit was used. In cubic spline interpolation, a set of cubics is passed through the points in sub-intervals along the profile and the function value, first derivative, and second derivative are required to be the same at the ends of the sub-intervals where one cubic meets the next. Thus we have a continuous second derivative (and a continuous curvature) throughout the whole range of interpolation. Each data point through which the spline fit passes is called a joint and defines the boundary between two adjacent sub-intervals. In computing the coefficients for the cubic in each sub-interval, the function value, the first derivative, and the second derivative at each joint are used in a set of $n \times n$ simultaneous equations for n joints. Thus the location of each joint affects the entire spline fit. The values of the second derivatives at the end points must be specified by the spline user.

Fitting profiles with joints at each data point resulted in curvature values that oscillated excessively between joints. This is due to at least three problems.

- a) In the recording of profile data points (done by digitization of profile plots or some other means), minor data point deviations from a "smooth" curve inevitably result. These small deviations are amplified in the calculation of derivatives of a curve passed through these points. In a spline fit, each joint (located at a data point) affects the entire curve-fit. The cumulative effects of small deviations of the data points from a smooth curve may cause large oscillations in the curvature. A solution to this problem is to select only a few of the data points for spline joints, which will tend to smooth out the fit and the curvature results.
- b) A cubic spline will fit a cubic (3rd degree polynomial) exactly to joints located on a cubic curve. However, when fitting joints lying in a straight line, oscillations or wiggles in the curve-fit occur between joints. This problem is particularly noticeable in the fitting of the straight taper of the new AAR wide flange wheel tread. The problem can be minimized by selecting joints at widely spaced data points along the wheel profile tread.

c) A very large range in the first and second derivatives between data points causes the curvature of a spline passed through the points to oscillate excessively. This was noticed in the fitting of a new standard AAR rail profile. When points on the vertical gauge and field sides of the rail were included in the spline fit, large oscillations in the curve-fit occurred along the top of the rail. This problem was solved by only including the contact portion of the rail in the spline fit.

Thus the procedure of selecting locations of spline joints from profile data points is important in obtaining accurate curvature results. The main program limits the range of profile data points for candidate joints to the range of contact points on the wheels and rails. The ENTRY PRFLES routine is called to select joint locations for the spline fit. End joints for the wheel curve-fits are located on the top of the flange and at either the furthest contact point from the tapeline on the tread or one inch from the tapeline (whichever is larger). Approximate joint spacing is 0.15 inch on the flange, 0.30 inch on the flange root, and 0.50 inch on the tread. This selection defines the curvature better on the flange and minimizes curve-fit oscillations on the tread. End joints for the rail curve-fits are located at the contact point closest to the centerline between rails and at either the furthest contact point from the rail centerline to the field side or one inch from the centerline (whichever is larger). Joint spacing is 0.1 to 0.2 inches on the gauge side of the rail and 0.4 inch on the rail head. This selection defines the curvature accurately on the rail gauge edge, while avoiding curve-fit oscillations on the rail head.

After selection of joint locations, the main program calls subroutine SPLINE to solve the set of simultaneous equations associated with a spline fit. Then the ENTRY SPIC routine is called for each wheel and rail profile to interpolate for profile curvatures at contact point locations. The main program prints and punches on cards the curvature results as a function of wheelset lateral position.

A separate printout of lateral profile principal curvatures as a function of distance along the profiles (in 0.05 inch increments), is furnished by the main program by calling the ENTRY

PRFLEP routine and the ENTRY SPIC routine. The coordinate systems used are given in Figure 1. This printout can be generated by itself by use of the user option ICURV = 1 (contact point search and geometric constraint calculations are bypassed).

The principal lateral profile curvature computation procedure was verified by comparing spline fit results of digitized profile data against design curvatures of the following profiles: New AAR rail, new AAR wide flange wheel for freight vehicles, new modified Heumann wheel, and new Canadian National Profile A wheel.

The principal rolling curvatures of the right and left wheels are computed for each location x_w of the wheelset by the equations

$$\text{RR CRV}(x_w) = \frac{\cos(\delta_R(x_w))}{r_R(x_w)} \quad (14)$$

$$\text{RL CRV}(x_w) = \frac{\cos(\delta_L(x_w))}{r_L(x_w)}$$

Limitations to the accuracy of principal lateral curvatures of wheel and rail profiles should be remembered:

- a) Inaccuracies or noise in the taking of profile data points can cause oscillation inaccuracies in the interpolated curvature values.
 - b) Curvature values may oscillate slightly in the wheel tread region, particularly for a straight taper tread.
 - c) Curvatures interpolated from the end spline sub-intervals can be in error. This is due to the assumption that the second derivative at the end joints is a linear extrapolation of the second derivative values of the adjacent two spline joints.
- 5) Quasi-linearization: The quasi-linearization method described here assumes that we have symmetric wheels on symmetric rails. The sinusoidal input describing function is defined by the following equation:

$$Y_q = \frac{1}{\pi A^2} \int_0^{2\pi} F(A \sin \phi) A \sin \phi d\phi. \quad (15)$$

The relations to quasi-linearize are the following:

$$\Delta r \equiv \frac{r_L - r_R}{2a_r}; \quad \Delta \delta \equiv \frac{\delta_L - \delta_R}{2}; \quad \text{and } \phi_w.$$

These are non-dimensional and non-hysteretic. Also, due to the symmetry of the wheel and rail profiles, they are odd functions of the wheelset lateral position, i.e. $\Delta r(x_w) = -\Delta r(-x_w)$. If these properties are applied, the describing function can be re-written as:

$$Y_q = \frac{4}{\pi A^2} \int_0^{\pi/2} F(A \sin \phi) A \sin \phi d\phi. \quad (16)$$

This equation is numerically integrated in the program. To do this, the integration increment, $d\phi$, was expressed as a function of x , because the functions to be quasi-linearized were tabulated as functions of x . The substitution was made by letting

$$x = A \sin \phi \quad (17)$$

or

$$\phi = \sin^{-1} \frac{x}{A}, \quad 0 \leq \phi \leq \pi/2 \quad (18)$$

and thus

$$\begin{aligned} \Delta \phi_n &= \phi_n - \phi_{n-1} \\ &= \sin^{-1} \left(\frac{x_n}{A} \right) - \sin^{-1} \left(\frac{x_{n-1}}{A} \right) \end{aligned} \quad (19)$$

Substitution of this result into the describing function equation (15) gives

$$Y_q = \frac{4}{\pi A^2} \int_0^{\pi/2} F(x)x \, d\phi(x) \quad (20)$$

When we let $f(x) = F(x)x$ and numerically integrate using the trapezoidal rule, we obtain

$$\begin{aligned} Y_q \approx & \frac{4}{\pi A^2} \frac{f(x_1) + f(x_2)}{2} \left(\sin^{-1} \frac{x_2}{A} - \sin^{-1} \frac{x_1}{A} \right) \\ & + \frac{f(x_2) + f(x_3)}{2} \left(\sin^{-1} \frac{x_3}{A} - \sin^{-1} \frac{x_2}{A} \right) + \dots \\ & + \frac{f(x_{n-1}) + f(x_n)}{2} \left(\sin^{-1} \frac{x_n}{A} - \sin^{-1} \frac{x_{n-1}}{A} \right) \quad (21) \end{aligned}$$

where $x_1 = 0$ and $x_n = A$.

This equation was programmed in subroutine DCRFCN. It was multiplied, in the subroutine, by a_r to non-dimensionalize the describing function for the parameters considered.

D. MAJOR DIFFERENCES BETWEEN WHRAILA AND WHRAIL PROGRAMS

- 1) The program can calculate wheel/rail contact points and geometric constraint functions for any given asymmetric wheelset, asymmetric rails, and asymmetric rail cant angles as well as the case of a symmetric wheelset on symmetric rails.
- 2) Execution time of the contact point search procedure, where most of the computer time is spent, has been reduced by about a factor of 10 by replacing the exhaustive search with a Fibonacci search procedure.
- 3) Execution time has been streamlined in several other places, particularly in CHECK, CHOOSE, EQSOLV, and EQSUB2. For example, redundant IF statements, redundant variable calculations and unneeded array processing have been removed.
- 4) Principal profile curvatures of the wheels and rails are calculated using cubic spline fits.
- 5) Options for suppressing punched card and plotter outputs have been introduced.

- 6) The plotting routines allow wheel rolling radii of any diameter and allow any rail height.
- 7) Processing of all real variables is in double precision.

E. TEST PROBLEMS

The following test problems are given to demonstrate the WHRAILA program. The calculations were performed on a IBM 370/3165-II computer. With the plot and punch options selected, CPU execution time was less than 10 seconds for the symmetric problem and less than 15 seconds for the asymmetric problem.

1) Symmetric Problem:

Profiles: New AAR Wheel
 New AAR Rail

Gauges: Rail gauge - nominal, 56.5 inches
 Wheel gauge - nominal, 53 inches

Rail Cant: 0.025 radians (1.4324 degrees)

Maximum Allowed Wheelset Lateral Displacement: 1 inch

2) Asymmetric Problem:

Profiles: Right wheel - Moderately Worn AAR Wheel
 Right rail - New AAR Rail
 Left wheel - Slightly Worn AAR Wheel
 Left rail - Worn AAR Rail

Gauges: Rail gauge - wide, 57.5 inches
 Wheel gauge - nominal, 53 inches

Rail Cants: Right rail - 0.025 radians
 Left rail - 0.025 radians

Maximum Allowed Wheelset Lateral Displacement: 1.2 inch

The program listing, card input, printer output, plotter output, and punched card output listing for these problems are contained in the following section.

F. PROGRAM LISTINGS WITH INPUTS AND OUTPUTS FOR TEST PROBLEMS

1) Program Listings

2) Symmetric Problem:

- a) Listing of input cards
- b) Printer output
- c) CALCOMP plotter output
- d) Partial listing of punched card output

3) Asymmetric Problem:

- a) Listing of input cards
- b) Printer output
- c) CALCOMP plotter output
- d) Partial listing of punched card output

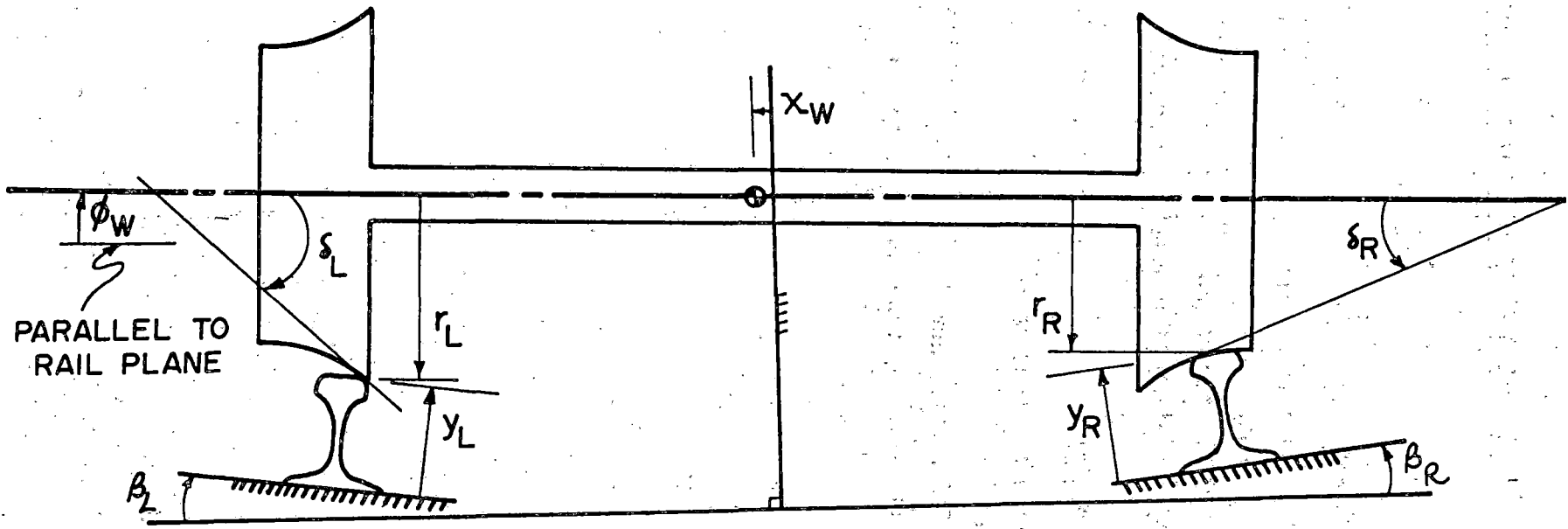


FIGURE 1A WHEEL / RAIL PARAMETERS, REAR VIEW [From Ref. 1]

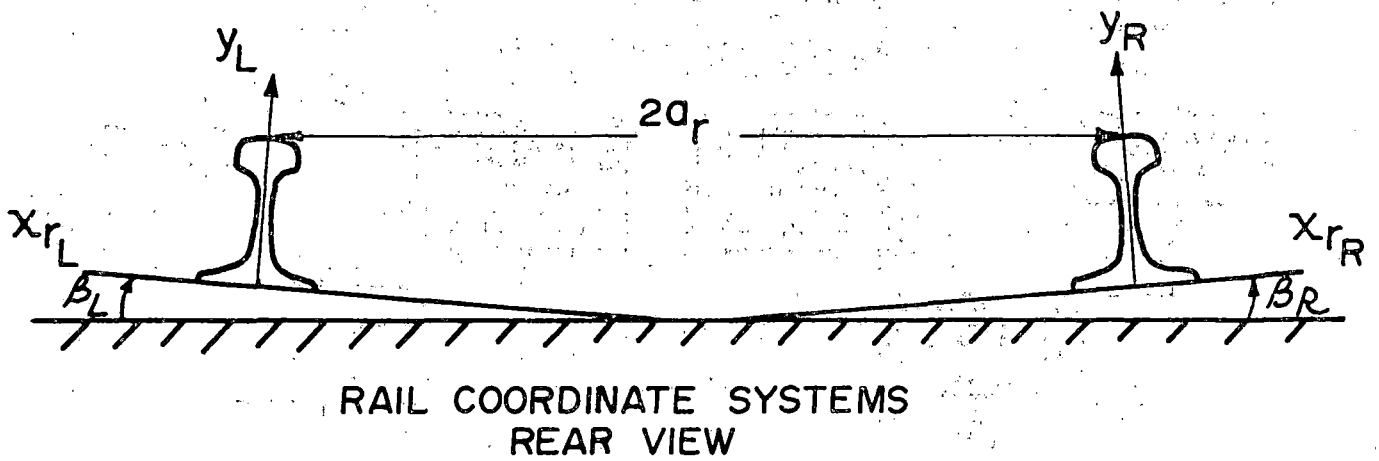
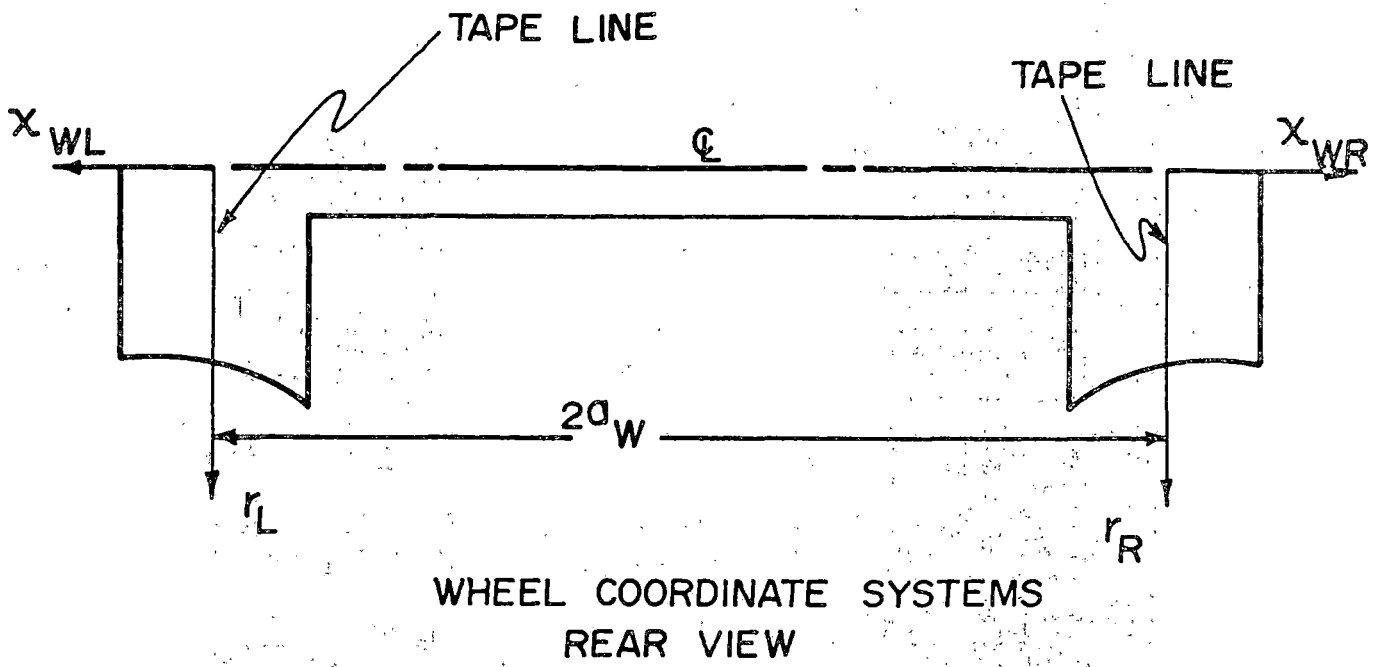
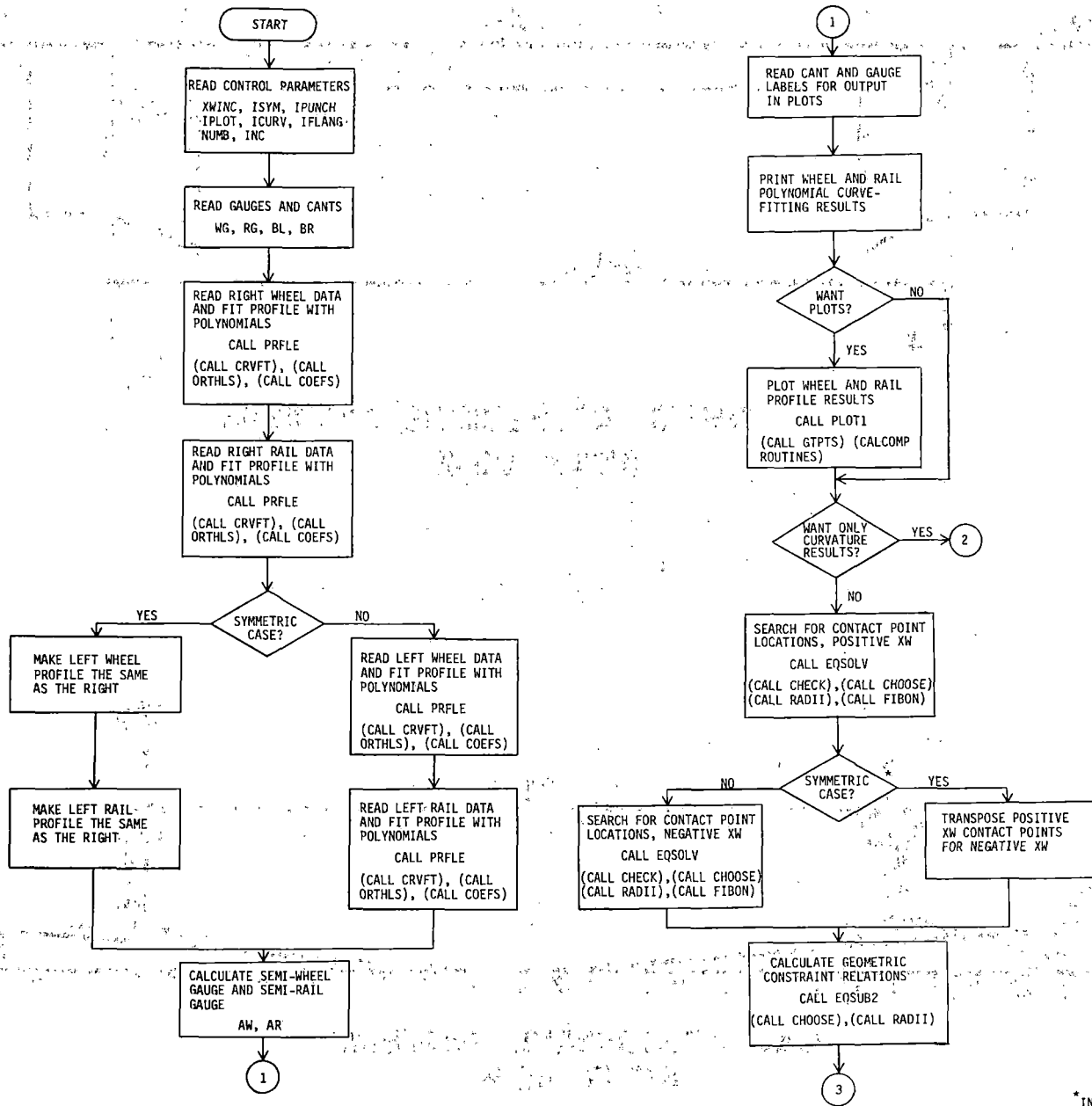


FIGURE 1B WHEEL/RAIL COORDINATE SYSTEMS [From Ref. 1]



* EQSOLV

FIGURE 2. FLOWCHART, ASYMMETRIC WHEEL/RAIL CONTACT CHARACTERIZATION PROGRAM

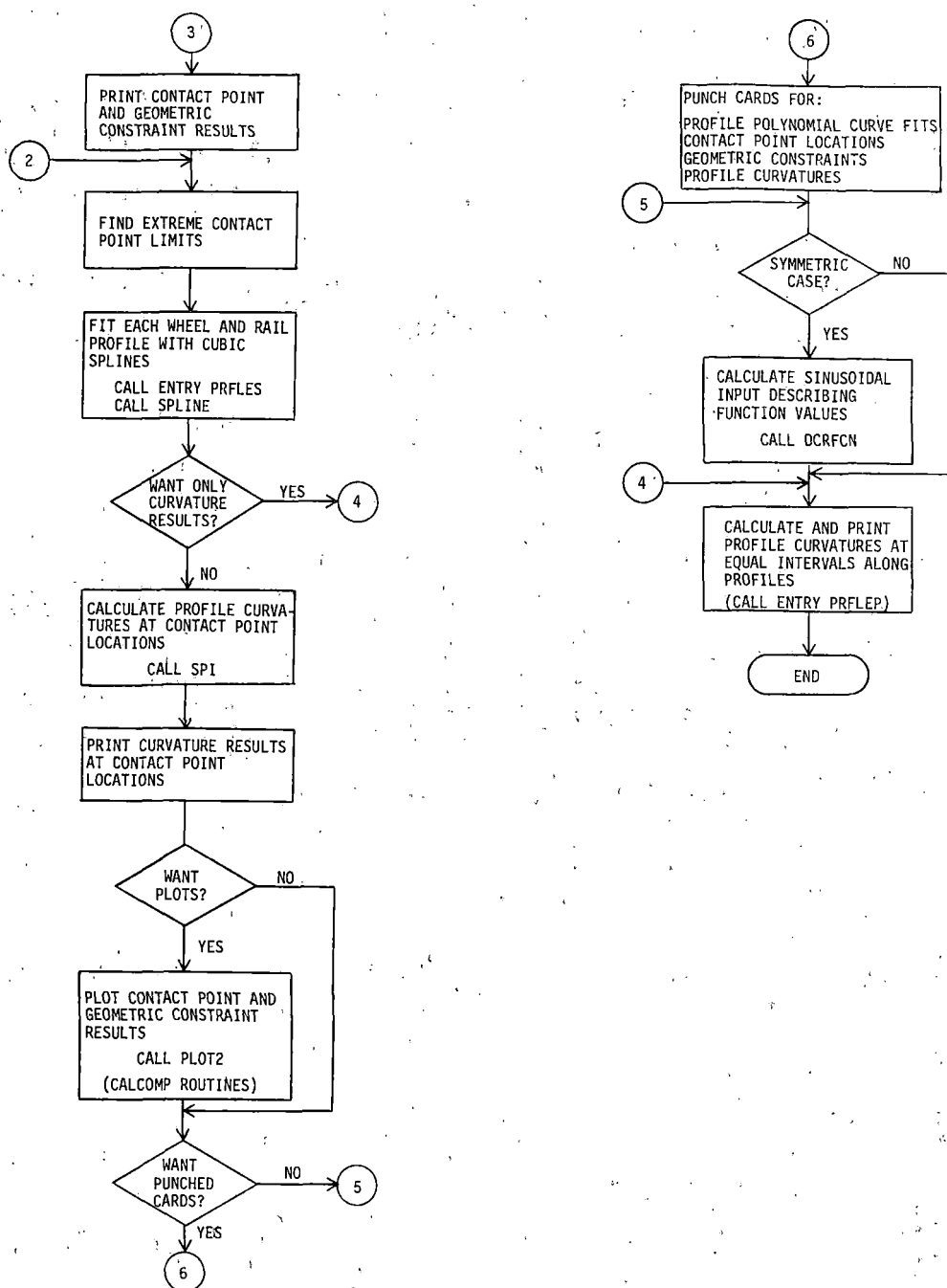


FIGURE 2 (continued). FLOWCHART, ASYMMETRIC WHEEL/RAIL CONTACT CHARACTERIZATION PROGRAM

PROGRAM LISTINGS

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C THE ASYMMETRIC WHEEL/RAIL CHARACTERIZATION PROGRAM - WHRAILA
C WRITTEN AT ARIZONA STATE UNIVERSITY BY R. HULL, N. K. COOPERRIDER
C REWRITTEN AT CLEMSON UNIVERSITY BY R. HELLER, C. H. CSTLING
C SUPPORTED BY U. S. DEPT. OF TRANSPORTATION/FED. RAIL ADMINISTRATION
C CONTRACT DOT-US-40018, PROGRAM DIRECTOR, E. HARRY LAW, CLEMSON UNIV.
C FOR DESCRIPTION REFER TO:
C 1) HELLER, R., N. K. COOPERRIDER, "USERS' MANUAL FOR ASYMMETRIC
C WHEEL/RAIL CONTACT CHARACTERIZATION PROGRAM", FRA REPORT, AUG 1977
C 2) COOPERRIDER, N. K., E. H. LAW, R. HULL, P. S. KADALA, J. M. TUTEN,
C "ANALYTICAL AND EXPERIMENTAL DETERMINATION OF NONLINEAR WHEEL/RAIL
C GEOMETRIC CONSTRAINTS", REPORT NO. FRA-CR&D 76-244, DEC 1975
C FIBONACCI SEARCH VERSION
C INCLUDES CALCOMP PLOTTING
C INCLUDES PROFILE SPLINE FIT RADIUS OF CURVATURE CALCULATIONS
C MODIFIED TO ALLOW MORE RUN OPTIONS
C MODIFIED TO RUN WITH DOUBLE PRECISION
C
C IMPLICIT REAL*8(A-H,O-Z)
C DIMENSION IRG(13), IWG(13), ICTR(13), ICTL(13)
C DIMENSION AR1C(244), AR2C(244), AR3C(244), AR4C(244),
C 1 ARR1C(244), ARR3C(244), XI05(140)
C DIMENSION XJ1(50), YJ1(50), SJ1(50), XJ2(50), YJ2(50), SJ2(50),
C 1 XJ3(50), YJ3(50), SJ3(50), XJ4(50), YJ4(50), SJ4(50)
C
C COMMON /COMA/ AW, AR, BR, BL, RR(30,5), YR(30,5), RL(30,5), YL(30,5),
C 1 B1(30,2), B2(30,2), B3(30,2), B4(30,2), S1(5), S2(5), S3(5), S4(5),
C 1 AXW(244), AX1(244), AX2(244), AX3(244), AX4(244), AR1(244), AR2(244),
C 1 AR3(244), AR4(244), AR5(244), AM1(244), AM2(244), AM3(244), AW1(244),
C 1 AY1(244), NC1, NC2, NC3, NC4, ISYM
C COMMON /COMB/ YWIM, IFLANG
C COMMON /COMC/ IWHLR(13), IWHL(13), ITRAILR(13), ITRAIL(13)
C COMMON /COMD/ XW1(200), YW1(200), XW2(200), YW2(200), NWR, NYR,
C 1 XW3(200), YW3(200), XW4(200), YW4(200), NWL, NYL
C COMMON /COME/ XMINWR, XMINRR, XMINWL, XMINRL, XMAXWR, XMAXRR,
C 1 XMAXWL, XMAXRL
C COMMON /COMF/ M1, M2, M3, M4, M5, M6, STEP, IPRT
C
C DATA XJ1, YJ1, SJ1, XJ2, YJ2, SJ2, XJ3, YJ3, SJ3, XJ4, YJ4, SJ4/600*0.000/
C
C *****MAXIMUM PROFILE PTS 200
C *****MAXIMUM NUMBER OF CURVE FITS 30
C *****MAXIMUM INCREMENTS OF XW IN POSITIVE DIRECTION 121
C PRINT 801
C 801 FORMAT(' THE ASYMMETRIC WHRAIL/RAIL CONTACT CHARACTERIZATION PROGR
C 1AM'/'/' RUN OPTIONS SELECTED'/' )
C
C READ(1,*)XWINC
C WRITE(3,1)XWINC
C 1 FORMAT(' ', T10, 'XWINC=', F8.4/)
C XWINC IS LATERAL INCREMENT OF WHEELSET CENTROID
C NUMB OF PTS TO BE CALC MUST TAKE XWINC INTO ACCOUNT
C
C READ 30, ISYM, IPUNCH
C WRITE(3,2) ISYM, IPUNCH
C 2 FORMAT(' ', T10, 'ISYM=', I3, T25, 'IPUNCH=', I2/)
C 30 FORMAT(3I3)
C ISYM=1 FOR SYMMETRIC CASE
C ISYM=2 FOR SAME PROFILES ON BOTH WHEELS AND RAILS, BUT WITH
C DIFFERENT RAIL CANTS.
C IPUNCH=1 FOR PUNCH RESULTS
C
C READ 30, IPLOT, ICURV
C WRITE(3,33) IPLOT, ICURV
C 33 FORMAT(' ', T10, 'IPLOT=', I2, T25, 'ICURV=', I2/)
C IPLOT=0 FOR NO CALCOMP PLOTTING (BYPASS PLOTTING ROUTINES)
C ICURV=1 FOR ONLY PERFORMING PROFILE CURVATURE CALC (BYPASS CONTACT
C PCINT, GEOM CALC)
C

```



```

      READ 30,IFLANG
      WRITE(3,34)IFLANG
34  FCRMAT(' ',T10,'IFLANG =',I2/)
C  IFLANG = 1 TO ADJUST LT WHEEL DATA SUCH THAT TOP OF FLANGE
C  UN LT WHEEL = RT WHEEL
C
      READ 30,NUMB,INC
      WRITE(3,31) NUMB,INC
31  FCRMAT(' ',T10,'NUMB=',I3,T25,'INC=',I2)
      NUMBR=2.*NUMB
C  NUMBR=NC OF PTS TO BE CALCULATED
C  * NC OF PTS TO BE CALCULATED MUST BE LT 400, XW IS + CR - NUMBR*.01/2.
C  * FIT A CURVE EVERY INC DATA PTS (SUGGEST INC=5)
C
      STEP=.01
      IPRT=0
      M1=12
      M2=9
      M3=9
      M4=12
      M5=9
      M6=11
C  WRITE(3,3)STEP,IPRT,M1,M2,M3,M4,M5,M6
3  FCRMAT(/' ',T10,'STEP=',F8.4,T25,'IPRT=',I2//
1  ' ',T10,'M1=',I3,9X,'M2=',I3,9X,'M3=',I3/
1  ' ',T10,'M4=',I3,9X,'M5=',I3,9X,'M6=',I3)
C  STEP = INCREMENT ALONG WHEEL PRFLE DURING CONTACT PT SEARCH
C  (SUGGEST STEP=0.01)
C  M1, ..., M6 ARE SIZES OF FIBONACCI SEARCHES
C  A CHANGE TO STEP REQUIRES CORRESPONDING CHANGES TO M1,...M6.
C  STEP=.01 M1,...M6 = 12 9 9 12 9 11
C  STEP=.005 M1,...M6 = 14 10 10 14 10 12
C  IPRT PRINTOUT SHOULD BE USED ONLY FOR PARTIAL RUNS (TESTING PURPOSES)
C  IPRT=1 TO PRINT INFORMATION DURING CONTACT PT SEARCH (7000 LINES)
C  IPRT=2 TO PRINT FIBONACCI CONTACT PT SEARCH PRCCEDURE (>20000 LINES)
C
C  WG=WHEEL GAGE, RG=RAIL GAGE, BR=BL=CANT CF RAILS
      READ(1,*)WG,RG,BR,BL
      PRINT 802
802  FCRMAT(/' WHEEL GAUGE (IN), RAIL GAUGE (IN), RIGHT RAIL CANT (RAD)
1, LEFT RAIL CANT (RAD)')
      WRITE(3,4)WG,RG,BR,BL
4  FCRMAT(/4F11.5/)
C
C  *** READ A ONE LINE LABEL FOR THE TYPE OF RIGHT WHEEL
      READ 10,(IWHLR(I),I=1,13)
10  FORMAT(13A4)
      PRINT 803
803  FCRMAT(/' RIGHT WHEEL PRCFILE INPUT DATA ',85('**')/)
      WRITE(3,12) (IWHLR(I),I=1,13)
12  FCRMAT(1X,13A4)
      READ(1,*)DTRF
      WRITE(3,5) DTRF
C  ** DTRF=DIST FROM TAPELINE TO FLANGEBACK ON RIGHT WHEEL
      CALL PRFLE(NWR,XW1,YW1,NC1,RR,B1,INC,1)
      IF(ISYM.EQ.1.OR.ISYM.EQ.2) IFLANG = 0
      IF(IFLANG.NE.1) GO TO 15
C  FIND TOP OF FLANGE FOR RT WHEEL
      YW1M = YW1(1)
      DO 14 I = 2, NWR
      IF(YW1(I)-YW1M) 14,14,13
13  YW1M = YW1(I)
14  CONTINUE
15  CONTINUE
C
C  *** READ A ONE LINE LABEL FOR TYPE CF RIGHT RAIL
      READ 10,(IRAILR(I),I=1,13)
      PRINT 804
804  FCRMAT(/' RIGHT RAIL PRCFILE INPUT DATA ',85('**')/)
      WRITE(3,12) (IRAILR(I),I=1,13)
      READ(1,*)DRWR
      WRITE(3,5) DRWR

```

```

C *** DRWR=1/2 RIGHT RAIL WIDTH AT 5/8 IN DCWN
CALL PRFLE(NYR,XW2,YW2,NC2,YR,B2,INC,0)
C
C CHECK FOR SYMMETRIC CASE
IF ((ISYM.NE.1).AND.(ISYM.NE.2)) GO TO 25
C USE THE SAME WHEEL PROFILE ON EITHER END OF THE WHEELSET
NC3=NC1
DO 60 I=1,NC1
DO 50 J=1,5
RL(I,J)=RR(I,J)
50 CONTINUE
B3(I,1)=B1(I,1)
B3(I,2)=B1(I,2)
60 CONTINUE
C USE THE SAME RAIL PROFILE ON EITHER SIDE OF THE TRACK
NC4=NC2
DO 80 I=1,NC2
DO 70 J=1,5
YL(I,J)=YR(I,J)
70 CONTINUE
B4(I,1)=B2(I,1)
B4(I,2)=B2(I,2)
80 CONTINUE
NWL=NWR
DO 90 I=1,NWR
XW3(I)=XW1(I)
YW3(I)=YW1(I)
90 CONTINUE
AYL=NYR
DO 91 I=1,NYR
XW4(I)=XW2(I)
YW4(I)=YW2(I)
91 CONTINUE
DTFL=DTFR
DRWL=DRWR
DO 92 I=1,13
IWHLL(I)=IWHLR(I)
IRAILL(I)=IRAILR(I)
92 CONTINUE
GO TO 45
C
C *** READ A ONE LINE LABEL FOR THE TYPE OF LEFT WHEEL
25 READ 10,(IWHLL(I),I=1,13)
PRINT 805
805 FORMAT(//' LEFT WHEEL PROFILE INPUT DATA ',85('**')/)
WRITE(3,12) (IWHLL(I),I=1,13)
READ(1,*) DTFL
WRITE(3,5) DTFL
CALL PRFLE(NWL,XW3,YW3,NC3,RL,B3,INC,2)
C
C *** READ A ONE LINE LABEL FOR TYPE OF LEFT RAIL
READ 10,(IRAILL(I),I=1,13)
PRINT 806
806 FORMAT(//' LEFT RAIL PROFILE INPUT DATA ',85('**')/)
WRITE(3,12) (IRAILL(I),I=1,13)
READ(1,*) DRWL
WRITE(3,5) DRWL
CALL PRFLE(NYL,XW4,YW4,NC4,YL,B4,INC,0)
5 FORMAT(2F11.5)
C
C *** AW=SEMI WHEEL GAGE=1/2 DIST BETWEEN TAPE LINES
45 AW=(WG+DTFR+DTFL)/2.
C *** AR=1/2 DIST FROM CENTER OF ONE RAIL TO CENTER OF THE OTHER
AR=(RG+DRWR+DRWL)/2.
C
XMINWR=XW1(NWR)
XMINRR=XW2(NYR)
XMINWL=XW3(NWL)
XMINRL=XW4(NYL)
XMAXWR=XW1(1)
XMAXRR=XW2(1)
XMAXWL=XW3(1)
XMAXRL=XW4(1)

```

```

C READ THE CANT, WHEEL GAGE, AND RAIL GAGE FOR USE ON CN OUTPUTTING
C THEM IN THE PLOTTING ROUTINES
  READ(1,10)(ICTR(I),I=1,13)
  READ(1,10)(ICTL(I),I=1,13)
  READ(1,10)(IRG(I),I=1,13)
  READ(1,10)(IWG(I),I=1,13)
  WRITE(3,11) ICTL
  WRITE(3,11) ICTR
  WRITE(3,11) IRG
  WRITE(3,11) IWG
11  FCORMAT(' ',13A4)
C
C PRINT RESULTS OF PROFILE CURVE-FITTING
  PRINT 190
190  FCORMAT(1H1,21X,'***** RESULTS ***** ')
  PRINT 195
195  FCORMAT(// 34X,'RIGHT SIDE//')
C
C PRINT MATHEMATICAL DESCRIPTIONS OF WHEELSET AND TRACK
  PRINT 200,IWHLR,WG,AW,INC
200  FCORMAT(12X,'WHEEL/RAIL CONTACT CHARACTERIZATION'// 9X,13A4//
1  2X,'WHEEL GAGE=' ,F6.3/2X,' 1/2 DIST BETWEEN TAPE LINES=' ,F6.3//
1  5X,'CURVE FITS' ,3X,I2,' PTS/CURVE FIT ZONE'//14X,'OTH' ,12X,'1ST' ,
1  12X,'2ND' ,12X,'3RD' ,12X,'4TH')
C
  DO 210 I=1,NC1
  PRINT 205,I,(KR(I,J),J=1,5),B1(I,1),B1(I,2)
205  FCORMAT(2X,I3,3X,5(D13.6,2X),3X,'FROM ' ,F8.4,' TC ' ,F7.4)
210  CCNTINUE
C
  PRINT 220,IRAILR,KG,AR,BR,INC
220  FCORMAT(//9X,13A4,//2X,'RAIL GAGE=' ,F6.3/2X,' 1/2 DIST BETWEEN RAIL
1  CENTERS=' ,F6.3/2X,'RAIL CANT=' ,F6.3,
1  //5X,'CURVE FITS' ,3X,I2,' PTS/CURVE FIT ZONE'//14X,'OTH' ,
1  12X,'1ST' ,12X,'2ND' ,12X,'3RD' ,12X,'4TH')
C
  DO 230 I=1,NC2
  PRINT 205,I,(YR(I,J),J=1,5),B2(I,1),B2(I,2)
230  CCNTINUE
  PRINT 231
231  FCORMAT(1H1,35X,'LEFT SIDE//')
  PRINT 200,IWHLR,WG,AW,INC
  DO 234 I=1,NC3
  PRINT 205,I,(RL(I,J),J=1,5),B3(I,1),B3(I,2)
234  CCNTINUE
  PRINT 220,IRAILL,KG,AR,BL,INC
  DO 238 I=1,NC4
  PRINT 205,I,(YL(I,J),J=1,5),B4(I,1),B4(I,2)
238  CCNTINUE
C
C PLOT TABULAR WHEEL AND RAIL DATA AND FITTED CURVES
  IF(IPLT.EQ.0 .OR. ICURV.EQ.1) GO TO 236
  CALL PLOTS(0,0,0)
  CALL PLOT(0,0,3)
  CALL PLOT1(ICTR,ICTL,IWG,IRG)
236  CCNTINUE
C
  IF(ICURV.EQ.1) GO TO 301
C FINDS THE CONTACT PT LOCATIONS
  CALL EQSOLV(NUMBR,XWINC)
C FINDS THE GEOMETRIC CONSTRAINT RELATIONS
  CALL EQSUB2(NUMBR)
C
C PRINT A TABLE OF MOST OF THE RESULTS
C
C FOR ROLLING RADII CURVATURE PRINTOUT
  DO 239 I=1,NUMBR
  ARR1C(I)=DCOS(AM1(I))/AR1(I)
  ARR3C(I)=DCOS(AM2(I))/AR3(I)
239  CCNTINUE
  PRINT 240
240  FCORMAT(1H1 2X,'***** DATA POINTS *****// )

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810 PRINT 810
FORMAT(' CONTACT PCINTS, GEOMETRIC CONSTRAINTS, AND PROFILE CURVAT
URES'// AS A FUNCTION OF WHEELSET LATERAL DISPLACEMENT'//
1' XW = WHEELSET LATERAL, POSITIVE TO THE LEFT (IN)'/
1' X1 = CONTACT LOCATION CN RIGHT WHEEL, POSITIVE OUT FROM TAPELINE
1 (IN)'/
1' X2 = CONTACT LOCATION CN RIGHT RAIL, POSITIVE OUT FROM CENTERLIN
E (IN)'/
1' X3 = CONTACT LOCATION CN LEFT WHEEL, POSITIVE OUT FROM TAPELINE
1 (IN)'/
1' X4 = CONTACT LOCATION CN LEFT RAIL, POSITIVE OUT FROM CENTERLINE
1 (IN)'/
1' RR = ROLLING RADII, RIGHT WHEEL (IN)'/
1' YR = RAIL HEAD PROFILE HEIGHT, RIGHT RAIL (IN)'/
1' RL = ROLLING RADII, LEFT WHEEL (IN)'/
1' YL = RAIL HEAD PROFILE HEIGHT, LEFT RAIL (IN)'/
1' MR = CONTACT ANGLE W.R.T. AXLE, RIGHT WHEEL (RAD)'/
1' ML = CONTACT ANGLE W.R.T. AXLE, LEFT WHEEL (RAD)'/
PRINT 815
FORMAT(' RR CRV = PRINCIPAL ROLLING CURVATURE OF RIGHT WHEEL PROFI
LE (1/IN)'/
1' RL CRV = PRINCIPAL ROLLING CURVATURE OF LEFT WHEEL PROFILE (1/IN
1)'/
PRINT 245
245 FORMAT(4X,'XW',7X,'X1',6X,'X2',6X,'X3',6X,'X4',7X,'RR',7X,'YR',
1 7X,'RL',7X,'YL',9X,'MR',8X,'ML',7X,'RR CRV',4X,'RL CRV'//
1 3X,'(IN)',5X,3'( (IN)',4X),5'( (IN)',5X),2X,
1 2'( (RAD)',5X),2'( (1/IN)',4X)'/
PRINT 250, (AXW(I), AX1(I), AX2(I), AX3(I), AX4(I), AR1(I), AR2(I),
1 AR3(I), AR4(I), AM1(I), AM2(I), ARR1C(I), ARR3C(I), I=1, NUMBR)
250 FORMAT(2X,F6.3,2X,F7.4,1X,F7.4,1X,F7.4,1X,F7.4,2X,F8.5,1X,F8.5,
1 1X,F8.5,1X,F8.5,2X,F9.6,1X,F9.6,F11.6,F10.6)
C
C CALCULATE PROFILE CURVATURES USING SPLINE FITS
C
C FIND LTMOST (MOST NEG) & RTMOST (MOST POS) CP LOCATIONS
AX1R = AX1(1)
AX2L = AX2(1)
AX2R = AX2(1)
AX3R = AX3(1)
AX4L = AX4(1)
AX4R = AX4(1)
DO 300 I = 2, NUMBR
IF(AX1(I).GT.AX1R) AX1R = AX1(I)
IF(AX2(I).LT.AX2L) AX2L = AX2(I)
IF(AX2(I).GT.AX2R) AX2R = AX2(I)
IF(AX3(I).GT.AX3R) AX3R = AX3(I)
IF(AX4(I).LT.AX4L) AX4L = AX4(I)
IF(AX4(I).GT.AX4R) AX4R = AX4(I)
300 CONTINUE
GO TO 303
C
C SET THE LEFTMOST & RIGHTMOST PTS FOR CURV CALC WHEN ICURV=1
C WHEEL: SET RT CURVE-FIT LIMIT AT 1ST PT LT OF 2.2 INCH
301 DO 701 I=1,NWR
IF(XW1(I).LT.2.2) GO TO 702
701 CONTINUE
702 AX1R=XW1(I)
DO 703 I=1,NWL
IF(XW3(I).LT.2.2) GO TO 704
703 CONTINUE
704 AX3R=XW3(I)
C RAIL: SET RT CURVE-FIT LIMIT AT 1ST PT WITH SLOPE LT 2.
C RAIL: SET LT CURVE-FIT LIMIT AT 1ST PT BEFORE SLOPE GT 6.
NR=NYR-1
NL=NYL-1
DO 705 I=1,NR
IF(DABS((YW2(I+1)-YW2(I))/(XW2(I+1)-XW2(I))).LT.2.) GO TO 706
705 CONTINUE
706 AX2R=XW2(I)
DO 707 I=1,NL
IF(DABS((YWL(I+1)-YWL(I))/(XWL(I+1)-XWL(I))).GT.6.) GO TO 708

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707  CCNTINUE
      I=NYR
708  AX2L=XW2(I)
      DG 709 I=1,NL
      IF(DABS((YW4(I+1)-YW4(I))/(XW4(I+1)-XW4(I))).LT.2.) GO TO 710
709  CCNTINUE
710  AX4R=XW4(I)
      DG 711 I=1,NL
      IF(DABS((YW4(I+1)-YW4(I))/(XW4(I+1)-XW4(I))).GT.6.) GO TO 712
711  CCNTINUE
      I=NYL
712  AX4L=XW4(I)
303  CCNTINUE
C
C FIT PROFILES WITH CUBIC SPLINES
C RIGHT WHEEL SPLINE FIT
  CALL PRFLES(NWR,XW1,YW1,NJ1,XJ1,YJ1,1,AX1R,AX1R)
  CALL SPLINE(NJ1,XJ1,YJ1,SJ1,0)
C RIGHT RAIL SPLINE FIT
  CALL PRFLES(NYR,XW2,YW2,NJ2,XJ2,YJ2,C,AX2R,AX2L)
  CALL SPLINE(NJ2,XJ2,YJ2,SJ2,0)
C LEFT WHEEL SPLINE FIT
  CALL PRFLES(NWL,XW3,YW3,NJ3,XJ3,YJ3,1,AX3R,AX3R)
  CALL SPLINE(NJ3,XJ3,YJ3,SJ3,0)
C LEFT RAIL SPLINE FIT
  CALL PRFLES(NYL,XW4,YW4,NJ4,XJ4,YJ4,0,AX4R,AX4L)
  CALL SPLINE(NJ4,XJ4,YJ4,SJ4,0)
302  CCNTINUE
      IF(ICURV.EQ.1) GO TO 401
C
C INTERPOLATE ALONG SPLINE FITS TO FIND PRFLE CRV AT THE CONTACT PT LCC
C CURVATURES ARE POSITIVE IF CENTER OF CURVATURE IS WITHIN BODY
  DO 304 I=1,NUMBR
    CALL SPIC(NJ1,XJ1,YJ1,SJ1,AX1(I),AR1C(I))
    CALL SPIC(NJ2,XJ2,YJ2,SJ2,AX2(I),AR2C(I))
    CALL SPIC(NJ3,XJ3,YJ3,SJ3,AX3(I),AR3C(I))
    CALL SPIC(NJ4,XJ4,YJ4,SJ4,AX4(I),AR4C(I))
304  CCNTINUE
C
  PRINT 820
820  FORMAT('1(RL-RR)/2A = NORMALIZED DIFFERENCE IN ROLLING RADII (IN/I
IN)'/
1' (ML-MR)/2 = NORMALIZED DIFFERENCE IN CONTACT ANGLES (RAD)'/
1' WR = WHEELSET ROLL ANGLE W.R.T. HCRIZCNTAL, POSITIVE UP O
IN LEFT (RAD)'/
1' YCG = VERTICAL DISPLACEMENT OF WHEELSET CENTROID FROM NOMI
INAL PGS. (IN)')
  PRINT 830
830  FORMAT(' CWR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT WHEE
IL PROFILE,*/13X,' POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)'/
1' CYR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT RAIL PROFILE
1,*/13X,' POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)'/
1' CWL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT WHEEL PROFILE
1,*/13X,' POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)'/
1' CYL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT RAIL PROFILE,
1' /13X,' POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)'/)
  PRINT 255
255  FORMAT( 4X,'XW',4X,'(RL-RR)/2A',1X,'(ML-MR)/2',
1 6X,'WR',8X,'YCG',8X,'CWR',8X,'CYR',8X,'CWL',8X,'CYL'
1 3X,'(IN)',4X,'(1N/IN)',5X,'(RAD)',7X,'(RAD)',8X,
1 '(IN)',6X,4(' (1/IN)',5X)'/)
  DO 256 I=1,NUMBR
    PRINT 260,AXW(I),AR5(I),AM3(I),AW1(I),AY1(I),
1 AR1C(I),AR2C(I),AR3C(I),AR4C(I)
256  CCNTINUE
260  FORMAT(2X,F6.3,8F11.6)
C
  IF(IPLT.EQ.0) GO TO 265
C PLCT THE C.P. LOCATIONS AND THE GEOMETRIC CCNSTRANT RELATIONS
  CALL PLOT2(NUMBR,ICTR,ICTL)
C PLCTTR CONTROL CARD, VARIES WITH COMPUTER
  CALL PLOT(J,J,999)

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C
265  CONTINUE
    IF(IPUNCH.NE.1) GO TO 400
C CLPUT RESULTS ON CARDS
    PUNCH 345, WG, AW, RG, AR, BR, BL
    PUNCH 18
18   FORMAT(/' COEFFICIENTS FOR PROFILE CURVE FITS')
    PUNCH 19, (1WHLR(I), I=1, 13)
19   FCRMAT(/13A4)
    PUNCH 335, NC1
    DO 322 I=1, NC1
    PUNCH 340, I, (RR(I, J), J=1, 5), B1(I, 1), B1(I, 2)
322  CONTINUE
    PUNCH 19, (IRAILR(I), I=1, 13)
    PUNCH 335, NC2
    DO 323 I=1, NC2
    PUNCH 340, I, (YR(I, J), J=1, 5), B2(I, 1), B2(I, 2)
323  CONTINUE
    PUNCH 19, (1WHLL(I), I=1, 13)
    PUNCH 335, NC3
    DO 324 I=1, NC3
    PUNCH 340, I, (RL(I, J), J=1, 5), B3(I, 1), B3(I, 2)
324  CONTINUE
    PUNCH 19, (IRAILL(I), I=1, 13)
    PUNCH 335, NC4
    DO 325 I=1, NC4
    PUNCH 340, I, (YL(I, J), J=1, 5), B4(I, 1), B4(I, 2)
325  CONTINUE
    PUNCH 398
398  FORMAT(/' THE DATA IS ORDERED AS FOLLOWS: '/')
    PUNCH 810
    PUNCH 820
    PUNCH 815
    PUNCH 830
    PUNCH 30, NUMBR, INC
    PUNCH 330, (AXW(I), AX1(I), AX2(I), AX3(I), AX4(I), AR1(I), AR2(I),
1 AR3(I), AR4(I), AM1(I), AM2(I), AR5(I), AM3(I), AW1(I), AY1(I),
1 ARRIC(I), ARRC(I), ARIC(I), AR2C(I), AR3C(I), AR4C(I), I=1, NUMBR)
330  FORMAT(6E13.6/6E13.6/3E13.6/6E13.6)
335  FORMAT(13)
340  FORMAT(13, 5E13.6/2E13.6)
345  FCRMAT(6E12.5)
400  CONTINUE
C
C COMPUTE DESCRIBING FUNCTIONS OF SOME OF THE RELATIONS AND PRINT
C RESULTS. ONLY VALID FOR SYMMETRICAL CASE.
    IF(ISYM.NE.1) GO TO 401
    CALL DCRFN(NUMBR, AXW, AR5, AM3, AW1, AR)
401  CONTINUE
C
C PRINT CURVATURES AT EQUAL INTERVALS ALONG PROFILES
    XI05(1) = -3.50 DO
    DO 410 I = 2, 140
410  XI05(I) = XI05(I-1) + 0.05 DO
C ZERO OUT AX1, ..., AX4 ARRAYS TO REUSE
    DO 411 I=1, 244
    AX1(I)=0.000
    AX2(I)=0.000
    AX3(I)=0.000
    AX4(I)=0.000
411  CONTINUE
C FIND POINTS AT 0.05" INCREMENTS ALONG PROFILES
    CALL PRFLEP(NWR, XW1, XI05, AX1)
    CALL PRFLEP(NYR, XW2, XI05, AX2)
    CALL PRFLEP(NWL, XW3, XI05, AX3)
    CALL PRFLEP(NYL, XW4, XI05, AX4)
C INTERPOLATE TO FIND PRFLE CRV'S AT THESE POINTS
    DC 412 I = 1, NWR
412  CALL SPIC(NJ1, XJ1, YJ1, SJ1, AX1(I), ARIC(I))
    DO 414 I = 1, NYR
414  CALL SPIC(NJ2, XJ2, YJ2, SJ2, AX2(I), AR2C(I))
    DC 416 I = 1, NWL

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416 CALL SPIC(NJ3,XJ3,YJ3,SJ3,AX3(I),AR3C(I))
    DC 418 I = 1,NYL
418 CALL SPIC(NJ4,XJ4,YJ4,SJ4,AX4(I),AR4C(I))
C ZERC OUT UNUSED PORTION OF CURVATURE ARRAYS
    DC 420 I = 1,100
    AR1C(NWR + I) = 0.000
    AR2C(NYR + I) = 0.000
    AR3C(NWL + I) = 0.000
    AR4C(NYL + I) = 0.000
420 CCNTINUE
C PRINT OUT PROFILE CURVATURE ARRAYS
    N = NWR
    IF(NYR.GT.N) N = NYR
    IF(NWL.GT.N) N = NWL
    IF(NYL.GT.N) N = NYL
    PRINT 840
840 FORMAT('PROFILE PRINCIPAL TRANSVERSE CURVATURES (1/IN)')//
1' XWR= LOCATION ON RIGHT WHEEL, POSITIVE OUT FROM TAPELINE (IN)'/
1' XRR= LOCATION ON RIGHT RAIL, POSITIVE OUT FROM CENTERLINE (IN)'/
1' XLW= LOCATION ON LEFT WHEEL, POSITIVE OUT FROM TAPELINE (IN)'/
1' XRL= LOCATION ON LEFT RAIL, POSITIVE OUT FROM CENTERLINE (IN)'/
    PRINT 830
    PRINT 430
430 FORMAT(/6X,'XWR',7X,'CWR',9X,'XRR',7X,'CYR',
1 9X,'XLW',7X,'CWL',9X,'XRL',7X,'CYL')/
1 6X,'(IN)',5X,'(1/IN)',3(7X,'(IN)',5X,'(1/IN)')//
    PRINT 440,(AX1(I),AR1C(I),AX2(I),AR2C(I),
1 AX3(I),AR3C(I),AX4(I),AR4C(I),I=1,N)
440 FORMAT(4(3X,F8.5,F11.6))
    STOP
    END

```

```

SUBROUTINE PRFLE(NW,XW,YW,NC,RR,XB,INC,IW)
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION XW(1),YW(1),RR(30,1),XB(30,1),
1 F1(200),F2(200),F3(200),SS(5)
DIMENSION XJ(1),YJ(1)
DIMENSION XI(1),AX(1)
COMMON /COMB/ YWIM,IFLANG

C
C INPUT
C NW=NC OF DATA PTS
C DATA MUST BE IN ORDER STARTING WITH POSITIVE X
C ITWO=1 FOR TWO (X,Y) COORDINATES PER INPUT CARD
C INEG=1 FOR CHANGING SIGN OF INPUT Y COORDINATE
C IW = 0 IS RAIL, IW = 1 IS RT WHEEL, IW = 2 IS LT WHEEL
10 FORMAT(1X,3I3)
15 FORMAT(10X,2D15.7)
   READ(1,*) NW
   WRITE(3,10) NW
C DECIDE WHICH FORMAT FOR INPUT CARDS
   READ(1,*) ITWO, INEG
21   WRITE(3,*) ITWO, INEG
   IF(ITWO.EQ.1) GO TO 3
   READ 15, (XW(I), YW(I), I=1, NW)
   GO TO 6
3   DO 4 I=1, NW, 2
   M=I+1
4   READ(1,*) XW(I), YW(I), XW(M), YW(M)
   IF(INEG.NE.1) GO TO 6
   DO 7 I=1, NW
7   YW(I)=-YW(I)
6   CONTINUE
C CHECK IF PRFLE CARDS ARE IN ORDER
   NW1 = NW - 1
   DO 31 I = 1, NW1
   IF(XW(I+1).GT.XW(I))GO TO 32
31  CONTINUE
   GO TO 34
32  JJ=I+1
   WRITE(3,33) XW(JJ)
33  FORMAT(/25('**'), ' WARNING ', 25('**')/
1 5('**'), ' PROFILE INPUT CARDS NOT IN DECENDING ',
2'ORDER AT X COORDINATE = ', F12.6, 5('**')/
3 5('**'), ' INVALID CURVE FIT IN THE CURVE FIT REGION CONTAINING ',
4'THAT POINT ', 5('**')//)
34  CONTINUE
   IF(IFLANG.NE.1) GO TO 17
   IF(IW.NE.2) GO TO 17
C FOR ASYMMETRIC CASE, MAKE TOP OF FLANGE ON LT WH = RT WH
C FIND TOP OF FLANGE OF LT WHEEL
   YW3M = YW(1)
   DO 13 I = 2, NW
   IF(YW(I) - YW3M) 13, 13, 12
12  YW3M = YW(I)
13  CONTINUE
C ADJUST LT WH DATA AND PRINT NOTE
   YWD = YWIM - YW3M
   DO 14 I = 1, NW
14  YW(I) = YW(I) + YWD
   WRITE(3,16) YWD
16  FORMAT(' TO EQUATE TOP OF WHEEL FLANGES ON LEFT ',
1'AND RIGHT, LEFT WHEEL ROLLING RADIUS DATA HAVE BEEN ',
1'ADJUSTED BY', F11.6, ' INCH')
17  CONTINUE
   WRITE(3,19) (1, XW(I), YW(I), I=1, NW)
19  FORMAT(14, 4X, 2D15.7)
C DECIDE THE NO OF CURVE FITS, NC, TO USE
C FIT A CURVE EVERY INC DATA PTS
   NC=NW/INC
   IF((NW-INC*NC).GE.3)NC=NC+1
   IF(NC.LT.3) PRINT 18
18 FORMAT(2X, '*** ERROR *** TOO LARGE AN INCREMENT OR NOT ENOUGH DATA
1 PTS')

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```

C   FIT FIRST CURVE
C   XB(I,1)=UPPER LIMIT OF CURVEFIT
C   XB(I,2)=LOWER LIMIT
      XE(1,1)=200.
      XE(1,2)=XW(INC)
      J=INC+3
      DC 20 I=1,J
      F1(I)=XW(I)
      F2(I)=YW(I)
.20  CCNTINUE
      CALL CRVFT(J,J,F1,F2,F3,SS)
      DC 25 I=1,5
      RR(1,I)=SS(I)
.25  CCNTINUE
C   FIT OTHER CURVES
      NC1=NC-1
      DO 100 II=2,NC1
      J=II-1
      XB(II,1)=XB(J,2)
      J=INC*II
      XB(II,2)=XW(J)
      J=(II-1)*INC-2
      K=II*INC+3
      L=0
      DC 40 I=J,K
      L=L+1
      F1(L)=XW(I)
      F2(L)=YW(I)
.40  CCNTINUE
      CALL CRVFT(L,0,F1,F2,F3,SS)
      DC 45 I=1,5
      RR(II,I)=SS(I)
.45  CCNTINUE
.100 CCNTINUE
C   FIT LAST CURVE
      XB(NC,1)=XB(NC1,2)
      XB(NC,2)=XW(NW)
      K=0
      J=NC1*INC-2
      DO 150 I=J,NW
      K=K+1
      F1(K)=XW(I)
      F2(K)=YW(I)
.150 CCNTINUE
      CALL CRVFT(K,0,F1,F2,F3,SS)
      DC 155 I=1,5
      RR(NC,I)=SS(I)
.155 CCNTINUE
      RETURN
C
C   SET UP JT ARRAYS FOR SPLINE FIT CALC OF RAD OF CURV
C
C   ENTRY PRFLES(NP,XW,YW,NJ,XJ,YJ,IW,XR,XL)
C   REARRANGE PRFLE PTS SO THAT XW(I) < XW(I+1)
C   F1,F2 USED AS TEMP STORAGE ARRAYS
      DC 50 I=1,NP
      J = 1 + NP - I
      F1(I) = XW(J)
.50  F2(I) = YW(J)
      DC 55 I=1,NP
      XW(I) = F1(I)
.55  YW(I) = F2(I)
C
C   IF(IW.EQ.0) GO TO 80
C   TOP OF FLANGE SEARCH
      YWM=YW(1)
      M=1
      DC 65 I=2,NP
      IF(YW(I)-YWM) 65,65,60
.60  YWM=YW(I)
      XWM=XW(I)
      M=I

```

```

65  CCNTINUE
C USE ONLY CONTACT PORTION OF WHEEL PROFILE FOR SPLINE FIT
DC 70 I=1, NP
XW(I)=XW(M)
YW(I)=YW(M)
IF(XW(I).GE.XW(NP)) GO TO 75
IF(XW(I).GT.XR.AND.XW(I).GT.2.00) GO TO 75
70  M=M+1
75  NP=I
C SPECIFY REGIONS AND INCREMENTS ALONG WHEEL PRFLE TO PLACE JOINTS
XREG1=-1.6000
XREG2=-J.9500
XJINC1=0.1500
XJINC2=0.3000
XJINC3=0.5000
GC TO 99
C USE ONLY CONTACT PORTION OF RAIL PROFILE FOR SPLINE FIT
80  DC 85 I=1, NP
IF(XL.LT.XW(I)) GO TO 90
85  CCNTINUE
90  L=I-1
DC 95 I=1, NP
XW(I)=XW(L)
YW(I)=YW(L)
IF(XW(I).GE.XW(NP)) GO TO 96
IF(XW(I).GT.XR.AND.XW(I).GT.1.00) GO TO 96
95  L=L+1
96  NP=I
C SPECIFY REGIONS AND INCREMENTS ALONG RAIL PROFILE TO PLACE JOINTS
XREG1=-1.2000
XREG2=-0.7000
XJINC1=0.1000
XJINC2=0.2000
XJINC3=0.4000
C
99  CCNTINUE
NP1=NP+1
DC 101 I=NP1, 200
XW(I)=J.000
YW(I)=0.000
101
C
C SET UP SPLINE JOINT COORDINATES
DO 106 I=1, 99
XJ(I)=J.000
106 YJ(I)=0.000
J=1
DC 110 I=1, NP
XJ(I)=XW(J)
YJ(I)=YW(J)
XJNEXT=XJ(I)+XJINC1
IF(XJNEXT.GE.XREG1) XJNEXT=XJ(I)+XJINC2
IF(XJNEXT.GE.XREG2) XJNEXT=XJ(I)+XJINC3
IF(XJNEXT.GE.XW(NP)) GO TO 120
SMDIF=100.
DC 116 K=1, NP
DIFXJ=DABS(XW(J+K)-XJNEXT)
IF(DIFXJ-SMDIF) 115, 117, 117
115 SMDIF=DIFXJ
116 CCNTINUE
117 J=J+K-1
118 CCNTINUE
119 K=I+1
120 IF(XJ(I).EQ.XW(NP)) K=I
XJ(K)=XW(NP)
YJ(K)=YW(NP)
NJ=K
RETURN
C

```

C SET UP X PRINT ARRAY FOR FINAL PRT OF PRFLE CRV

```

C
  ENTRY PRFLEP(NP,XW,XI,AX)
  DO 151 I = 1,140
  IF(XW(I).LE.XI(I)) GO TO 160
151  CCNTINUE
160  AX(I) = XW(I)
  DO 170 J = 2,140
  AX(J) = XI(I)
  IF(AX(J).GE.XW(NP)) GO TO 180
170  I = I + 1
180  AX(J) = XW(NP)
  NP = J
  RETURN
  END

```

```

SUBROUTINE CRVFT(N,L,X,Y,W,A)
  IMPLICIT REAL*8(A-H,O-Z)
  DIMENSION X(1),Y(1),W(1),A(1)
  DIMENSION C(5),ALPHA(4),BETA(4),T1(402),T2(402),T3(402)
  J=0
  K=4
C FIT CURVE
  CALL ORTHLS(X,Y,W,N,L,J,C,ALPHA,BETA,K,T1,T2,T3,IND1)
C GET COEFFICIENTS OF THE CURVE
  CALL COEFS(J,C,ALPHA,BETA,K,A,T1,T2,T3,IND2)
  RETURN
  END

```

```

SUBROUTINE ORTHLS (X,Y,W,N,L,J,C,ALPHA,BETA,K,T1,T2,T3,IND1)
  IMPLICIT REAL*8(A-F,O-Z)
C-----
C THIS SUBROUTINE COMPUTES THE COEFFICIENTS OF THE POLYNOMIAL
C EQUATION OF DEGREE K AND THE ALPHA AND BETA PARAMETERS.
C-----
C DIMENSION X(N),Y(N),W(N),C(K),ALPHA(K),BETA(K),T1(N),T2(N),T3(N)
C-----
C PROGRAM INITIALIZATION.
C-----
      KJ1=K-J+1
      IF (KJ1.LE.0) GO TO 16
      SUM=0.0
      IF (L.EQ.1) GO TO 3
      DO 2 I=1,N
        T3(I)=X(I)
      IF (J.GT.0) GO TO 1
      SUM=SUM+1.0
      GO TO 2
1     SUM=SUM+X(I)**(2*J)
2     W(I)=1.0
      GO TO 7
3     DO 6 I=1,N
        T3(I)=X(I)
      IF (J.GT.0) GO TO 4
      SUM=SUM+W(I)
      GO TO 5
4     SUM=SUM+W(I)*X(I)**(2*J)
5     X(I)=W(I)*X(I)
6     Y(I)=W(I)*Y(I)
7     B=0.0
      RC=SUM
      DO 9 I=1,N
      IF (J.GT.0) GO TO 8
      T2(I)=1.0
      GO TO 9
8     T2(I)=T3(I)**J
9     T1(I)=0.0
C-----
C BEGIN COMPUTATION.
C-----
      II=1
10    S=0.0
      DO 11 I=1,N
11    S=S+Y(I)*T2(I)
C-----
C COMPUTATION OF A COEFFICIENT IN THE POLYNOMIAL EQUATION.
C-----
      C(II)=S/RO
      IF (II.GE.KJ1) GO TO 15
C-----
C COMPUTATION OF AN ALPHA FOR THE POLYNOMIAL EQUATION.
C-----
      SUMXPS=0.0
      DO 12 I=1,N
12    SUMXPS=SUMXPS+X(I)*T2(I)*T2(I)
      ALPHA(II)=SUMXPS/RC
C-----
C COMPUTATION OF A NEW POLYNOMIAL.
C-----
      DO 13 I=1,N
      TEMP=T2(I)
      T2(I)=(T3(I)-ALPHA(II))*T2(I)-B*T1(I)
13    T1(I)=TEMP
C-----
C COMPUTATION OF A BETA FOR THE POLYNOMIAL EQUATION.
C-----
      R=0.0
      DO 14 I=1,N
14    R=R+W(I)*T2(I)*T2(I)
      BETA(II)=K/RO
      RC=R

```

```
B=BETA(II)  
II=II+1  
GO TO 10
```

```
C-----  
C SUCCESSFUL RETURN.  
C-----
```

```
15 INDI=+1  
RETURN
```

```
C-----  
C ERROR RETURN. SET ALL C COEFFICIENTS, ALPHA AND BETA TO ZERO.  
C-----
```

```
16 DG 17 II=1,K  
C(II)=0.0  
ALPHA(II)=0.0  
17 BETA(II)=0.0  
C(K+1)=0.0  
INDI=-1  
RETURN  
END
```

SUBROUTINE COEFS (J,C,ALPHA,BETA,KC,A,T1,T2,T3,IND2)
 IMPLICIT REAL*8(A-H,O-Z)

```

C-----
C THIS SUBROUTINE COMPUTES THE A COEFFICIENTS FOR A POLYNOMIAL
C OF DEGREE KC WHERE KC IS LESS THAN OR EQUAL TO K.
C-----
C DIMENSION C(KC),ALPHA(KC),BETA(KC),A(KC),T1(KC),T2(KC),T3(KC)
C-----
C PROGRAM INITIALIZATION.
C-----
C KCJ1=KC-J+1
C IF(KCJ1.LE.0) GO TO 9
C B=0.0
C DO 1 NN=1,KCJ1
C A(NN)=C(NN)
C T1(NN)=0.0
C T2(NN)=0.0
C 1 T3(NN)=0.0
C IF (KC.LE.J) GO TO 5
C II=2
C-----
C BEGIN COMPUTATION.
C-----
C 2 T2(II)=1.0
C DO 3 NN=2,II
C T3(NN)=T2(NN-1)-T2(NN)*ALPHA(II-1)-B*T1(NN)
C-----
C COMPUTATION OF AN A COEFFICIENT.
C-----
C 3 A(NN-1)=A(NN-1)+C(II)*T3(NN)
C IF (II.GE.KCJ1) GO TO 5
C-----
C RESETTING THE VECTORS FOR THE NEXT COEFFICIENT.
C-----
C DO 4 NN=1,II
C T1(NN)=T2(NN)
C 4 T2(NN)=T3(NN)
C B=BETA(II-1)
C II=II+1
C GO TO 2
C 5 IF (J.LE.0) GO TO 8
C-----
C ARRANGE COEFFICIENTS PROPERLY IF J IS NON ZERO.
C-----
C DO 6 NN=1,KCJ1
C N1=KCJ1-NN+1
C N2=N1+J
C 6 A(N2)=A(N1)
C DO 7 NN=1,J
C 7 A(NN)=0.0
C-----
C SUCCESSFUL RETURN.
C-----
C 8 IND2=+2
C RETURN
C-----
C ERROR RETURN. SET ALL THE A COEFFICIENTS EQUAL TO ZERO.
C-----
C 9 DO 10 NN=1,KC
C 10 A(NN)=0.0
C A(KC+1)=0.0
C IND2=-2
C RETURN
C END

```

SUBROUTINE PLOT1(ICTR,ICTL,IWG,IRG)
 IMPLICIT REAL*8(A-H,O-Z)

C
 REAL SAXW(244),SAX1(244),SAX2(244),SAX3(244),SAX4(244),
 1 SXW1(244),SXW2(244),SXW3(244),SXW4(244),
 1 SYW1(244),SYW2(244),SYW3(244),SYW4(244),
 1 SAR1(244),SAR2(244),SAR3(244),SAR4(244)
 COMMON /CUMA/ AW,AR,BR,BL,RR(30,5),YR(30,5),RL(30,5),YL(30,5),
 1 B1(30,2),B2(30,2),B3(30,2),B4(30,2),S1(5),S2(5),S3(5),S4(5),
 1 AXW(244),AX1(244),AX2(244),AX3(244),AX4(244),AR1(244),AR2(244),
 1 AR3(244),AR4(244),AR5(244),AM1(244),AM2(244),AM3(244),AW1(244),
 1 AY1(244),NC1,NC2,NC3,NC4
 DIMENSION ICTR(13),ICTL(13),IWG(13),IRG(13)

C
 COMMON /COMC/ IWHLR(13),IWHLL(13),IRAILR(13),IRAILL(13)

C
 COMMON /CMD/ XW1(200),YW1(200),XW2(200),YW2(200),NWR,NYR,
 1 XW3(200),YW3(200),XW4(200),YW4(200),NWL,NYL

C
 C CALCULATE AN ARRAY OF PTS FROM POLYNOMIALS FIT TO WHEEL PROFILE

CALL GTPTS(XW1(1),XW1(NWR),RR,B1,NC1,AX1,AR1,S1,NUR)

CALL GTPTS(XW3(1),XW3(NWL),RL,B3,NC3,AX3,AR3,S3,NUL)

C
 C CALCULATE AN ARRAY OF PTS FROM POLYNOMIALS FIT TO RAIL PROFILE

CALL GTPTS(XW2(1),XW2(NYR),YR,B2,NC2,AX2,AR2,S2,NBR)

CALL GTPTS(XW4(1),XW4(NYL),YL,B4,NC4,AX4,AR4,S4,NBL)

C
 C DEFINE STARTING AND DELTX VALUES FOR PLCTS

NWR1=NWR+1

NWR2=NWR+2

NYR1=NYR+1

NYR2=NYR+2

NWL1=NWL+1

NWL2=NWL+2

NYL1=NYL+1

NYL2=NYL+2

XW1(NWR1)=0.

YW1(NWR1)=0.

XW2(NYR1)=0.

YW2(NYR1)=0.

XW1(NWR2)=1.

YW1(NWR2)=1.

XW2(NYR2)=1.

YW2(NYR2)=1.

XW3(NWL1)=0.

YW3(NWL1)=0.

XW4(NYL1)=0.

YW4(NYL1)=0.

XW3(NWL2)=1.

YW3(NWL2)=1.

XW4(NYL2)=1.

YW4(NYL2)=1.

NBR1=NBR+1

NBR2=NBR+2

NUR1=NUR+1

NUR2=NUR+2

NUL1=NUL+1

NUL2=NUL+2

NBL1=NBL+1

NBL2=NBL+2

AX1(NUR1)=0.

AR1(NUR1)=0.

AR2(NBR1)=0.

AX2(NBR1)=0.

AX1(NUR2)=1.

AR1(NUR2)=-1.

AR2(NBR2)=1.

AX2(NBR2)=1.

AX3(NUL1)=0.

AR3(NUL1)=0.

AR4(NBL1)=0.

AX4(NBL1)=0.

AX3(NUL2)=1.

```

AR3(NBL2)=-1.
AR4(NBL2)=1.
AX4(NBL2)=1
C
C SUBTRACT CONSTANT TERMS FROM DATA POINTS TO REDUCE MAGNITUDES
CSTW=DBLE((AINT(SNGL(AR1(NUR/2)*10.)))/10.)
CSTR=DBLE((AINT(SNGL(AR2(NBR/2)*10.)))/10.)
DO 10 I=1,NUR
  AR1(I)=AR1(I)-CSTW
10 CONTINUE
DO 11 I=1,NUL
  AR3(I)=AR3(I)-CSTW
11 CONTINUE
DO 15 I=1,NBR
  AR2(I)=AR2(I)-CSTR
15 CONTINUE
DO 16 I=1,NBL
  AR4(I)=AR4(I)-CSTR
16 CONTINUE
DO 20 I=1,NWR
  YW1(I)=-YW1(I)+CSTW
20 CONTINUE
DO 21 I=1,NWL
  YW3(I)=-YW3(I)+CSTW
21 CONTINUE
DO 30 I=1,NYR
  YW2(I)=YW2(I)-CSTR
30 CONTINUE
DO 31 I=1,NYL
  YW4(I)=YW4(I)-CSTR
31 CONTINUE
C
C ** CHANGE DOUBLE PRECISION ARRAYS TO SINGLE PRECISION FOR PLOTTING
DO 40 I=1,244
  SAXW(I)=SNGL(AXW(I))
  SAX1(I)=SNGL(AX1(I))
  SAX2(I)=SNGL(AX2(I))
  SAX3(I)=SNGL(AX3(I))
  SAX4(I)=SNGL(AX4(I))
  SAR1(I)=SNGL(AR1(I))
  SAR2(I)=SNGL(AR2(I))
  SAR3(I)=SNGL(AR3(I))
  SAR4(I)=SNGL(AR4(I))
40 CONTINUE
DO 50 I=1,200
  SXW1(I)=SNGL(XW1(I))
  SXW2(I)=SNGL(XW2(I))
  SXW3(I)=SNGL(XW3(I))
  SXW4(I)=SNGL(XW4(I))
  SYW1(I)=SNGL(YW1(I))
  SYW2(I)=SNGL(YW2(I))
  SYW3(I)=SNGL(YW3(I))
  SYW4(I)=SNGL(YW4(I))
50 CONTINUE
C PLOT THE PROFILES AND LABEL THEM
CALL PLOT(39.,17.5,-3)
CALL AXIS(-2.,.75,1,'RIGHT WHEEL',-11.4,.0,-2.,1.)
CALL LINE(SAX1,SAR1,NUR,1,0,3)
CALL LINE(SXW1,SYW1,NWR,1,-2,3)
CALL SYMBOL(-2.,-.4,.14,IWHLR,0.,52)
CALL PLOT(5.5,0,-3)
CALL AXIS(-2.,.75,1,'RIGHT RAIL',-10.4,.0,-2.,1.)
CALL LINE(SAX2,SAR2,NBR,1,0,3)
CALL LINE(SXW2,SYW2,NYR,1,-2,3)
CALL SYMBOL(-2.,-.4,.14,IRAILR,0.,52)
CALL SYMBOL(-6.0,-1.4,.14,IWG,0.,52)
CALL SYMBOL(-6.0,-1.63,.14,IRG,0.,52)
CALL NUMBER(-4.0,-1.63,.14,RC,0.,2)
CALL SYMBOL(-2.48,-1.4,.14,ICTR,0.,52)
CALL PLOT(-5.5,-13.25,-3)
CALL AXIS(-2.,.75,1,'LEFT WHEEL',-10.4,.0,-2.,1.)
CALL LINE(SAX3,SAR3,NUL,1,0,3)

```



```

CALL LINE(SXW3,SYW3,NWL,1,-2,3)
CALL SYMBOL(-2.,-4.,14,IWHL,0.,52)
CALL PLOT(5.5,0.,-3)
CALL AXIS(-2.,.75,'LEFT RAIL',-9,4.,C.,-2.,1.)
CALL LINE(SAX4,SAR4,NBL,1,0,3)
CALL LINE(SXW4,SYW4,NYL,1,-2,3)
CALL SYMBOL(-2.,-4.,14,IRAIL,0.,52)
CALL SYMBOL(-2.48,-1.4,14,ICTL,C.,52)
CALL PLOT(-44.5,-4.25,-3)
DO 60 I=1,NWR
60 YW1(I)=-YW1(I)+CSTW
DO 61 I=1,NWL
61 YW3(I)=-YW3(I)+CSTW
DO 70 I=1,NYR
70 YW2(I)=YW2(I)+CSTR
DO 71 I=1,NYL
71 YW4(I)=YW4(I)+CSTR
RETURN
END

```

```

SUBROUTINE GTPIS(XMAX,XMIN,RR,B,NC,AXW,ARI,S1,NU)
IMPLICIT REAL*8(A-H,C-Z)
DIMENSION AXW(1),ARI(1),S1(1),RR(30,1),B(30,1)
C DEFINE STARTING VALUES
X=XMAX
IJ=1
C LOOP TO FIND EACH PT.
DO 6 I=1,400
NU=I
C CHOOSE THE POLYNOMIAL VALID FOR THE SPECIFIC X
DO 2 J=1,NC
IF(B(J,2).LE.X.AND.B(J,1).GT.X) GO TO 2
2 CONTINUE
3 IJ=J
C STORE THE POLY COEFS
DO 4 K=1,5
S1(K)=RR(IJ,K)
4 CONTINUE
AXW(I)=X
C CALCULATE THE Y VALUE
ARI(1)=S1(1)+S1(2)*X+S1(3)*X**2+S1(4)*X**3+S1(5)*X**4
C INCREMENT X BY -.025 INCHES
X=X-.025
C CHECK FOR END OF PROFILE
IF(X.LT.XMIN) GO TO 7
6 CONTINUE
7 CONTINUE
RETURN
END

```

```

SUBROUTINE EQSOLV(NUMBR,XWINC)
  IMPLICIT REAL*8(A-F,C-Z)
  COMMON /COMA/ AW,AR,BR,BL,RR(30,5),YR(30,5),RL(30,5),YL(30,5),
  1 B1(30,2),B2(30,2),B3(30,2),B4(30,2),S1(5),S2(5),S3(5),S4(5),
  1 AXW(244),AX1(244),AX2(244),AX3(244),AX4(244),AR1(244),AR2(244),
  1 AR3(244),AR4(244),AR5(244),AM1(244),AM2(244),AM3(244),AW1(244),
  1 AY1(244),NC1,NC2,NC3,NC4,ISYM
  COMMON /COMF/ M1,M2,M3,M4,M5,M6,STEP,IPRT
  COMMON /COMH/ IFLAG,IFLAGA

C
C   DIMENSION XOLD(4)
C   INITIALIZE WHEELSET DISPLACEMENT, INCREMENTS OF DISPLACEMENT, AND ROLL
  XW=0.
  XWI=0.
  WR=0.
  IFLAG=0
  IFLAGA=J

C   COMPUTE 1/2 THE NUMBER OF DATA PTS DESIRED
  NHALF=NUMBR/2

C   COMPUTE C.P. LOCATIONS AS WHEELSET IS LATERED INCREMENTALLY IN THE
C   POSITIVE DIRECTION
  ISTART=NHALF+1
  DO 250 NUMB=ISTART,NUMBR

C   ROUTINE THAT FINDS CONTACT PT LOCATIONS
  CALL CHECK(XW,XWI,WR,XOLD)

C   XW IS INCREMENTED WITHIN CHECK
  M3=5
  IF(XW.LE.0.45) M3=10
  IF(XW.LE.0.15) M3=12

C   STORE CONTACT PTS AND WHEELSET LATERAL
  AXW(NUMB)=XW
  AX1(NUMB)=XOLD(1)
  AX2(NUMB)=XOLD(2)
  AX3(NUMB)=XOLD(3)
  AX4(NUMB)=XOLD(4)
  IF(IPRT.EQ.1.OR.IPRT.EQ.2) WRITE(3,1) (XOLD(J),J=1,4)

C   XWI=SIZE OF WHEELSET LATERAL INCREMENTS
  XWI=XWINC

250 CONTINUE

C   FOR SYMMETRIC CASE FORCE SAME VALUES AT XW=C.
  IF(ISYM.EQ.1) AX1(ISTART) = AX3(ISTART)
  IF(ISYM.EQ.1) AX2(ISTART) = AX4(ISTART)
1   FORMAT(/4F13.7)

C
C   CHECK FOR SYMMETRIC CASE
  IF(ISYM.EQ.1) GO TO 301

C
C   NEGATIVE DIRECTION
  XW=0.
  XWI=0.
  WR=0.
  IFLAG=0
  IFLAGA=1
  M1=M4
  M2=M5
  M3=M6
  M4=M1
  M5=M2
  M6=M3
  ISTART=NHALF
  DO 300 NUMB=1,ISTART
  CALL CHECK(XW,XWI,WR,XOLD)

C   XW IS INCREMENTED WITHIN CHECK
  M6=9
  IF(XW.GE.-.45) M6=10
  IF(XW.GE.-.15) M6=12

C   STORE CONTACT PTS AND WHEELSET LATERAL
  AXW(1-NUMB+ISTART)=XW
  AX1(1-NUMB+ISTART)=XOLD(1)
  AX2(1-NUMB+ISTART)=XOLD(2)
  AX3(1-NUMB+ISTART)=XOLD(3)
  AX4(1-NUMB+ISTART)=XOLD(4)

```

```
IF(IPRT.EQ.1.OR.IPRT.EQ.2) WRITE(3,1) (XCLD(J),J=1,4)
C XWI=SIZE OF WHEELSET LATERAL INCREMENTS
  XWI=-XWINC
300 CONTINUE
C FORCE SAME VALUES AT Xh = 0.
  AX1(NHALF+1)=AX1(NHALF)
  AX2(NHALF+1)=AX2(NHALF)
  AX3(NHALF+1)=AX3(NHALF)
  AX4(NHALF+1)=AX4(NHALF)
  RETURN
C
301 NUMB1=I START
  DO 311 NUMB=I START,NUMBR
    NUMB1=NUMB-1
    AXW(NUMB1)=-AXW(NUMB)
    AX1(NUMB1)=AX3(NUMB)
    AX2(NUMB1)=AX4(NUMB)
    AX3(NUMB1)=AX1(NUMB)
    AX4(NUMB1)=AX2(NUMB)
311 CONTINUE
  RETURN
  END
```

```

SUBROUTINE CHECK(XW,DXW,WR,XOLD)
IMPLICIT REAL*8(A-H,C-Z)
COMMON /CUMA/ AW,AR,BR,BL,RR(30,5),YR(30,5),RL(30,5),YL(30,5),
1 B1(30,2),B2(30,2),B3(30,2),B4(30,2),S1(5),S2(5),S3(5),S4(5),
1 Z(366J),NC1,NC2,NC3,NC4,ISYM
COMMON /CUME/ XMINWR,XMINRR,XMINWL,XMINFL,XMAXWR,XMAXRR,
1 XMAXWL,XMAXRL
COMMON /COMF/ M1,M2,M3,M4,M5,M6,STEP,IP
COMMON /COMG/ XXW,C,S
COMMON /CUMH/ IFLAG,IFLAGA
DIMENSION XOLD(1)

C
C INCREMENT WHEELSET LATERAL
XW=XW+DXW
XXW=XW
IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,3CC)XW
300 FORMAT(/'/: XW =',F8.4)
C FOR EACH INCREMENT OF XW, CHOOSE STARTING PTS
IF (IFLAG.EQ.1) GO TO 1
47 IF (A1.GT.-1.6) GO TO 48
A1 = XMINWR + 0.4
A1 = A1 + STEP
GO TO 47
48 CCNTINUE
A3 = A1
IFLAG = 1
STEPBK=10.*STEP
1 A1 = A1 + DXW - STEPBK
A3 = A3 - DXW - STEPBK
IF (A3.LT.XMINWL) A3 = XMINWL
SBR = DSIN(BR)
SBL = DSIN(BL)
SPI=1.000
SNI=-1.000
C ITERATION LOOP ON WHEELSET ROLL ANGLE
DO 120 IJK=1,8
IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,400)IJK
400 FORMAT(/'/: IJK =',I2/)
C CHOOSE PTS, ON INSIDE EDGES, FROM WHICH TO START SEARCH
AX1=A1
AX3=A3
C=DCOS(WR)
S=DSIN(WR)
C LOCATE INSIDE EDGE OF RT RAIL
DO 10 I=1,300
DO 11 J=1,NC1
IF (B1(I,2).LE.AX1) GO TO 12
11 CONTINUE
12 R1=RR(I,1)+AX1*(RR(I,2)+AX1*(RR(I,3)+AX1*(RR(I,4)+AX1*RR(I,5))))
AX2=-XW-AR+(AW+AX1)*C -R1*S
IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,500)I1,AX1,AX2
500 FORMAT(10,2(F9.4))
IF(AX2.GE.XMINRR) GO TO 15
10 AX1=AX1+STEP
15 CCNTINUE
IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,9CC)
900 FORMAT(' ')
C LOCATE INSIDE EDGE OF LT RAIL
DO 20 I=1,300
DO 21 J=1,NC3
IF (B3(I,2).LE.AX3) GO TO 22
21 CONTINUE
22 R3=RL(I,1)+AX3*(RL(I,2)+AX3*(RL(I,3)+AX3*(RL(I,4)+AX3*RL(I,5))))
AX4=XW-AR+(AW+AX3)*C +R3*S
IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,5CC)I1,AX3,AX4
IF(AX4.GE.XMINRL) GO TO 40
20 AX3=AX3+STEP
40 CCNTINUE
C SAVE CURRENT STARTING VALUES
A1=AX1
A3=AX3
C THREE INTERVAL FIBONACCI SEARCH TO FIND CANDIDATE CONTACT PTS

```

```

C M1,...M6 ARE CHANGED IN EQSOLV
C IFLAGA=1 FOR XW INCREMENTED IN NEG DIR
C FIND CONTACT POINT ON THE RIGHT
  CALL FIBON(M1,AX1,XMINWR,XMAXWR,XMINRR,XMAXRR,SBR,NC1,NC2,B1,B2,
  1 RR,YR,SN1,X1,X2,Y1)
  AX1=X1-0.65DO
  IF(IFLAGA.EQ.1) AX1=A1
  CALL FIBON(M2,AX1,XMINWR,XMAXWR,XMINRR,XMAXRR,SBR,NC1,NC2,B1,B2,
  1 RR,YR,SN1,X1A,X2A,Y1A)
  AX1=X1+0.10DO
  IF(IFLAGA.EQ.1) AX1=A1+1.5DO
  CALL FIBON(M3,AX1,XMINWR,XMAXWR,XMINRR,XMAXRR,SBR,NC1,NC2,B1,B2,
  1 RR,YR,SN1,X1B,X2B,Y1B)
  IF(Y1-Y1A) 2,2,4
  IF(Y1-Y1B) 6,6,3
2
3
  X1=X1B
  X2=X2B
  GO TO 6
4
  IF(Y1A-Y1B) 5,5,3
5
  X1=X1A
  X2=X2A
6
  CCNTINUE
C FIND CONTACT POINT ON THE LEFT
  CALL FIBON(M4,AX3,XMINWL,XMAXWL,XMINRL,XMAXRL,SBL,NC3,NC4,B3,B4,
  1 RL,YL,SP1,X3,X4,Y1)
  AX3=A3
  IF(IFLAGA.EQ.1) AX3=X3-0.65DO
  CALL FIBON(M5,AX3,XMINWL,XMAXWL,XMINRL,XMAXRL,SBL,NC3,NC4,B3,B4,
  1 RL,YL,SP1,X1A,X2A,Y1A)
  AX3=A3+1.5DO
  IF(IFLAGA.EQ.1) AX3=X3+0.10DO
  CALL FIBON(M6,AX3,XMINWL,XMAXWL,XMINRL,XMAXRL,SBL,NC3,NC4,B3,B4,
  1 RL,YL,SP1,X1B,X2B,Y1B)
  IF(Y1-Y1A) 7,7,9
  IF(Y1-Y1B) 19,19,8
7
8
  X3=X1B
  X4=X2B
  GO TO 19
9
  IF(Y1A-Y1B) 18,18,8
18
  X3=X1A
  X4=X2A
19
  CCNTINUE
200
  IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,200)X1,X2,X3,X4
  FORMAT(/4(F9.4)/)
C KEEP PREVIOUS ROLL ANGLE
  110 WR2=WR
C COMPUTE NEW ROLL ANGLE
  CALL CHOOSE(X1,X2,X3,X4)
  CALL RADII(S1,S2,S3,S4,X1,X2,X3,X4,R1,R2,R3,R4)
  WR=(R4-R2+X4*SBL -X2*SBR +(R3-R1)*C )/
  1 ((2.*AW+X1+X3)*C )
600
  IF(IP.EQ.1.OR.IP.EQ.2) WRITE(3,600) WR2,WR
  FORMAT(' WR2 = ',F15.7/' WR = ',F15.7)
C CHECK FOR CONVERGENCE BY COMPAIRING ROLL ANGLES
  IF(DABS(WR-WR2).LE..00001 ) GO TO 125
  120 CCNTINUE
  125 CCNTINUE
C ERROR CHECK
  ER=WR-WR2
  IF(IJK.GE.8) PRINT 130,ER,XW
  130 FORMAT( 4X,'*** WARNING *** WHEELSET ROLL ANGLE CONVERGED ONLY WI
  1THIN WR(NEW)-WR(OLD)=' ,F9.5,' AT XW=' ,F6.3)
C STORE THE CONTACT PT LOCATIONS
  XOLD(1)= X1
  XOLD(2)= X2
  XOLD(3)= X3
  XOLD(4)= X4
  RETURN
  END

```

```

SUBROUTINE CHOOSE(X1,X2,X3,X4)
  IMPLICIT REAL*8(A-H,C-Z)
  COMMON /COMA/ AW,AR,BR,BL,RR(30,5),YR(30,5),RL(30,5),YL(30,5),
  1 B1(30,2),B2(30,2),B3(30,2),B4(30,2),S1(5),S2(5),S3(5),S4(5),
  1 AXW(244),AX1(244),AX2(244),AX3(244),AX4(244),AR1(244),AR2(244),
  1 AR3(244),AR4(244),AR5(244),AM1(244),AM2(244),AM3(244),AW1(244),
  1 AY1(244),NC1,NC2,NC3,NC4
C
C CHOOSE THE CURVEFIT VALID FOR PT X1 ON THE RT WHEEL
  DO 20 I=1,NC1
    IF(B1(I,2).LE.X1) GO TO 25
  20 CONTINUE
  25 DO 30 J=1,5
    S1(J)=RR(I,J)
  30 CONTINUE
C
C CHOOSE THE CURVEFIT VALID FOR PT X2 ON THE RT RAIL
  DO 40 I=1,NC2
    IF(B2(I,2).LE.X2) GO TO 45
  40 CONTINUE
  45 DO 50 J=1,5
    S2(J)=YR(I,J)
  50 CONTINUE
C
C CHOOSE THE CURVEFIT VALID FOR PT X3 ON THE LEFT WHEEL
  DO 60 I=1,NC3
    IF(B3(I,2).LE.X3) GO TO 65
  60 CONTINUE
  65 DO 70 J=1,5
    S3(J)=RL(I,J)
  70 CONTINUE
C
C CHOOSE THE CURVEFIT VALID FOR PT X4 ON THE LEFT RAIL
  DO 80 I=1,NC4
    IF(B4(I,2).LE.X4) GO TO 85
  80 CONTINUE
  85 DO 90 J=1,5
    S4(J)=YL(I,J)
  90 CONTINUE
  RETURN
  END

```

```

SUBROUTINE RADII(KR,YR,RL,YL,X1,X2,X3,X4,R1,R2,R3,R4)
  IMPLICIT REAL*8(A-H,C-Z)
  DIMENSION RR(1),YR(1),RL(1),YL(1)
C COMPUTES THE VALUES OF FOUR 4TH ORDER POLYNOMIALS AT THE GIVEN
C PTS, RESPECTIVELY
  R1=RR(1)+X1*(RR(2)+X1*(RR(3)+X1*(RR(4)+X1*RR(5))))
  R2=YR(1)+X2*(YR(2)+X2*(YR(3)+X2*(YR(4)+X2*YR(5))))
  R3=RL(1)+X3*(RL(2)+X3*(RL(3)+X3*(RL(4)+X3*RL(5))))
  R4=YL(1)+X4*(YL(2)+X4*(YL(3)+X4*(YL(4)+X4*YL(5))))
  RETURN
  END

```

SUBROUTINE FIBON(N,AX,XMINW,XMAXW,XMINR,XMAXR,SBX,NCA,NCB,BA,BB,
1 R,Y,SIGN,X1,X2,Y1)

C FIBONACCI SEARCH TO FIND CONTACT POINTS.
C LOOKING FOR PROFILE PTS WITH MIN IN HGT BETWEEN WH & RAIL.
C
C N = N PT FIB SEARCH, AX = AX1,AX3, STEP = X INCREM ALONG WH PROFILE
C C = COS(WR), S = SIN(WR), SBX = SBL,SBR, SIGN = + OR - 1. IN EQNS
C 1) SIGN=-1. FOR AX1 CALLS, 2) SIGN=1. FOR AX3 CALLS: IP=PRINT FLAG
C ARRAYS: BA = B1,B3, BB = B2,B4, R = RR,RL, Y = YR,YL
C OUTPUT OF SUBR; CANDIDATE CONTACT PTS: X1 = X1,X3, X2 = X2,X4
C ; MINIMUM HEIGHT AT CONTACT PT = Y1
C

IMPLICIT REAL*8(A-H,O-Z)
DIMENSION F(15),BA(30,2),BB(30,2),R(30,5),Y(30,5)
COMMON /COMA/ AW,AR,BR,BL
COMMON /COMF/ M1,M2,M3,M4,M5,M6,STEP,IP
COMMON /COMG/ XW,C,S
DATA F/1.,2.,3.,5.,8.,13.,21.,34.,55.,89.,144.,
1 233.,377.,610.,987.7

C SKIP LINE FOR FIB SEARCH PRINTOUT
C IF(IP.NE.2) GO TO 601
600 WRITE(3,600)
601 FORMAT(' ')
CONTINUE

C SET UP FIRST FIBONACCI SEARCH INTERVAL
N1 = N - 1
XL = AX
XR = AX + F(N)*STEP
XFIB = F(N1)*STEP
X1 = XR - XFIB
X2 = XL + XFIB

C FIBONACCI SEARCH PROCEDURE, (N-1) INTERVALS
DO 100 IFIB = 2,N

C CALC FUNCTION VALUES (HEIGHTS)
C FOR THE LEFT FIBONACCI POINT, X1
IF(X1.GT.XMAXW)X1=XMAXW
IF(X1.LT.XMINW)X1=XMINW
DO 10 I = 1,NCA
IF (BA(I,2).LE.X1)GO TO 11

10 CONTINUE
11 R1 = R(I,1) + X1*(R(I,2) + X1*(R(I,3) + X1*(R(I,4) + X1*(R(I,5))))
XZ = SIGN*XW - AR + (AW+X1)*C + SIGN*R1*S
IF(XZ.GT.XMAXR) GO TO 15
IF(XZ.LT.XMINR) GO TO 15
DO 12 I = 1,NCB
IF (BB(I,2).LE.XZ) GO TO 13

12 CONTINUE
13 R2 = Y(I,1) + XZ*(Y(I,2) + XZ*(Y(I,3) + XZ*(Y(I,4) + XZ*(Y(I,5))))
H1 = -R1*C + SIGN*(AW+X1)*S
H2 = R2 + XZ*SBX
Y1 = H1 - H2
X1X2 = XZ
GO TO 19

15 Y1=1000.
19 CONTINUE
C FOR THE RIGHT FIBONACCI POINT, X2
IF(X2.GT.XMAXW)X2=XMAXW
IF(X2.LT.XMINW)X2=XMINW
DO 20 I = 1,NCA
IF (BA(I,2).LE.X2)GO TO 21

20 CONTINUE
21 R1 = R(I,1) + X2*(R(I,2) + X2*(R(I,3) + X2*(R(I,4) + X2*(R(I,5))))
XZ = SIGN*XW - AR + (AW+X2)*C + SIGN*R1*S
IF(XZ.GT.XMAXR) GO TO 25
IF(XZ.LT.XMINR) GO TO 25
DO 22 I = 1,NCB
IF (BB(I,2).LE.XZ) GO TO 23

22 CONTINUE
23 R2 = Y(I,1) + XZ*(Y(I,2) + XZ*(Y(I,3) + XZ*(Y(I,4) + XZ*(Y(I,5))))

```

H1 = -R1*C + SIGN*(AW+X2)*S
H2 = R2 + XZ*SBX
Y2 = H1 - H2
GO TO 29
25 Y2=1000.
29 CCNTINUE
C AT THIS PT WE HAVE X1,X2,Y1,Y2, & X1AX2,X2AX2.
C
C PRINT OUT RESULTS OF IFIB DO LOOP
IF(IP.NE.2) GO TO 501
WRITE (3,500)IFIB,XFIB,XL,X1,Y1,X2,Y2,XR,X1AX2,XZ
500 FORMAT(I3,3F9.4,F13.7,F9.4,F13.7,3F9.4)
501 CONTINUE
C
IF(IFIB.EQ.N) GO TO 9
XFIB = F(N - IFIB)*STEP
9 IF (Y1 - Y2) 1,2,2
C MIN FROM X2 TO THE LEFT
1 XR = X2
X2 = X1
X1 = XR - XFIB
IF(IFIB.EQ.N1) X1 = XL
GO TO 100
C MIN FROM X1 TO THE RIGHT
2 XL = X1
X1 = X2
X2 = XL + XFIB
IF (IFIB.EQ.N1) X2 = XR
100 CONTINUE
C
C STORE CANDIDATE CONTACT POINTS
IF (Y1 - Y2) 3,4,4
C MIN AT PT ON LEFT: AX1MIN=X2, AX2MIN=X1AX2, MIN VAL Y1
3 X1 = X2
X2 = X1AX2
GO TO 5
C MIN AT PT ON RIGHT: AX1MIN=X1, AX2MIN=X2AX2=XZ, MIN VAL Y2
4 X2 = XZ
Y1 = Y2
5 RETURN
END

```



```

SUBROUTINE EQSUB2(NUMBR)
IMPLICIT REAL*8(A-H,C-Z)
COMMON /COMA/ AW,AR,BR,BL,RR(30,5),YR(30,5),RL(30,5),YL(30,5),
1 B1(30,2),B2(30,2),B3(30,2),B4(30,2),S1(5),S2(5),S3(5),S4(5),
1 AXW(244),AX1(244),AX2(244),AX3(244),AX4(244),AR1(244),AR2(244),
1 AR3(244),AR4(244),AR5(244),AM1(244),AM2(244),AM3(244),AW1(244),
1 AY1(244),NC1,NC2,NC3,NC4

```

```

C
C CALCULATE THE CONSTRAINT RELATIONS AT EACH OF THE INCREMENTS OF
C WHEELSET LATERAL
SBR=DSIN(BR)
SBL=DSIN(BL)
AWT2=2.*AW
ART2=2.*AR
DO 100 I=1,NUMBR
C CHOOSE THE CURVE FITS VALID AT THE POINTS
CALL CHOOSE(AX1(I),AX2(I),AX3(I),AX4(I))
C CALCULATE THE ROLLING RADII AND HEIGHT OF THE RAIL AT THE POINTS
CALL RADII(S1,S2,S3,S4,AX1(I),AX2(I),AX3(I),AX4(I),AR1(I),
1 AR2(I),AR3(I),AR4(I))
C CALCULATE WHEELSET ROLL ANGLE
AW1(I)=(AR4(I)-AR2(I)+AX4(I)*SBL -AX2(I)*SBR +AR3(I)
1 -AR1(I))/(AWT2 +AX1(I)+AX3(I))
AK1(I)=DATAN(AW1(I))
AW1(I)=(AR4(I)-AR2(I)+AX4(I)*SBL -AX2(I)*SBR +(AR3(I)-
1 AR1(I))*DCOS(AW1(I)))/((AWT2 +AX1(I)+AX3(I))*DCOS(AW1(I)))
AW1(I)=DATAN(AW1(I))
C CALCULATE RIGHT CONTACT ANGLE
AM1(I)=-(S1(2)+2.*S1(3)*AX1(I)+3.*S1(4)*AX1(I)**2+4.*S1(5)*
1 AX1(I)**3)
AM1(I)=DATAN(AM1(I))
C CALCULATE LEFT CONTACT ANGLE
AM2(I)=-(S3(2)+2.*S3(3)*AX3(I)+3.*S3(4)*AX3(I)**2+4.*S3(5)*
1 AX3(I)**3)
AM2(I)=DATAN(AM2(I))
C CALCULATE NORMALIZED DIFFERENCE IN CONTACT ANGLES
AM3(I)=(AM2(I)-AM1(I))/2.
C CALCULATE NORMALIZED DIFFERENCE IN ROLLING RADII
AR5(I)=(AR3(I)-AR1(I))/ART2
C CALCULATE VERTICAL DISPLACEMENT OF WHEELSET
AY1(I)=(AR4(I)+AR2(I)+AX4(I)*SBL +AX2(I)*SBR +(AR3(I)
1 +AR1(I))*DCOS(AW1(I)))/2.
100 CONTINUE
C NORMALIZE VERTICAL DISPLACEMENT TO ZERO AT XW=0
N=NUMBR/2
Y=AY1(N)
DO 110 I=1,NUMBR
AY1(I)=AY1(I)-Y
110 CONTINUE
RETURN
END

```

```

SUBROUTINE PLOT2(NUMBR,ICTR,ICTL)
  IMPLICIT REAL*8(A-H,O-Z)
  REAL SAXW(244),SAM1(244),SAM2(244),SAM3(244),SAR1(244),
  CSAR3(244),SAR5(244),SAW1(244),SAX1(244),SAX2(244),SAX3(244),
  CSAX4(244)
  COMMON /CUMA/ AW,AR,BR,BL,RR(30,5),YR(30,5),RL(30,5),YL(30,5),
  1 B1(30,2),B2(30,2),B3(30,2),B4(30,2),S1(5),S2(5),S3(5),S4(5),
  1 AXW(244),AX1(244),AX2(244),AX3(244),AX4(244),AR1(244),AR2(244),
  1 AR3(244),AR4(244),AR5(244),AM1(244),AM2(244),AM3(244),AW1(244),
  1 AY1(244),NC1,NC2,NC3,NC4
C
C   COMMON /CUMC/ IWHLR(13),IWHLL(13),IRAILR(13),IRAILL(13)
C
C   DIMENSION ICTR(13),ICTL(13)
C
C   COMPUTE SCALING FACTORS
  AN=NUMBR
  XW=-AN*.005 +.01
  NI=-XW/.01+1.
  N1=NUMBR+1
  N2=NUMBR+2
  NI1=NI+1
  NI2=NI+2
  AXW(N1)=-1.2
  AXW(N2)=.3
  AR1(N1)=DBLE((AINT(SNGL((AR1(NUMBR/2)-.9)*10.)))/10.)
  AR1(N2)=.4
  AR3(N1)=AR1(N1)
  AR3(N2)=AR1(N2)
  AR5(N1)=-.05
  AR5(N2)=.01
C
  AW1(N1)=-.025
  AW1(N2)=.005
C
  AM1(N1)=-.2
  AM1(N2)=.2
  AM2(N1)=AM1(N1)
  AM2(N2)=AM1(N2)
  AM3(N1)=-1.
  AM3(N2)=.2
C
C   ** CHANGE DOUBLE PRECISION ARRAYS TO SINGLE PRECISION FOR PLOTTING
  DO 50 I=1,244
    SAXW(I)=SNGL(AXW(I))
    SAM1(I)=SNGL(SAM1(I))
    SAM2(I)=SNGL(SAM2(I))
    SAM3(I)=SNGL(SAM3(I))
    SAR1(I)=SNGL(SAR1(I))
    SAR3(I)=SNGL(SAR3(I))
    SAR5(I)=SNGL(SAR5(I))
    SAW1(I)=SNGL(SAW1(I))
  50 CONTINUE
C   PLCT DIFF IN CONTACT ANGLES
  CALL PLOT(.5,.5,-3)
  CALL SYMBOL(.5,10.2,.21,'ONE HALF CONTACT ANGLE DIFFERENCE',0.,33)
  CALL GRID(0.,0.,.5,.5,16,20)
  CALL AXIS(0.,0.,21,HWHEELSET LATERAL (IN),-21,8.,0.,AXW(N1),
  1 AXW(N2))
  CALL LINE(SAXW,SAM3,NUMBR,1,+1,5)
  CALL AXIS(4.,0.,.46F1/2 DIFF. IN CONTACT ANGLES W.R.T. AXLE, LT-RT
  1,46,9.9,90.,AM3(N1),AM3(N2))
C   PLCT DIFF IN ROLLING RADII
  CALL PLOT(0.,11.5,-3)
  CALL SYMBOL(.3,10.2,.21,'NORMALIZED ROLLING RADII DIFFERENCE',0.,
  1 35)
  CALL GRID(0.,0.,.5,.5,16,20)
  CALL AXIS(0.,0.,21,HWHEELSET LATERAL (IN),-21,8.,0.,AXW(N1),
  1 AXW(N2))
  CALL LINE(SAXW,SAR5,NUMBR,1,+1,5)

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CALL AXIS(4.0,0.,.35SHDIFF. IN ROLLING RADIUS/RAIL GAGE, LF-RT,
1 39.9,9.9,90.,AR5(N1),AR5(N2))
C
C PLCT ROLLING RADII
CALL PLOT(9.,0.,-3)
CALL SYMBOL(2.6,10.2,.21,'ROLLING RADII',0.,13)
CALL GRID(0.,0.,.5,.5,16,20)
CALL AXIS(0.,0.,.21HWHEELSET LATERAL (IN),-21,8.,0.,AXW(N1),
1 AXW(N2))
CALL AXIS(4.0,0.,.35HROLLING RADIUS, +=RIGHT, *=LEFT, IN.,35,9.9,
1 90.,AR1(N1),AR1(N2))
CALL LINE(SAXW,SAR1,NUMBR,1,+1,3)
CALL LINE(SAXW,SAR3,NUMBR,1,+1,11)
C
C PLCT CONTACT ANGLES
CALL PLOT(0.,-11.5,-3)
CALL SYMBOL(2.5,10.2,.21,'CONTACT ANGLES',0.,14)
CALL GRID(0.,0.,.5,.5,16,20)
CALL AXIS(0.,0.,.21HWHEELSET LATERAL (IN),-21,8.,0.,AXW(N1),
1 AXW(N2))
CALL AXIS(4.0,0.,.37CONTACT ANGLE W.R.T. AXLE, +=RT, *=LT,37,
1 9.9,90.,AM1(N1),AM1(N2))
CALL LINE(SAXW,SAM1,NUMBR,1,+1,3)
CALL LINE(SAXW,SAM2,NUMBR,1,+1,11)
C
C PLCT WHEELSET ROLL ANGLES
CALL PLOT(9.,0.,-3)
CALL SYMBOL(2.6,10.2,.21,'WHEELSET ROLL',0.,13)
CALL GRID(0.,0.,.5,.5,16,20)
CALL AXIS(0.,0.,.21HWHEELSET LATERAL (IN),-21,8.,0.,AXW(N1),
1 AXW(N2))
CALL AXIS(4.0,0.,.13HWHEELSET ROLL,13,9.9,90.,AW1(N1),AW1(N2))
CALL LINE(SAXW,SAW1,NUMBR,1,+1,5)
C
C TITLES
CALL SYMBOL(1.5,21.,.21,'RIGHT SIDE',0.,10)
CALL SYMBOL(1.0,20.,.21,IWHLR,0.,52)
CALL SYMBOL(1.0,19.5,.21,IRAILR,0.,52)
CALL SYMBOL(1.0,19.,.21,ICTR,0.,52)
CALL SYMBOL(1.5,18.0,.21,'LEFT SIDE',0.,9)
CALL SYMBOL(1.0,17.0,.21,IWFL,0.,52)
CALL SYMBOL(1.0,16.5,.21,IRAILL,0.,52)
CALL SYMBOL(1.0,16.0,.21,ICTL,0.,52)
C
C SCALING FACTORS
AX1(N1)=0.
AX1(N2)=1.
AX2(N1)=0.
AX2(N2)=1.
AX3(N1)=0.
AX3(N2)=1.
AX4(N1)=0.
AX4(N2)=1.
C ** CHANGE DOUBLE PRECISION VALUES TO SINGLE PRECISION FOR PLOTTING
DC 60 I=1,244
SAX1(I)=SNGL(AX1(I))
SAX2(I)=SNGL(AX2(I))
SAX3(I)=SNGL(AX3(I))
SAX4(I)=SNGL(AX4(I))
60
C PLCT RIGHT WHEEL CONTACT PTS
CALL PLOT(20.5,13.25,-3)
CALL AXIS(0.,0.,.21HWHEELSET LATERAL (IN),21,7.9,90.,-1.2,-3)
CALL SYMBOL(-2.5,8.2,.21,'WHEEL CONTACT POSITION',0.,22)
CALL GRID(-2.5,0.,.5,.5,10,16)
CALL LINE(SAX1,SAXW,NUMBR,1,+1,5)
C PLOT RIGHT RAIL CONTACT PTS
CALL PLOT(15.5,0.,-3)
CALL AXIS(0.,0.,.21HWHEELSET LATERAL (IN),21,7.9,90.,-1.2,-3)
CALL SYMBOL(-2.0,8.2,.21,'RAIL CONTACT POSITION',0.,21)
CALL GRID(-2.,0.,.5,.5,8,16)

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```
CALL LINE(SAX2,SAXW,NUMBR,1,+1,5)
C PLCT LEFT RAIL CONTACT PTS
CALL PLOT(0.,-13.25,-3)
CALL AXIS(0.,0.,21,HWHEELSET LATERAL (IN),21,7.9,9),-1.2,-3)
CALL SYMBOL(-2.0,8.2,.21,'RAIL CONTACT POSITION',0.,21)
CALL GRID(-2.,0.,.5,.5,8,16)
CALL LINE(SAX4,SAXW,NUMBR,1,1,5)
C PLOT LEFT WHEEL CONTACT PTS
CALL PLOT (-5.5,0.,-3)
CALL AXIS(0.,0.,21,HWHEELSET LATERAL (IN),21,7.9,90),-1.2,-3)
CALL SYMBOL(-2.5,8.2,.21,'WHEEL CONTACT POSITION',0.,22)
CALL GRID(-2.5,0.,.5,.5,10,16)
CALL LINE(SAX3,SAXW,NUMBR,1,1,5)
RETURN
END
```

C CUBIC SPLINE FITTING ROUTINE

C PURPOSE:

C SOLVE BASIC SIMULTANEOUS SET OF N SPLINE LINEAR EQUATIONS
 C FOR SECOND DERIVATIVES S(I) AT SPLINE JOINTS. RESULTS STORED IN
 C VECTOR C. ROUTINE CAN ACCOMMODATE UP TO N=200 SPLINE JOINTS.

C VARIABLES:

C N = NUMBER OF SPLINE JOINTS (INPUT)
 C X = N X 1 VECTOR OF ABSCISSA JOINT COORDINATES (INPUT)
 C Y = N X 1 VECTOR OF ORDINATE JOINT COORDINATES (INPUT)
 C C = N X 1 VECTOR OF S(I) 2ND DERIV SCALN (OUTPUT)
 C IPRINT = PRINT FLAG, 0=NO PRINT, 1=PRINT (INPUT)
 C H(I) = X(I+1) - X(I) = DIST BETWEEN ADJACENT JOINTS

C TRIDIAGONAL SYSTEM:

C SYSTEM IS TRIDIAGONAL ALLOWING QUICK SOLUTION OF A LARGE NUMBER
 C OF EQUATIONS.
 C B(I) = ELEMENTS BELOW DIAGONAL
 C D(I) = ELEMENTS ON DIAGONAL
 C A(I) = ELEMENTS ABOVE DIAGONAL
 C C(I) = CONSTANT RIGHT HAND SIDE ELEMENTS
 C THE N SIMULTANEOUS EQNS IN 2ND DERIVATIVES S(I) HAVE BEEN REDUCED
 C TO (N-2) EQNS TO TAKE ADVANTAGE OF THE RAPID SOLN OF A TRIDIAGONAL
 C SYSTEM. THE 1ST EQN HAS BEEN INCORPORATED IN THE 2ND EQN,
 C AND THE NTH IN THE (N-1)ST EQN.

C THE END CONDITIONS:

C THE END CONDITIONS FOR SPLINE FITTING MUST BE CHOSEN.
 C THE VALUES OF THE 2ND DERIVATIVES AT END
 C JOINTS X(1) AND X(N) ARE ESTIMATED AS A LINEAR EXTRAPLOATION
 C OF THE 2ND DERIVATIVES AT THE TWO ADJACENT JOINTS, RESPECTIVELY

C THIS SUBROUTINE CAN BE CHANGED TO ACCOMMODATE OTHER END CONDITIONS
 C BY REPLACING THE CODING LOCATED BETWEEN THE LINES OF ASTERISKS.

C SUBROUTINE SPLINE(N,X,Y,C,IPRINT)
 C IMPLICIT REAL*8(A-H,O-Z)
 C DIMENSION X(1),Y(1),C(1),B(201),D(201),A(201),H(201)
 C N1=N-1
 C N2=N-2
 C H(1)=X(2)-X(1)
 C H(2)=X(3)-X(2)
 C H(N1)=X(N)-X(N1)

C THE MODIFIED SECOND SYSTEM EQN (I=2)

C P(2)=0.
 C *****
 C D(2)=(2.+H(1)/H(2))*H(1)+H(2)
 C A(2)=H(2)-H(1)*H(1)/H(2)
 C *****
 C C(2)=6.*((Y(3)-Y(2))/H(2)-(Y(2)-Y(1))/H(1))

C THE NEXT (N-4) SYS EQNS (I=3,4,...,N-2)

C DO 10 I=3,N2
 C H(I)=X(I+1)-X(I)
 C B(I)=H(I-1)
 C D(I)=2.*H(I-1)+H(I)
 C A(I)=H(I)
 C C(I)=6.*((Y(I+1)-Y(I))/H(I)-(Y(I)-Y(I-1))/H(I-1))

10

C THE MODIFIED NEXT TO LAST SYS EQN (I=N-1)

C A(N1)=0.
 C *****
 C B(N1)=H(N2)-H(N1)*H(N1)/H(N2)
 C D(N1)=(2.+H(N1)/H(N2))*H(N1)+H(N2)
 C *****
 C C(N1)=6.*((Y(N)-Y(N1))/H(N1)-(Y(N1)-Y(N2))/H(N2))

C

C PRINT RESULTS

C IF(IPRINT.EQ.0) GO TO 15
 C WRITE(3,100)
 C 100 FORMAT ('0')

```

WRITE(3,200) (1,B(I),D(I),A(I),C(I),H(I),I=2,N1)
200  FORMAT(15,5F14.6)
C
C  SOLVE TRIDIAGONAL SYSTEM BY ELIMINATION.
C  STORAGE IS MINIMIZED BY COMPRESSING COEFS INTO 4 VECTORS.
C  N-2 EQNS IN N-2 UNKNOWN'S
C
C  COMPUTE NEW MATRIX.  VALS OF VAR WILL BE STORED IN C ARRAY.
15  DC 20 I=3,N1
    R=B(I)/D(I-1)
    D(I)=D(I)-R*A(I-1)
20  C(I)=C(I)-R*C(I-1)
C  BACK SUBSTITUTION.
    C(N1)=C(N1)/D(N1)
    DC 30 I=2,N2
    J=N1-I+1
30  C(J)=(C(J)-A(J)*C(J+1))/D(J)
C
C  CALCULATE THE SOLUTION VALUES FOR I=1 AND I=N
C *****
C(1)=(H(1)+H(2))*C(2)-C(3)*H(1))/H(2)
C(N)=(H(N2)+H(N1))*C(N1)-C(N2)*H(N1))/H(N2)
C *****
C
C  PRINT RESULTS
    IF(IPRINT.EQ.0) GO TO 40
    WRITE(3,100)
    WRITE(3,300) (1,C(I),I=1,N)
300  FORMAT(15,F14.6)
C
40  RETURN
    END

```

```

C CUBIC SPLINE INTERPOLATION ROUTINE
C C
C C PURPOSE:
C C INTERPOLATE TO FIND Y ORDNATE VALUE BETWEEN JOINTS
C C AND FIND VALUES OF 1ST DERIV, 2ND DERIV, RADIUS OF
C C CURVATURE, AND CURVATURE AT THIS Y VALUE.
C C THIS ROUTINE IS USED IN CONJUNCTION WITH THE SPLINE
C C ROUTINE WHICH FINDS THE VALUES OF 2ND DERIV S(I) AT JOINTS.
C C
C C VARIABLES:
C C N = NUMBER OF JOINTS
C C X = INPUT VECTOR OF JOINT COORDINATES - ABSCISSAS
C C Y = INPUT VECTOR OF JOINT COORDINATES - ORDINATES
C C S = INPUT VECTOR OF 2ND DERIVATIVES AT JOINTS
C C XP = INPUT X VALUE
C C YP = OUTPUT Y VALUE
C C D1 = OUTPUT 1ST DERIVATIVE
C C D2 = OUTPUT 2ND DERIVATIVE
C C RC = OUTPUT RADIUS OF CURVATURE
C C CV = OUTPUT CURVATURE = 1./RC
C C IER = ERROR FLAG, 0=NO ERROR, 1=X VALUE INPUT ERROR
C C
C C SUBROUTINE SPI(N,X,Y,S,XP,YP,D1,D2,RC,CV,IER)
C C IMPLICIT REAL*8(A-H,O-Z)
C C DIMENSION X(1),Y(1),S(1)
C C ENTRY SPIC(N,X,Y,S,XP,CV)
C C
C C CHECK FOR X INPUT ERROR.
C IER=0
C IF(XP.GE.X(1).AND.XP.LE.X(N)) GO TO 10
C IF(IER.EQ.1) GO TO 5
C IER=1
C XPI=C.000001
C IF(XP.GT.0.0) XPI=-0.000001
C XP=XP+XPI
C GO TO 1
C 5 WRITE(3,100) XP
C 100 FORMAT(' THE INPUT X VALUE X =',F12.6,
C 1 ' IS OUTSIDE JOINT RANGE *****')
C RETURN
C C
C C LOCATE WHICH INTERVAL XP IS IN.
C 10 DO 20 L=2,N
C IF(X(L).GE.XP) GO TO 30
C 20 CONTINUE
C 30 I=L-1
C C
C C CALCULATE CUBIC COEFFICIENTS ON ITH INTERVAL
C H=X(L)-X(I)
C AP=(S(L)-S(I))/(6.*H)
C BP=S(I)/2.
C CP=(Y(L)-Y(I))/H-(S(L)+2.*S(I))*H/6.
C XD=XP-X(I)
C C
C C CALC YP VALUE, DERIVATIVES, AND RAD OF CURV FOR THIS XP.
C YP=AP*XD**3+BP*XD*XD+CP*XD+Y(I)
C D1=3.*AP*XD*XD+2.*BP*XD+CP
C D2=6.*AP*XD+2.*BP
C RC=((1.+D1*D1)**1.5)/D2
C C NEGATE THE CURVATURE FOR WRAIL PROFILES
C CV=-1./RC
C RETURN
C END

```

```

SUBROUTINE DCRFCN(N,AXW,AR5,AM3,AW1,AR)
  IMPLICIT REAL*8(A-F,C-Z)
  DIMENSION AXW(1),AR5(1),AM3(1),AW1(1)
C LINEARIZATION USING DESCRIBING FUNCTIONS WITH A SINUSIODAL INPUT
C AMP=AMP OF MOTION=A
C ALAM=SLOPE OF (RL-RR)/2AR=AN2
C DELM=SLOPE OF (ML-MR)/2=AN1
C WSRL=SLOPE OF WHEELSET ROLL ANGLE DATA =AN3
  PRINT 10
  10 FORMAT(///2X,'LINEARIZATION USING DESCRIBING FCNS'/3X,'AMP',
    1 5X,'ALAM',5X,'DELM',5X,'WSRL'/)
C COMPUTE POINT IN ARRAYS CORRESPONDING TO START OF XW GT 0
  N2=N/2+2
C COMPUTE FOR EACH AMPLITUDE
  DO 100 IJK=1,30
    AI=IJK
    A=.05*AI
C CHECK LIMIT OF ARRAY
    IF(A.GT.AXW(N)+.002) GO TO 200
C DEFINE OR INITIALIZE PARAMETERS
    AK=4./(3.14159*A**2.)
    AN1=0
    AN2=0
    AN3=0
C USE TRAPAZOIDAL RULE TO NUMERICALLY INTEGRATE EQUATIONS
  DO 40 I=N2,402
    I1=I-1
C *****
C ** RCUND-UP ROUTINE FOR ARCSIN ARGUMENT GREATER THAN ONE
    TEST1=AXW(I)/A
    TEST2=AXW(I1)/A
    IF(ABS(TEST1).GT.1.000001.AND.ABS(TEST2).GT.1.000001)GOTO 1
  1    TEST1=1.00000000000000000000+00
  2    IF(ABS(TEST2).GT.1.000001.AND.ABS(TEST2).LT.1.000001)GOTO 3
    GOTO 4
  3    TEST2=1.00000000000000000000+00
  4    CONTINUE
C ** IF ARGUMENT OF ARSIN IS GREATER THEN 1.00001
C ** THE PROGRAM WILL TERMINATE ABNCRMALLY
C ** END OF ARGUMENT PROTECTION ROUTINE
C *****
    S1=DARSIN(TEST1)-DARSIN(TEST2)
    AN1=AN1+(AM3(I1)*AXW(I1)+AM3(I)*AXW(I))*S1/2.
    AN2=AN2+(AR5(I1)*AXW(I1)+AR5(I)*AXW(I))*S1/2.
    AN3=AN3+(AW1(I1)*AXW(I1)+AW1(I)*AXW(I))*S1/2.
C CHECK TO SEE IF AMPLITUDE REACHED
    IF((AXW(I)-A).GE.-.002) GO TO 50
  40 CONTINUE
C COMBINE TERMS AND NORMALIZE
  50 AN1=AN1*AK*AR
    AN2=AN2*AK*AR
    AN3=AN3*AK*AR
C OUTPUT
  PRINT 60,AXW(I),AN2,AN1,AN3
  60 FORMAT(  F7.3,3(  F9.4))
  100 CONTINUE
  200 CONTINUE
  RETURN
  END

```


LISTING OF INPUT CARDS - SYMMETRIC PROBLEM

.01
 001001
 001000
 000
 101005
 53.0 56.5 .025 .025
 NEW AAR WHEEL DATA 026
 3.0525
 0072
 1 1

0.2849992E+01	-0.1517651E+02	0.2563899E+01	-0.1605087E+02
0.2482374E+01	-0.1637062E+02	0.2379514E+01	-0.1638278E+02
0.2298308E+01	-0.1638788E+02	0.2210096E+01	-0.1639655E+02
0.2121566E+01	-0.1640149E+02	0.2004057E+01	-0.1641267E+02
0.1900559E+01	-0.1642101E+02	0.1819672E+01	-0.1642586E+02
0.1724455E+01	-0.1642905E+02	0.1621276E+01	-0.1642966E+02
0.1518735E+01	-0.1643260E+02	0.1423199E+01	-0.1643344E+02
0.1334988E+01	-0.1643835E+02	0.1224484E+01	-0.1644630E+02
0.1106657E+01	-0.1645422E+02	0.1003796E+01	-0.1645920E+02
0.9082613E+00	-0.1646436E+02	0.8050820E+00	-0.1646925E+02
0.6802480E+00	-0.1647444E+02	0.5627390E+00	-0.1647919E+02
0.4522360E+00	-0.1648421E+02	0.3493760E+00	-0.1649142E+02
0.2388720E+00	-0.1649567E+02	0.1286880E+00	-0.1650182E+02
0.2582800E-01	-0.1650694E+02	-0.7735097E-01	-0.1651505E+02
-0.1732060E+00	-0.1652180E+02	-0.2980390E+00	-0.1652998E+02
-0.4085430E+00	-0.1653506E+02	-0.5040790E+00	-0.1654015E+02
-0.5996140E+00	-0.1654073E+02	-0.7094800E+00	-0.1654124E+02
-0.7976910E+00	-0.1654204E+02	-0.8859030E+00	-0.1655125E+02
-0.9601030E+00	-0.1655791E+02	-0.1062963E+01	-0.1657082E+02
-0.1136845E+01	-0.1658423E+02	-0.1204040E+01	-0.1660268E+02
-0.1270916E+01	-0.1662659E+02	-0.1338110E+01	-0.1665831E+02
-0.1391294E+01	-0.1668880E+02	-0.1459127E+01	-0.1674220E+02
-0.1512948E+01	-0.1679153E+02	-0.1536196E+01	-0.1681941E+02
-0.1567407E+01	-0.1686533E+02	-0.1599255E+01	-0.1691809E+02
-0.1623141E+01	-0.1696332E+02	-0.1647346E+01	-0.1700359E+02
-0.1686200E+01	-0.1707988E+02	-0.1703718E+01	-0.1711224E+02
-0.1735567E+01	-0.1718874E+02	-0.1760090E+01	-0.1723038E+02
-0.1790982E+01	-0.1728351E+02	-0.1822830E+01	-0.1732303E+02
-0.1868690E+01	-0.1737601E+02	-0.1914549E+01	-0.1741570E+02
-0.1960089E+01	-0.1745094E+02	-0.2012954E+01	-0.1748557E+02
-0.2073144E+01	-0.1752026E+02	-0.2125690E+01	-0.1754588E+02
-0.2177917E+01	-0.1756200E+02	-0.2244155E+01	-0.1757417E+02
-0.2325361E+01	-0.1757899E+02	-0.2398605E+01	-0.1758299E+02
-0.2464843E+01	-0.1757506E+02	-0.2529806E+01	-0.1755930E+02
-0.2609099E+01	-0.1752475E+02	-0.2688073E+01	-0.1747803E+02
-0.2758766E+01	-0.1742532E+02	-0.2829459E+01	-0.1735641E+02

NEW RAIL DATA 025

1.5
072
0 0

0.14329410	01	0.61061130	01
0.14291980	01	0.61597160	01
0.14256830	01	0.62024020	01
0.14221670	01	0.62558520	01
0.14188780	01	0.62999160	01
0.14115450	01	0.64079960	01
0.14084830	01	0.64595930	01
0.14052700	01	0.65026490	01
0.13848190	01	0.66204050	01
0.13772590	01	0.66489650	01
0.13565820	01	0.67263300	01
0.13270590	01	0.67767390	01
0.12887660	01	0.68278590	01
0.12460500	01	0.68722490	01
0.12031830	01	0.69068200	01
0.11558180	01	0.69354830	01
0.11040300	01	0.69586720	01
0.10392000	01	0.69851670	01
0.97879400	00	0.70091350	01
0.93127700	00	0.70256050	01
0.88361000	00	0.70380430	01
0.83594200	00	0.70459280	01
0.78385200	00	0.70525030	01
0.71872000	00	0.70597570	01
0.65366300	00	0.70663340	01
0.59295400	00	0.70750920	01
0.53644100	00	0.70799950	01
0.44957300	00	0.70834930	01
0.38436600	00	0.70858620	01
0.31915800	00	0.70883990	01
0.24967900	00	0.70912570	01
0.19316600	00	0.70935360	01
0.14534700	00	0.70957540	01
0.93256980-01		0.70967250	01
0.38668000-01		0.70966410	01
-0.37310000-01		0.70929160	01
-0.98246010-01		0.70913560	01
-0.15910600	00	0.70909650	01
-0.21561900	00	0.70933440	01
-0.27640400	00	0.70930600	01
-0.34176300	00	0.70901480	01
-0.38096300	00	0.70872740	01
-0.47667600	00	0.70784160	01
-0.51602750	00	0.70773310	01
-0.57248510	00	0.70720110	01
-0.62478230	00	0.70704020	01
-0.68571830	00	0.70615160	01
-0.72941680	00	0.70554230	01
-0.78608120	00	0.70413460	01
-0.82985530	00	0.70346050	01

-0.89948560	00	0.70233440	01
-0.94745560	00	0.70174310	01
-0.99107850	00	0.70067760	01
-0.10479700	01	0.69881620	01
-0.11092840	01	0.69678310	01
-0.11660240	01	0.69449910	01
-0.12143720	01	0.69243820	01
-0.12582220	01	0.68990890	01
-0.12978000	01	0.68719200	01
-0.13331820	01	0.68444620	01
-0.13728350	01	0.68047690	01
-0.14040220	01	0.67669180	01
-0.14308610	01	0.67112460	01
-0.14403870	01	0.66880750	01
-0.14586070	01	0.66212080	01
-0.14681330	01	0.65845440	01
-0.14775830	01	0.65141430	01
-0.14785660	01	0.65070630	01
-0.14835940	01	0.64519760	01
-0.14929690	01	0.63853160	01
-0.14937250	01	0.63817730	01
-0.15031750	01	0.63237230	01

RAIL CANT FOR RIGHT RAIL .025

RAIL CANT FOR LEFT RAIL .025

RAIL GAUGE 56.5 (IN)

WHEEL GAUGE 53.0 (IN)

PRINTER OUTPUT - SYMMETRIC PROBLEM

THE ASYMMETRIC RAIL/RAIL CONTACT CHARACTERIZATION PROGRAM

RUN OPTIONS SELECTED

XWINC= 0.0100

ISYM= 1 IPUNCH= 1

IPLT= 1 I CURV= 0

IFLANG = 0

NUMB=101 INC= 5

WHEEL GAUGE (IN), RAIL GAUGE (IN), RIGHT RAIL CANT (RAD), LEFT RAIL CANT (RAD)

53.0000 56.5000 0.02500 0.02500

RIGHT WHEEL PROFILE INPUT DATA *****

NEW RAIL WHEEL DATA 026

3.06250

72

1	0.28499920+01	0.15176510+02
2	0.25638990+01	0.16050870+02
3	0.24823740+01	0.16370620+02
4	0.23795140+01	0.16382780+02
5	0.22983080+01	0.16387880+02
6	0.22100960+01	0.16396550+02
7	0.21215660+01	0.16401490+02
8	0.20040570+01	0.16412670+02
9	0.19005590+01	0.16421010+02
10	0.18196720+01	0.16425860+02
11	0.17244550+01	0.16429050+02
12	0.16212760+01	0.16429660+02
13	0.15187350+01	0.16432600+02
14	0.14231990+01	0.16433440+02
15	0.13349880+01	0.16438350+02
16	0.12244840+01	0.16446300+02
17	0.11066570+01	0.16454220+02
18	0.10037960+01	0.16459200+02
19	0.90826130+00	0.16464360+02
20	0.80508200+00	0.16469250+02
21	0.68024800+00	0.16474440+02
22	0.56273900+00	0.16479190+02
23	0.45223600+00	0.16484210+02
24	0.34937600+00	0.16489140+02
25	0.25887200+00	0.16496670+02
26	0.12868800+00	0.16501820+02
27	0.25028000-01	0.16506540+02
28	-0.77350970-01	0.16515050+02
29	-0.17320600+00	0.16521800+02
30	-0.29839900+00	0.16529980+02
31	-0.40854300+00	0.16535060+02
32	-0.50479900+00	0.16540150+02
33	-0.59961400+00	0.16540730+02
34	-0.70948300+00	0.16541240+02
35	-0.79769100+00	0.16542040+02
36	-0.88599300+00	0.16551250+02
37	-0.96010300+00	0.16557510+02
38	-0.10629630+01	0.16570820+02
39	-0.11368450+01	0.16584230+02
40	-0.12040400+01	0.16602680+02
41	-0.12709160+01	0.16626590+02
42	-0.13381100+01	0.16658310+02
43	-0.13912940+01	0.16688800+02
44	-0.14591270+01	0.16742200+02
45	-0.15129480+01	0.16791530+02
46	-0.15361960+01	0.16819410+02
47	-0.15674770+01	0.16865330+02
48	-0.15992550+01	0.16918090+02
49	-0.16231410+01	0.16963320+02
50	-0.16473460+01	0.17003590+02
51	-0.16802000+01	0.17075880+02
52	-0.17037180+01	0.17112240+02
53	-0.17355670+01	0.17186740+02
54	-0.17609900+01	0.17230380+02
55	-0.17909820+01	0.17283510+02
56	-0.18228300+01	0.17323030+02
57	-0.18686900+01	0.17376010+02
58	-0.19145400+01	0.17415700+02
59	-0.19600890+01	0.17450940+02
60	-0.20129540+01	0.17485570+02
61	-0.20731440+01	0.17520260+02
62	-0.21256900+01	0.17545880+02
63	-0.21779170+01	0.17562000+02
64	-0.22441550+01	0.17574170+02
65	-0.23253610+01	0.17578990+02
66	-0.23986050+01	0.17582590+02
67	-0.24648430+01	0.17575060+02
68	-0.25298060+01	0.17559300+02
69	-0.26090990+01	0.17524750+02
70	-0.26880730+01	0.17478030+02
71	-0.27587660+01	0.17425320+02
72	-0.28294590+01	0.17356410+02

***** RESULTS *****

RIGHT SIDE

WHEEL/RAIL CONTACT CHARACTERIZATION

NEW AAR WHEEL DATA 026
WHEEL GAGE=53.4001
1/2" DIST BETWEEN TAPE LINES=29.563

CURVE FITS 5 PIS/CURVE FIT ZONE

1	0.4430	104	-1	71.943	1ST	0.444	2AD	0.121	3RD	0.128	4TH	FROM	20	0.000	T0	2.819
2	0.1552	378	0	157.744	CD+CI	0.171	88	0.273	115	0.497	100	FROM	21	0.897	T0	1.819
3	0.1570	80	-1	24.214	TD+OI	0.177	89	0.144	88	0.001	0	FROM	22	0.855	T0	1.335
3	0.1570	80	-1	24.214	TD+OI	0.177	89	0.144	88	0.001	0	FROM	23	0.855	T0	1.335
4	0.1530	36	0	3.707	888	0	0	0.339	10	0.002	0	FROM	24	0.838	T0	0.929
5	0.0000	0	0	6.149	790	-1	0	0.173	79	0.001	0	FROM	25	0.835	T0	0.929
5	0.0000	0	0	6.149	790	-1	0	0.173	79	0.001	0	FROM	26	0.835	T0	0.929
6	0.1200	6	0	16.599	860	0	0	0.208	80	0.001	0	FROM	27	0.835	T0	0.929
7	0.1689	30	0	3.839	288	0	0	0.266	81	0.002	0	FROM	28	0.835	T0	0.929
8	0.2853	30	0	3.839	288	0	0	0.266	81	0.002	0	FROM	29	0.835	T0	0.929
10	0.2853	30	0	3.839	288	0	0	0.266	81	0.002	0	FROM	30	0.835	T0	0.929
11	0.5869	4	0	11.894	99	0	0	0.566	81	0.002	0	FROM	31	0.835	T0	0.929
11	0.5869	4	0	11.894	99	0	0	0.566	81	0.002	0	FROM	32	0.835	T0	0.929
12	0.4780	2	-1	12.171	70	0	0	0.497	77	0.001	0	FROM	33	0.835	T0	0.929
13	0.5119	2	0	1.602	55	0	0	0.800	44	0.001	0	FROM	34	0.835	T0	0.929

NEW AAR RAIL DATA 025

RAIL GAGE=56.500
1/2" DIST BETWEEN TAPE LINES=29.563
RAIL CANT=0.025

CURVE FITS 5 PIS/CURVE FIT ZONE

1	0.1332	110	0	3.498	1ST	0.364	2AD	0.173	3RD	0.309	4TH	FROM	20	0.000	T0	1.419
2	0.2337	110	0	3.498	290	0	0	0.273	115	0.497	100	FROM	21	0.897	T0	1.819
3	0.2187	140	0	0.769	790	0	0	0.355	80	0.003	0	FROM	22	0.835	T0	0.929
3	0.2187	140	0	0.769	790	0	0	0.355	80	0.003	0	FROM	23	0.835	T0	0.929
4	0.6109	10	0	2.237	88	0	0	0.519	46	0.001	0	FROM	24	0.835	T0	0.929
5	0.7115	8	0	2.237	88	0	0	0.519	46	0.001	0	FROM	25	0.835	T0	0.929
5	0.7115	8	0	2.237	88	0	0	0.519	46	0.001	0	FROM	26	0.835	T0	0.929
6	0.7094	2	0	2.629	51	0	0	0.473	40	0.001	0	FROM	27	0.835	T0	0.929
7	0.7094	2	0	2.629	51	0	0	0.473	40	0.001	0	FROM	28	0.835	T0	0.929
8	0.6867	4	0	1.039	39	0	0	0.611	31	0.001	0	FROM	29	0.835	T0	0.929
9	0.6867	4	0	1.039	39	0	0	0.611	31	0.001	0	FROM	30	0.835	T0	0.929
10	0.9771	5	0	0.764	41	0	0	0.929	35	0.002	0	FROM	31	0.835	T0	0.929
11	0.9771	5	0	0.764	41	0	0	0.929	35	0.002	0	FROM	32	0.835	T0	0.929
12	0.1532	3	0	4.981	88	0	0	0.228	53	0.001	0	FROM	33	0.835	T0	0.929
13	0.1874	10	0	1.881	190	0	0	0.465	41	0.001	0	FROM	34	0.835	T0	0.929

***** DATA POINTS *****

CONTACT POINTS, GEOMETRIC CONSTRAINTS, AND PROFILE CURVATURES AS A FUNCTION OF WHEELSET LATERAL DISPLACEMENT

XW = WHEELSET LATERAL, POSITIVE TO THE LEFT (IN)
X1 = CONTACT LOCATION ON RIGHT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
X2 = CONTACT LOCATION ON RIGHT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
X3 = CONTACT LOCATION ON LEFT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
X4 = CONTACT LOCATION ON LEFT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
RR = ROLLING RADIUS, RIGHT WHEEL (IN)
YR = RAIL HEAD PROFILE HEIGHT, RIGHT RAIL (IN)
YL = ROLLING RADIUS, LEFT WHEEL (IN)
YR = RAIL HEAD PROFILE HEIGHT, LEFT RAIL (IN)
MR = CONTACT ANGLE W-R-T. AXLE, RIGHT WHEEL (RAD)
ML = CONTACT ANGLE W-R-T. AXLE, LEFT WHEEL (RAD)
RR CRV = PRINCIPAL ROLLING CURVATURE OF RIGHT WHEEL PROFILE (1/IN)
RL CRV = PRINCIPAL ROLLING CURVATURE OF LEFT WHEEL PROFILE (1/IN)

Table with 14 columns: XW (IN), X1 (IN), X2 (IN), X3 (IN), X4 (IN), RR (IN), YR (IN), YL (IN), YL (IN), MR (RAD), ML (RAD), RR CRV (1/IN), RL CRV (1/IN). Rows represent data points for various wheelset lateral positions from -1.000 to -0.040.

PROFILE PRINCIPAL TRANSVERSE CURVATURES (1/IN)

XWR= LOCATION ON RIGHT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
 XRR= LOCATION ON RIGHT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 XWL= LOCATION ON LEFT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
 XRL= LOCATION ON LEFT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 CWR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CWL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)

XWR (IN)	CWR (1/IN)	XRR (IN)	CYR (1/IN)	XWL (IN)	CWL (1/IN)	XRL (IN)	CYL (1/IN)
-2.39861	1.086594	-1.43086	1.229009	-2.39861	1.086594	-1.43086	1.229009
-2.35000	1.239624	-1.40000	1.648176	-2.35000	1.239624	-1.40000	1.648176
-2.30000	1.381223	-1.35000	2.351565	-2.30000	1.381223	-1.35000	2.351565
-2.25000	1.495469	-1.30000	2.587111	-2.25000	1.495469	-1.30000	2.587111
-2.20000	1.570747	-1.25000	1.853100	-2.20000	1.570747	-1.25000	1.853100
-2.15000	1.597979	-1.20000	C.831286	-2.15000	1.597979	-1.20000	C.831286
-2.10000	1.573413	-1.15000	C.881850	-2.10000	1.573413	-1.15000	C.881850
-2.05000	1.500123	-1.10000	C.929957	-2.05000	1.500123	-1.10000	C.929957
-2.00000	1.387651	-1.05000	C.974213	-2.00000	1.387651	-1.05000	C.974213
-1.95000	1.249490	-1.00000	1.013174	-1.95000	1.249490	-1.00000	1.013174
-1.90000	1.299115	-0.95000	C.833619	-1.90000	1.299115	-0.95000	C.833619
-1.85000	1.526603	-0.90000	C.566033	-1.85000	1.526603	-0.90000	C.566033
-1.80000	1.358862	-0.85000	C.322516	-1.80000	1.358862	-0.85000	C.322516
-1.75000	0.868422	-0.80000	C.058143	-1.75000	0.868422	-0.80000	C.058143
-1.70000	0.212215	-0.75000	C.011668	-1.70000	0.212215	-0.75000	C.011668
-1.65000	-0.217905	-0.70000	C.650544	-1.65000	-0.217905	-0.70000	C.650544
-1.60000	-0.880738	-0.65000	C.089676	-1.60000	-0.880738	-0.65000	C.089676
-1.55000	-1.243132	-0.60000	C.128926	-1.55000	-1.243132	-0.60000	C.128926
-1.50000	-1.639226	-0.55000	C.168350	-1.50000	-1.639226	-0.55000	C.168350
-1.45000	-1.970916	-0.50000	C.208337	-1.45000	-1.970916	-0.50000	C.208337
-1.40000	-2.380044	-0.45000	C.248931	-1.40000	-2.380044	-0.45000	C.248931
-1.35000	-1.855027	-0.40000	C.288938	-1.35000	-1.855027	-0.40000	C.288938
-1.30000	-1.312234	-0.35000	C.328566	-1.30000	-1.312234	-0.35000	C.328566
-1.25000	-0.822938	-0.30000	C.367833	-1.25000	-0.822938	-0.30000	C.367833
-1.20000	-0.849465	-0.25000	C.406846	-1.20000	-0.849465	-0.25000	C.406846
-1.15000	-0.802314	-0.20000	C.445683	-1.15000	-0.802314	-0.20000	C.445683
-1.10000	-0.745202	-0.15000	C.484352	-1.10000	-0.745202	-0.15000	C.484352
-1.05000	-0.642032	-0.10000	C.522823	-1.05000	-0.642032	-0.10000	C.522823
-1.00000	-0.611559	-0.05000	C.561158	-1.00000	-0.611559	-0.05000	C.561158
-0.95000	-0.535782	0.00000	C.600300	-0.95000	-0.535782	0.00000	C.600300
-0.90000	-0.453786	0.05000	C.639271	-0.90000	-0.453786	0.05000	C.639271
-0.85000	-0.365733	0.10000	C.678092	-0.85000	-0.365733	0.10000	C.678092
-0.80000	-0.284482	0.15000	C.716750	-0.80000	-0.284482	0.15000	C.716750
-0.75000	-0.198605	0.20000	C.755247	-0.75000	-0.198605	0.20000	C.755247
-0.70000	-0.112444	0.25000	C.793581	-0.70000	-0.112444	0.25000	C.793581
-0.65000	-0.026184	0.30000	C.831762	-0.65000	-0.026184	0.30000	C.831762
-0.60000	0.060097	0.35000	C.869793	-0.60000	0.060097	0.35000	C.869793
-0.55000	0.146333	0.40000	C.907683	-0.55000	0.146333	0.40000	C.907683
-0.50000	J.222966	0.45000	C.945433	-0.50000	J.222966	0.45000	C.945433
-0.45000	J.193186	0.50000	C.983054	-0.45000	J.193186	0.50000	C.983054
-0.40000	J.163457	0.55000	C.102056	-0.40000	J.163457	0.55000	C.102056
-0.35000	0.133805	0.60000	C.106000	-0.35000	0.133805	0.60000	C.106000
-0.30000	J.104237	0.65000	C.110000	-0.30000	J.104237	0.65000	C.110000
-0.25000	0.074749	0.70000	C.114000	-0.25000	0.074749	0.70000	C.114000
-0.20000	0.045325	0.75000	C.118000	-0.20000	0.045325	0.75000	C.118000
-0.15000	J.015944	0.80000	C.122000	-0.15000	J.015944	0.80000	C.122000
-0.10000	-0.013422	0.85000	C.126000	-0.10000	-0.013422	0.85000	C.126000
-0.05000	-0.042801	0.90000	C.130000	-0.05000	-0.042801	0.90000	C.130000
0.00000	-0.072220	0.95000	C.134000	0.00000	-0.072220	0.95000	C.134000
0.05000	J.083347	1.00000	C.138000	0.05000	J.083347	1.00000	C.138000
0.10000	-0.074860	1.05000	C.142000	0.10000	-0.074860	1.05000	C.142000
0.15000	J.066354	1.10000	C.146000	0.15000	J.066354	1.10000	C.146000
0.20000	-0.057830	1.15000	C.150000	0.20000	-0.057830	1.15000	C.150000
0.25000	J.049292	1.20000	C.154000	0.25000	J.049292	1.20000	C.154000
0.30000	-0.040744	1.25000	C.158000	0.30000	-0.040744	1.25000	C.158000
0.35000	-0.032189	1.30000	C.162000	0.35000	-0.032189	1.30000	C.162000
0.40000	-0.023675	1.35000	C.166000	0.40000	-0.023675	1.35000	C.166000
0.45000	-0.015058	1.40000	C.170000	0.45000	-0.015058	1.40000	C.170000
0.50000	-0.006489	1.45000	C.174000	0.50000	-0.006489	1.45000	C.174000
0.55000	0.002082	1.50000	C.178000	0.55000	0.002082	1.50000	C.178000
0.60000	J.004395	1.55000	C.182000	0.60000	J.004395	1.55000	C.182000
0.65000	0.004568	1.60000	C.186000	0.65000	0.004568	1.60000	C.186000
0.70000	J.004741	1.65000	C.190000	0.70000	J.004741	1.65000	C.190000
0.75000	0.004914	1.70000	C.194000	0.75000	0.004914	1.70000	C.194000
0.80000	J.005087	1.75000	C.198000	0.80000	J.005087	1.75000	C.198000
0.85000	0.005260	1.80000	C.202000	0.85000	0.005260	1.80000	C.202000
0.90000	0.005433	1.85000	C.206000	0.90000	0.005433	1.85000	C.206000
0.95000	0.005606	1.90000	C.210000	0.95000	0.005606	1.90000	C.210000
1.00000	0.005778	1.95000	C.214000	1.00000	0.005778	1.95000	C.214000
1.05000	0.005951	2.00000	C.218000	1.05000	0.005951	2.00000	C.218000
1.10000	0.006124	2.05000	C.222000	1.10000	0.006124	2.05000	C.222000
1.15000	J.006297	2.10000	C.226000	1.15000	J.006297	2.10000	C.226000
1.20000	0.006470	2.15000	C.230000	1.20000	0.006470	2.15000	C.230000
1.25000	J.006643	2.20000	C.234000	1.25000	J.006643	2.20000	C.234000
1.30000	0.006816	2.25000	C.238000	1.30000	0.006816	2.25000	C.238000
1.35000	-0.006989	2.30000	C.242000	1.35000	-0.006989	2.30000	C.242000
1.40000	0.007162	2.35000	C.246000	1.40000	0.007162	2.35000	C.246000
1.45000	-0.007335	2.40000	C.250000	1.45000	-0.007335	2.40000	C.250000
1.50000	0.007508	2.45000	C.254000	1.50000	0.007508	2.45000	C.254000
1.55000	0.007681	2.50000	C.258000	1.55000	0.007681	2.50000	C.258000
1.60000	-0.007854	2.55000	C.262000	1.60000	-0.007854	2.55000	C.262000
1.65000	0.008027	2.60000	C.266000	1.65000	0.008027	2.60000	C.266000
1.70000	0.008200	2.65000	C.270000	1.70000	0.008200	2.65000	C.270000
1.75000	-0.008373	2.70000	C.274000	1.75000	-0.008373	2.70000	C.274000
1.80000	0.008546	2.75000	C.278000	1.80000	0.008546	2.75000	C.278000
1.85000	0.008719	2.80000	C.282000	1.85000	0.008719	2.80000	C.282000
1.90000	-0.008892	2.85000	C.286000	1.90000	-0.008892	2.85000	C.286000
1.95000	0.009065	2.90000	C.290000	1.95000	0.009065	2.90000	C.290000
2.00000	-0.009238	2.95000	C.294000	2.00000	-0.009238	2.95000	C.294000
2.00406	-0.019729	3.00000	C.298000	2.00406	-0.019729	3.00000	C.298000

CALCOMP PLOTTER OUTPUT - SYMMETRIC PROBLEM

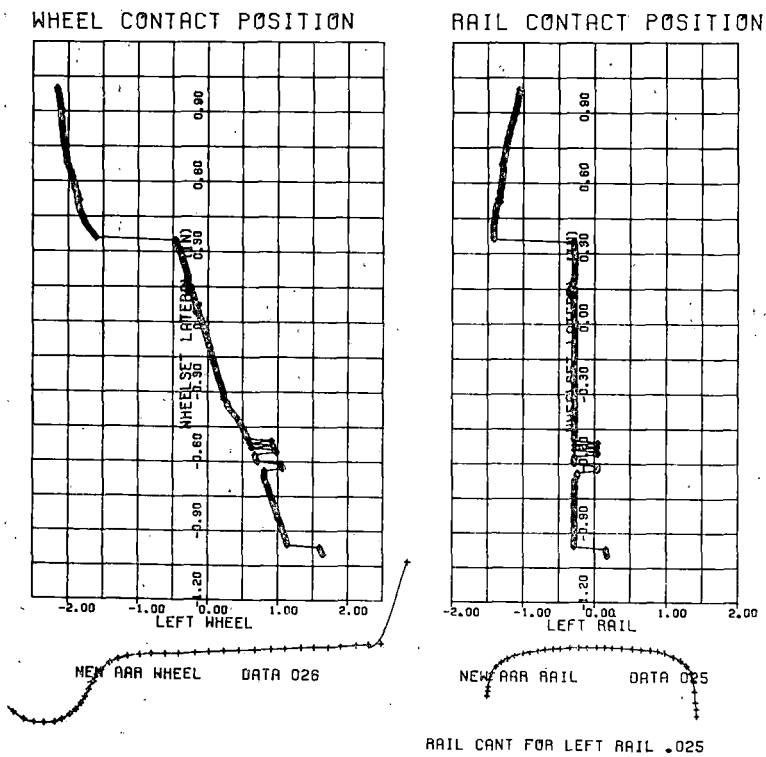
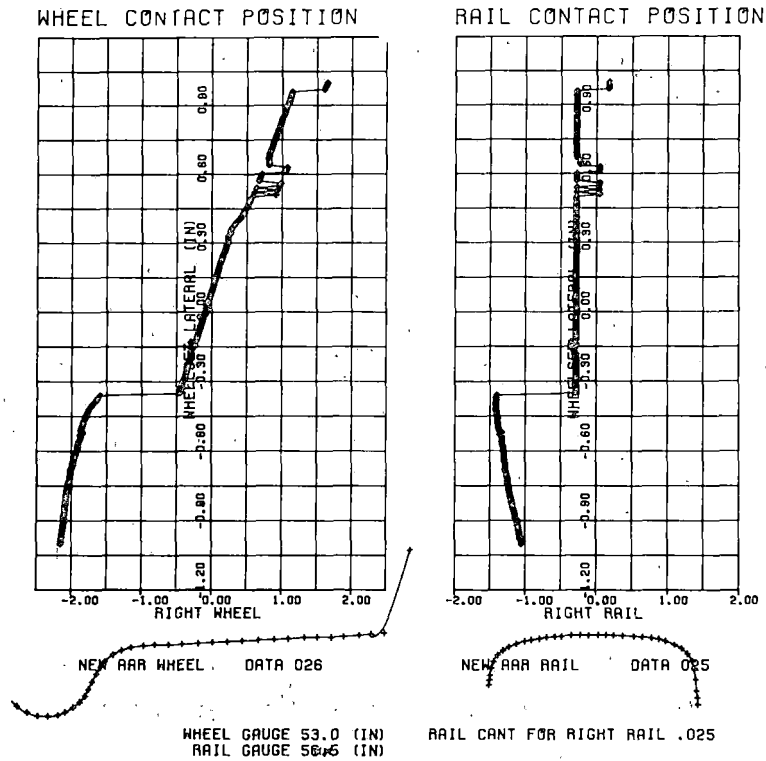
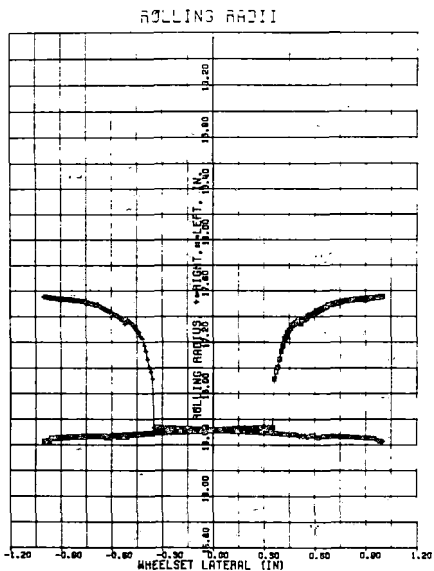
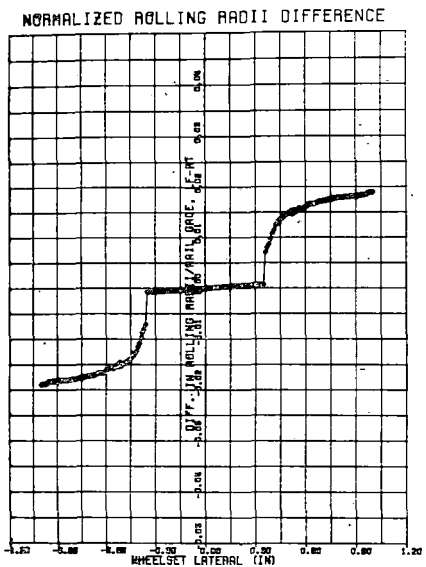


FIGURE 3A. CALCOMP PLOTTER OUTPUT - SYMMETRIC PROBLEM, WHEEL/RAIL PROFILES AND LOCATION OF CONTACT POINTS.



RIGHT SIDE

NEW AAR WHEEL DATA 026
 NEW AAR RAIL DATA 025
 RAIL CANT FOR RIGHT RAIL .025

LEFT SIDE

NEW AAR WHEEL DATA 026
 NEW AAR RAIL DATA 025
 RAIL CANT FOR LEFT RAIL .025

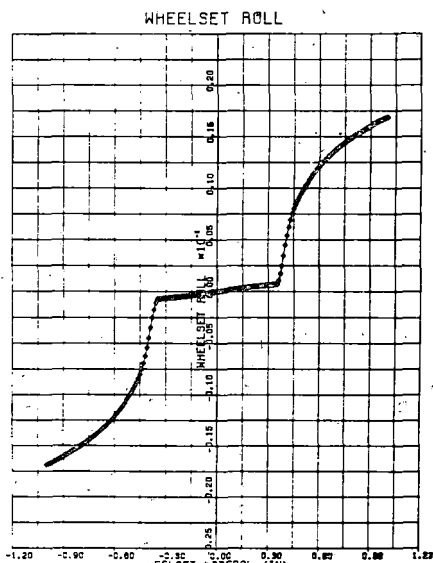
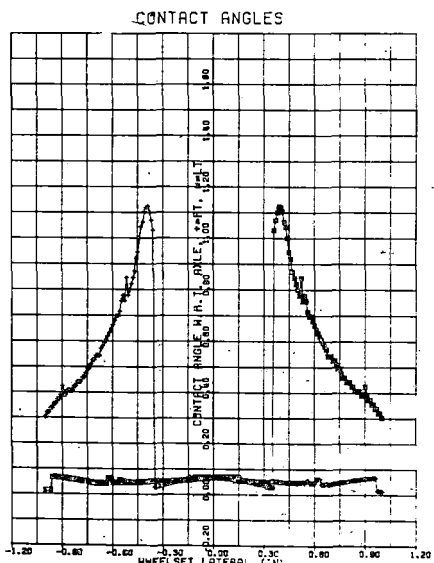
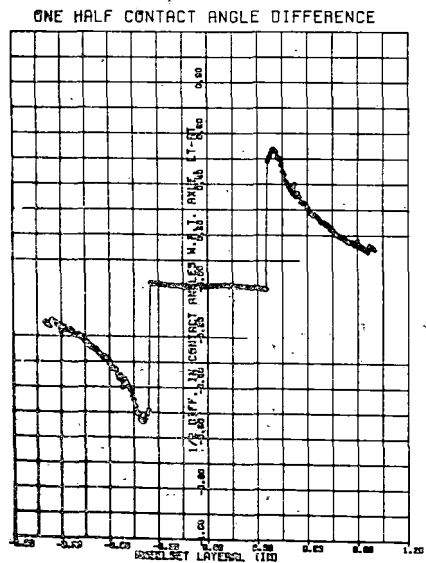


FIGURE 3B. CALCOMP PLOTTER OUTPUT - SYMMETRIC PROBLEM, GEOMETRIC CONSTRAINTS.

PARTIAL LISTING OF PUNCHED CARD OUTPUT - SYMMETRIC PROBLEM

0.530000D+02 0.295630D+02 0.565000D+02 0.297500D+02 0.250000D-01 0.250000D-01

COEFFICIENTS FOR PROFILE CURVE FITS

NEW AAR WHEEL DATA 026

14

1 0.4405190+03-0.7104370+03 0.4421820+03-0.1210410+03 0.1227390+02
 0.2000000+03 0.2298310+01
 2 0.1555370+02 0.1575400+01-0.1006580+01 0.2731350+00-0.2813760-01
 0.2298310+01 0.1819670+01
 3 0.1570280+02 0.2427170+01-0.2778270+01 0.1344880+01-0.2368990+00
 0.1819670+01 0.1334990+01
 4 0.1656630+02-0.3707880+00 0.6042870+00-0.4639510+00 0.1241230+00
 0.1334990+01 0.8050820+00
 5 0.1650960+02-0.6147290-01 0.1825800-01-0.3133290-02-0.3608650-02
 0.8050820+00 0.2388720+00
 6 0.1650960+02-0.5166240-01 0.3217590-01 0.1192490-01-0.1154260+00
 0.2388720+00-0.2980390+00
 7 0.1650960+02-0.8422190-01 0.1647020-01 0.2117730+00 0.1642800+00
 -0.2980390+00-0.7976910+00
 8 0.1689900+02 0.1639960+01 0.2765980+01 0.2088070+01 0.6248470+00
 -0.7976910+00-0.1204040+01
 9 0.2853000+02 0.3839280+02 0.4606830+02 0.2463610+02 0.5003670+01
 -0.1204040+01-0.1512950+01
 10 -0.2695490+02-0.1189490+03-0.1206460+03-0.5360570+02-0.8721790+01
 -0.1512950+01-0.1647350+01
 11 0.5869440+03 0.1284520+04 0.1079240+04 0.4009410+03 0.5563560+02
 -0.1647350+01-0.1790980+01
 12 -0.1476490+03-0.3212700+03-0.2359790+03-0.7743020+02-0.9558570+01
 -0.1790980+01-0.2012950+01
 13 0.4283870+01-0.1754740+02-0.8679330+01-0.1954130+01-0.1759460+00
 -0.2012950+01-0.2325360+01
 14 0.5214570+02 0.5661550+02 0.3395990+02 0.8804470+01 0.8263800+00
 -0.2325360+01-0.2829460+01

NEW AAR RATL DATA 025

14

1 -0.1239710+07 0.3493540+07-0.3691700+07 0.1733770+07-0.3053340+06
 0.2000000+03 0.1418880+01
 2 -0.2234710+05 0.6678590+05-0.7481690+05 0.3724760+05-0.6953580+04
 0.1418880+01 0.1377260+01
 3 -0.2187900+03 0.7699750+03-0.9822300+03 0.5558040+03-0.1178130+03
 0.1377260+01 0.1203180+01
 4 -0.2830060-01 0.2871520+02-0.4312910+02 0.2858740+02-0.7144460+01
 0.1203180+01 0.9312770+00
 5 0.6709010+01 0.2383070+01-0.5439600+01 0.5314960+01-0.1964740+01
 0.9312770+00 0.6536630+00
 6 0.7115480+01-0.2075830+00 0.6369020+00-0.9094470+00 0.3865160+00
 0.6536630+00 0.3191580+00
 7 0.7094790+01 0.2694400-01-0.9564850-01-0.4791310+00 0.9752210+00
 0.3191580+00 0.3666800-01

8 0.7094520+01 0.2457210-01 0.4792250-02-0.4739000+00-0.1108990+01
 0.3666800-01-0.2764040+00
 9 0.7038680+01-0.6152510+00-0.2305770+01-0.3374480+01-0.1819050+01
 -0.2754040+00-0.5724650+00
 10 0.6887400+01-0.1039940+01-0.1636330+01-0.8570420+00-0.1212760+00
 -0.5724650+00-0.3298550+00
 11 0.9771500+01 0.1084690+02 0.1610840+02 0.1049630+02 0.2466900+01
 -0.8298550+00-0.1109280+01
 12-0.1452650+02-0.7645140+02-0.1011520+03-0.5929450+02-0.1306350+02
 -0.1109280+01-0.1333180+01
 13-0.1632580+04-0.4911880+04-0.5515700+04-0.2751820+04-0.5147570+03
 -0.1333180+01-0.1458610+01
 14 0.1787410+06 0.4888190+06 0.5012280+06 0.2283780+06 0.3901320+05
 -0.1458610+01-0.1503170+01

NEW AAR WHEEL DATA 026

14

1 0.4405190+03-0.7104370+03 0.4421820+03-0.1210410+03 0.1227390+02
 0.2000000+03 0.2298310+01
 2 0.1555370+02 0.1575400+01-0.1006580+01 0.2731350+00-0.2813760-01
 0.2298310+01 0.1819670+01
 3 0.1570280+02 0.2427170+01-0.2778270+01 0.1344880+01-0.2368990+00
 0.1819670+01 0.1334990+01
 4 0.1656830+02-0.3707880+00 0.6042870+00-0.4639510+00 0.1241230+00
 0.1334990+01 0.8050820+00
 5 0.1650960+02-0.6147290-01 0.1825800-01-0.3133290-02-0.3608650-02
 0.8050820+00 0.2388720+00
 6 0.1650960+02-0.6166240-01 0.3217590-01 0.1192490-01-0.1154260+00
 0.2388720+00-0.2980390+00
 7 0.1650820+02-0.8422190-01 0.1647020-01 0.2117730+00 0.1642800+00
 -0.2980390+00-0.7976910+00
 8 0.1689800+02 0.1639960+01 0.2765980+01 0.2088070+01 0.6248470+00
 -0.7976910+00-0.1204040+01
 9 0.2053000+02 0.3839280+02 0.4606830+02 0.2463610+02 0.5003670+01
 -0.1204040+01-0.1512950+01
 10-0.2695490+02-0.1189490+03-0.1206460+03-0.5360570+02-0.8721790+01
 -0.1512950+01-0.1647350+01
 11 0.5869440+03 0.1284520+04 0.1079240+04 0.4009410+03 0.5563560+02
 -0.1647350+01-0.1790980+01
 12-0.1476490+03-0.3212700+03-0.2359790+03-0.7743020+02-0.9558570+01
 -0.1790980+01-0.2012950+01
 13 0.4283870+01-0.1754740+02-0.8679330+01-0.1954130+01-0.1759460+00
 -0.2012950+01-0.2325360+01
 14 0.5214570+02 0.5661550+02 0.3395990+02 0.8804470+01 0.8263800+00
 -0.2325360+01-0.2829460+01

NEW AAR RAIL DATA 025

14

1-0.1239710+07 0.3493540+07-0.3691700+07 0.1733770+07-0.3053340+06
 0.2000000+03 0.1418880+01
 2-0.2234710+05 0.6678590+05-0.7481690+05 0.3724760+05-0.6953580+04
 0.1418880+01 0.1377260+01
 3-0.2187900+03 0.7699750+03-0.9822300+03 0.5558040+03-0.1178130+03
 5 0.6709010+01 0.2383070+01-0.5439600+01 0.5314960+01-0.1964740+01

0.0312770+00 0.6536630+00
 6 0.7115480+01-0.2075830+00 0.6369020+00-0.9094470+00 0.3865160+00
 0.5536630+00 0.3191580+00
 7 0.7094700+01 0.2694400-01-0.9564850-01-0.4791310+00 0.9752210+00
 9 0.7038580+01-0.6152510+00-0.2305770+01-0.3374480+01-0.1819050+01
 -0.2754040+00-0.5724650+00
 10 0.6867400+01-0.1039940+01-0.1636330+01-0.8570420+00-0.1212760+00
 -0.5724650+00-0.8298550+00
 11 0.9771500+01 0.1084690+02 0.1610640+02 0.1049630+02 0.2466900+01
 -0.8298550+00-0.1109280+01
 12-0.1452450+02-0.7645140+02-0.1011520+03-0.5929450+02-0.1306350+02
 -0.1109280+01-0.1333180+01
 13-0.1632580+04-0.4911880+04-0.5515700+04-0.2751820+04-0.5147570+03
 -0.1333180+01-0.1458610+01
 14 0.1767410+06 0.4888190+06 0.5012280+06 0.2283780+06 0.3901320+05
 -0.1458610+01-0.1503170+01

THE DATA IS ORDERED AS FOLLOWS:

CONTACT POINTS, GEOMETRIC CONSTRAINTS, AND PROFILE CURVATURES
AS A FUNCTION OF WHEELSET LATERAL DISPLACEMENT

XW = WHEELSET LATERAL, POSITIVE TO THE LEFT (IN)
 Y1 = CONTACT LOCATION ON RIGHT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
 Y2 = CONTACT LOCATION ON RIGHT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 Y3 = CONTACT LOCATION ON LEFT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
 Y4 = CONTACT LOCATION ON LEFT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 PR = ROLLING RADII, RIGHT WHEEL (IN)
 YR = RAIL HEAD PROFILE HEIGHT, RIGHT RAIL (IN)
 RL = ROLLING RADII, LEFT WHEEL (IN)
 YL = RAIL HEAD PROFILE HEIGHT, LEFT RAIL (IN)
 MR = CONTACT ANGLE W.R.T. AXLE, RIGHT WHEEL (RAD)
 ML = CONTACT ANGLE W.R.T. AXLE, LEFT WHEEL (RAD)
 (PR-RR)/2A = NORMALIZED DIFFERENCE IN ROLLING RADII (IN/IN)
 (ML-MR)/2 = NORMALIZED DIFFERENCE IN CONTACT ANGLES (RAD)
 WR = WHEELSET ROLL ANGLE W.R.T. HORIZONTAL, POSITIVE UP ON LEFT (RAD)
 YCG = VERTICAL DISPLACEMENT OF WHEELSET CENTROID FROM NOMINAL POS. (IN)
 RR CRV = PRINCIPAL ROLLING CURVATURE OF RIGHT WHEEL PROFILE (1/IN)
 RL CRV = PRINCIPAL ROLLING CURVATURE OF LEFT WHEEL PROFILE (1/IN)
 CWR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYP = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CWL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)

202 5

-0.1000000+01-0.2159460+01-0.1055060+01 0.1540540+01 0.1717930+00 0.1755500+02
 0.6987950+01 0.1642940+02 0.7095020+01 0.3031390+00 0.1375680-01-0.1891750-01
 -0.1446910+00-0.1685400-01 0.4185990+00
 0.5436560-01 0.6086080-01 0.1596780+01 0.9699470+00-0.9239000-02 0.8316530-01

-0.9900000+00	-0.2149460+01	-0.1056220+01	0.1630540+01	0.1728840+00	0.1755180+02
0.6987580+01	0.1642950+02	0.7094990+01	0.3203360+00	0.1412320-01	0.1886100-01
-0.1531070+00	-0.1678990-01	0.4168740+00			
0.5407600-01	0.6086000-01	0.1597990+01	0.9689660+00	-0.8950670-02	0.8291880-01
-0.0800000+00	-0.2149460+01	-0.1067370+01	0.1610540+01	0.1640200+00	0.1755180+02
0.6983930+01	0.1642980+02	0.7095230+01	0.3203360+00	0.1521070-01	0.1885610-01
-0.1525630+00	-0.1672320-01	0.4150840+00			
0.5407600-01	0.6085790-01	0.1597990+01	0.9593660+00	-0.8374060-02	0.8492240-01
-0.9700000+00	-0.2139460+01	-0.1068600+01	0.1600540+01	0.1651850+00	0.1754830+02
0.6983520+01	0.1643000+02	0.7095200+01	0.3375750+00	0.1592030-01	0.1879610-01
-0.1605280+00	-0.1665470-01	0.4132510+00			
0.5376920-01	0.6085660-01	0.1597110+01	0.9582890+00	-0.8085770-02	0.8465910-01
-0.0600000+00	-0.2139460+01	-0.1079880+01	0.1140540+01	-0.2838410+00	0.1754830+02
0.6979640+01	0.1645120+02	0.7092910+01	0.3375750+00	0.6621020-01	0.1844020-01
-0.1356830+00	-0.1658330-01	0.4150220+00			
0.5376920-01	0.6065280-01	0.1597110+01	0.9483140+00	0.5170640-02	0.2611690+00
-0.0500000+00	-0.2129460+01	-0.1081390+01	0.1130540+01	-0.2824100+00	0.1754470+02
0.6979110+01	0.1645180+02	0.7092970+01	0.3548450+00	0.6589340-01	0.1836840-01
-0.1444760+00	-0.1649840-01	0.4133380+00			
0.5344630-01	0.6065170-01	0.1594140+01	0.9469570+00	0.5458850-02	0.2605230+00
-0.0400000+00	-0.2129460+01	-0.1092700+01	0.1120540+01	-0.2811230+00	0.1754470+02
0.6975040+01	0.1645250+02	0.7093020+01	0.3548450+00	0.6551850-01	0.1835740-01
-0.1446630+00	-0.1641350-01	0.4115590+00			
0.5344630-01	0.6065070-01	0.1594140+01	0.9366970+00	0.5747070-02	0.2599410+00
-0.0300000+00	-0.2119460+01	-0.1094280+01	0.1110540+01	-0.2796200+00	0.1754090+02
0.6974460+01	0.1645310+02	0.7093090+01	0.3721330+00	0.6508830-01	0.1828240-01
-0.1535220+00	-0.1632440-01	0.4097470+00			
0.5310740-01	0.6065000-01	0.1589090+01	0.9352390+00	0.6035290-02	0.2592620+00
-0.0200000+00	-0.2119460+01	-0.1105820+01	0.1100540+01	-0.2781060+00	0.1754090+02
0.6970120+01	0.1645380+02	0.7093150+01	0.3721330+00	0.6460590-01	0.1827150-01
-0.1537640+00	-0.1623460-01	0.4078330+00			
0.5310740-01	0.6064950-01	0.1589090+01	0.9245290+00	0.6126110-02	0.2585770+00
-0.0100000+00	-0.2109460+01	-0.1107420+01	0.1090540+01	-0.2765940+00	0.1753690+02
0.6969500+01	0.1645440+02	0.7093210+01	0.3894290+00	0.6407420-01	0.1819340-01
-0.1626770+00	-0.1614170-01	0.4059010+00			
0.5275300-01	0.6064920-01	0.1581980+01	0.9230270+00	0.6091540-02	0.2578930+00
-0.0000000+00	-0.2089460+01	-0.1099610+01	0.1070540+01	-0.2845840+00	0.1752830+02
0.6972470+01	0.1645570+02	0.7092870+01	0.4239950+00	0.6267460-01	0.1802720-01
-0.1605600+00	-0.1603540-01	0.4035730+00			
0.5199890-01	0.6064920-01	0.1561790+01	0.9303230+00	0.6022390-02	0.2615050+00
-0.8900000+00	-0.2109460+01	-0.1131190+01	0.1060540+01	-0.2828840+00	0.1753690+02
0.6958480+01	0.1645630+02	0.7092950+01	0.3894290+00	0.6221270-01	0.1816150-01
-0.1636080+00	-0.1592470-01	0.4008920+00			
0.5275300-01	0.6064940-01	0.1581960+01	0.9003090+00	0.5987820-02	0.2607370+00
-0.8800000+00	-0.2109460+01	-0.1142860+01	0.1050540+01	-0.2812340+00	0.1753690+02
0.6953670+01	0.1645600+02	0.7093020+01	0.3894290+00	0.6151340-01	0.1815110-01
-0.1639580+00	-0.1582690-01	0.3987310+00			
0.5275300-01	0.6064970-01	0.1581980+01	0.8888980+00	0.5953250-02	0.2599920+00
-0.8700000+00	-0.2099460+01	-0.1144610+01	0.1040540+01	-0.2795800+00	0.1753270+02
0.6952940+01	0.1645760+02	0.7093090+01	0.4067200+00	0.6077950-01	0.1807010-01
-0.1729700+00	-0.1572880-01	0.3966320+00			
0.5238340-01	0.6065020-01	0.1572870+01	0.8871780+00	0.5918670-02	0.2592440+00
-0.8600000+00	-0.2099460+01	-0.1156440+01	0.1030540+01	-0.2777740+00	0.1753270+02
0.6947990+01	0.1645820+02	0.7093160+01	0.4067200+00	0.6001410-01	0.1806000-01

-0.1733530+00-0.1562850-01 0.3943940+00
 0.5238340-01 0.6065080-01 0.1572870+01 0.8754460+00 0.5884100-02 0.2584270+00
 -0.8500000+00-0.2099460+01-0.1167940+01 0.1010540+01-0.2863100+00 0.1753270+02
 0.6943100+01 0.1645930+02 0.7092790+01 0.4067200+00 0.5840040-01-0.1804000-01
 -0.1741600+00-0.1553440-01 0.3921330+00
 0.5238340-01 0.6065220-01 0.1572870+01 0.8639240+00 0.5814940-02 0.2622840+00
 -0.8400000+00-0.2099460+01-0.1179680+01 0.1000540+01-0.2845890+00 0.1753270+02
 0.6938020+01 0.1645990+02 0.7092870+01 0.4067200+00 0.5755810-01-0.1803030-01
 -0.1745810+00-0.1543240-01 0.3896250+00
 0.5238340-01 0.6065300-01 0.1572870+01 0.8520440+00 0.5780360-02 0.2615070+00
 -0.8300000+00-0.2089460+01-0.1191500+01 0.9905410+00-0.2826620+00 0.1752830+02
 0.6937220+01 0.1645050+02 0.7092950+01 0.4239950+00 0.5669610-01-0.1794660-01
 -0.1836500+00-0.1533000-01 0.3875710+00
 0.5199800-01 0.6065300-01 0.1561790+01 0.8501920+00 0.5745790-02 0.2607270+00
 -0.8200000+00-0.2089460+01-0.1193290+01 0.9805410+00-0.2811030+00 0.1752830+02
 0.6932000+01 0.1646110+02 0.7093020+01 0.4239950+00 0.5581730-01-0.1793710-01
 -0.1840890+00-0.1522580-01 0.3851820+00
 0.5199890-01 0.6065480-01 0.1561790+01 0.8381670+00 0.5711200-02 0.2599320+00
 -0.8100000+00-0.2079460+01-0.1195190+01 0.9705410+00-0.2793040+00 0.1752370+02
 0.6931150+01 0.1646160+02 0.7093100+01 0.4412420+00 0.5492480-01-0.1785020-01
 -0.1931590+00-0.1511910-01 0.3827860+00
 0.5159990-01 0.6065580-01 0.1548810+01 0.8362230+00 0.5676620-02 0.2591190+00
 -0.8000000+00-0.2079460+01-0.1207010+01 0.9605410+00-0.2775100+00 0.1752370+02
 0.6925750+01 0.1646220+02 0.7093170+01 0.4412420+00 0.5402140-01-0.1784100-01
 -0.1936100+00-0.1501200-01 0.3802990+00
 0.5159990-01 0.6065680-01 0.1548810+01 0.8240780+00 0.5642040-02 0.2583080+00
 -0.7900000+00-0.2079460+01-0.1218820+01 0.9405410+00-0.2867350+00 0.1752370+02
 0.6920170+01 0.1646320+02 0.7092820+01 0.4412420+00 0.5219420-01-0.1782310-01
 -0.1945240+00-0.1490730-01 0.3776420+00
 0.5159990-01 0.6065870-01 0.1548810+01 0.9605330+00 0.5572870-02 0.2620250+00
 -0.7800000+00-0.2069460+01-0.1220810+01 0.9305410+00-0.2838470+00 0.1751890+02
 0.6919210+01 0.1646370+02 0.7092900+01 0.4584500+00 0.5127630-01-0.1773330-01
 -0.2035870+00-0.1479550-01 0.3750770+00
 0.5116710-01 0.6065970-01 0.1533970+01 0.1023980+01 0.5538290-02 0.2611720+00
 -0.7700000+00-0.2069460+01-0.1232790+01 0.9205410+00-0.2818910+00 0.1751890+02
 0.6913290+01 0.1646420+02 0.7092990+01 0.4584500+00 0.5035940-01-0.1772470-01
 -0.2040450+00-0.1467960-01 0.3723160+00
 0.5118710-01 0.6066070-01 0.1533970+01 0.1390110+01 0.5503700-02 0.2602880+00
 -0.7600000+00-0.2059460+01-0.1234870+01 0.9105410+00-0.2799160+00 0.1751380+02
 0.6912240+01 0.1646470+02 0.7093070+01 0.4756060+00 0.4944660-01-0.1763160-01
 -0.2130800+00-0.1456270-01 0.3695870+00
 0.5076080-01 0.6066160-01 0.1517370+01 0.1450390+01 0.5469120-02 0.2593960+00
 -0.7500000+00-0.2049460+01-0.1237010+01 0.9005410+00-0.2778880+00 0.1750860+02
 0.6911140+01 0.1646520+02 0.7093160+01 0.4926990+00 0.4854080-01-0.1753490-01
 -0.2226790+00-0.1444140-01 0.3667270+00
 0.5032160-01 0.6066250-01 0.1499090+01 0.1511160+01 0.5434530-02 0.2584790+00

ETC.

LISTING OF INPUT CARDS - ASYMMETRIC PROBLEM

.02
 000001
 001000
 001000
 061000
 53.0 57.5 .025 .025
 MODERATELY WORN WHEEL DATA 020
 3.0625
 0000
 1 1

0.2426139E+01	-0.1636135E+02	0.2356796E+01	-0.1637052E+02
0.2310379E+01	-0.1637600E+02	0.2255187E+01	-0.1638466E+02
0.2194052E+01	-0.1639578E+02	0.2131219E+01	-0.1640157E+02
0.2069517E+01	-0.1641274E+02	0.2014892E+01	-0.1641339E+02
0.1961965E+01	-0.1641689E+02	0.1899897E+01	-0.1641766E+02
0.1837996E+01	-0.1642466E+02	0.1706388E+01	-0.1643241E+02
0.1652892E+01	-0.1643501E+02	0.1591191E+01	-0.1643305E+02
0.1522414E+01	-0.1643066E+02	0.1468921E+01	-0.1642669E+02
0.1407786E+01	-0.1642724E+02	0.1345518E+01	-0.1642546E+02
0.1292591E+01	-0.1642369E+02	0.1246740E+01	-0.1641792E+02
0.1185604E+01	-0.1641339E+02	0.1124469E+01	-0.1640888E+02
0.1040408E+01	-0.1640848E+02	0.9781411E+00	-0.1640560E+02
0.9099301E+00	-0.1640576E+02	0.8558706E+00	-0.1640162E+02
0.7947354E+00	-0.1639981E+02	0.6801070E+00	-0.1639132E+02
0.6113299E+00	-0.1638622E+02	0.5425529E+00	-0.1638342E+02
0.4579259E+00	-0.1638334E+02	0.3962247E+00	-0.1638538E+02
0.3268815E+00	-0.1638565E+02	0.2581045E+00	-0.1638540E+02
0.1734775E+00	-0.1638223E+02	0.1047004E+00	-0.1638213E+02
0.4299915E-01	-0.1638326E+02	-0.3418267E-02	-0.1638344E+02
-0.1027630E+00	-0.1638253E+02	-0.1644642E+00	-0.1638017E+02
-0.2179576E+00	-0.1638113E+02	-0.2720169E+00	-0.1637954E+02
-0.3331521E+00	-0.1638013E+02	-0.4024952E+00	-0.1637759E+02
-0.4789142E+00	-0.1637744E+02	-0.5406154E+00	-0.1638026E+02
-0.6028827E+00	-0.1638264E+02	-0.6869437E+00	-0.1638493E+02
-0.7639287E+00	-0.1638717E+02	-0.8338379E+00	-0.1639190E+02
-0.9031810E+00	-0.1639995E+02	-0.9654484E+00	-0.1640773E+02
-0.1027716E+01	-0.1641790E+02	-0.1097625E+01	-0.1642993E+02
-0.1152250E+01	-0.1644249E+02	-0.1207442E+01	-0.1645221E+02
-0.1284427E+01	-0.1646835E+02	-0.1331977E+01	-0.1648047E+02
-0.1379526E+01	-0.1649506E+02	-0.1449435E+01	-0.1651424E+02
-0.1504627E+01	-0.1652915E+02	-0.1559818E+01	-0.1655545E+02
-0.1616708E+01	-0.1658703E+02	-0.1664824E+01	-0.1662938E+02
-0.1699354E+01	-0.1665851E+02	-0.1739827E+01	-0.1670933E+02
-0.1766716E+01	-0.1674117E+02	-0.1791906E+01	-0.1678137E+02
-0.1818228E+01	-0.1682096E+02	-0.1844550E+01	-0.1687028E+02
-0.1863230E+01	-0.1690551E+02	-0.1880778E+01	-0.1694565E+02
-0.1900024E+01	-0.1699547E+02	-0.1910496E+01	-0.1702543E+02
-0.1929743E+01	-0.1710227E+02	-0.1933705E+01	-0.1711329E+02
-0.1951819E+01	-0.1718142E+02	-0.1962858E+01	-0.1721567E+02
-0.1973330E+01	-0.1725868E+02	-0.1984934E+01	-0.1730452E+02
-0.1995406E+01	-0.1736129E+02	-0.1998803E+01	-0.1737267E+02
-0.2016917E+01	-0.1743076E+02	-0.2035597E+01	-0.1747601E+02
-0.2045503E+01	-0.1750527E+02	-0.2055976E+01	-0.1753198E+02

-0.2082298E+01 -0.1757451E+02 -0.2130979E+01 -0.1761585E+02
 -0.2186737E+01 -0.1764060E+02 -0.2249004E+01 -0.1765983E+02
 -0.2311838E+01 -0.1766874E+02 -0.2404106E+01 -0.1767679E+02
 -0.2488733E+01 -0.1767543E+02 -0.2572794E+01 -0.1765680E+02
 -0.2531099E+01 -0.1763573E+02 -0.2683460E+01 -0.1769249E+02

NEW AAR RAIL DATA 025

1.5
 0072
 0 0

0.1432941D	01	0.6106113D	01
0.1429198D	01	0.6159716D	01
0.1425683D	01	0.6202402D	01
0.1422167D	01	0.6255852D	01
0.1418878D	01	0.6299916D	01
0.1411545D	01	0.6407996D	01
0.1408483D	01	0.6459593D	01
0.1405270D	01	0.6502649D	01
0.1384819D	01	0.6620405D	01
0.1377259D	01	0.6648965D	01
0.1356582D	01	0.6720330D	01
0.1327059D	01	0.6776739D	01
0.1288766D	01	0.6827859D	01
0.1246050D	01	0.6872249D	01
0.1203183D	01	0.6906820D	01
0.1155818D	01	0.6935483D	01
0.1104030D	01	0.6958672D	01
0.1039200D	01	0.6985167D	01
0.9787940D	00	0.7009135D	01
0.9312770D	00	0.7025605D	01
0.8836100D	00	0.7038043D	01
0.8359420D	00	0.7045928D	01
0.7838520D	00	0.7052503D	01
0.7187200D	00	0.7059757D	01
0.6536630D	00	0.7068334D	01
0.5929540D	00	0.7075092D	01
0.5364410D	00	0.7079995D	01
0.4495730D	00	0.7083493D	01
0.3843660D	00	0.7085862D	01
0.3191580D	00	0.7088399D	01
0.2496790D	00	0.7091257D	01
0.1931660D	00	0.7093536D	01
0.1453470D	00	0.7095754D	01
0.9325698D	-01	0.7096725D	01
0.3666800D	-01	0.7096641D	01
-0.3731000D	-01	0.7092916D	01
-0.9824601D	-01	0.7091356D	01
-0.1591060D	00	0.7090965D	01
-0.2156190D	00	0.7093344D	01
-0.2764040D	00	0.7093060D	01
-0.3417630D	00	0.7090148D	01
-0.3809630D	00	0.7087274D	01
-0.4766760D	00	0.7078416D	01
-0.5160275D	00	0.7077331D	01
-0.5724651D	00	0.7072011D	01

-0.62478230	00	0.70704020	01
-0.68571830	00	0.70515160	01
-0.72941680	00	0.70554230	01
-0.78608120	00	0.70413460	01
-0.82985530	00	0.70346050	01
-0.89948560	00	0.70233440	01
-0.94745560	00	0.70174310	01
-0.99107850	00	0.70067760	01
-0.10479700	01	0.59881620	01
-0.11092840	01	0.59578310	01
-0.11660240	01	0.59449910	01
-0.12143720	01	0.59243820	01
-0.12582220	01	0.58990890	01
-0.12978000	01	0.58719200	01
-0.13331820	01	0.58444620	01
-0.13728350	01	0.58047690	01
-0.14040220	01	0.57669180	01
-0.14308610	01	0.57112460	01
-0.14403870	01	0.56980750	01
-0.14586070	01	0.56212080	01
-0.14681330	01	0.55845440	01
-0.14775830	01	0.55141430	01
-0.14785660	01	0.55070630	01
-0.14835940	01	0.54519760	01
-0.14929690	01	0.53853160	01
-0.14937250	01	0.53817730	01
-0.15031750	01	0.53237230	01

SLIGHTLY WORN WHEEL DATA 019

3.0625

0096

1 1

0.2531451E+01	=0.1637387E+02	0.2440929E+01	=0.1640701E+02
0.2357767E+01	=0.1642572E+02	0.2260439E+01	=0.1644249E+02
0.2171022E+01	=0.1644784E+02	0.2090069E+01	=0.1645463E+02
0.1977469E+01	=0.1646223E+02	0.1895964E+01	=0.1646889E+02
0.1814458E+01	=0.1647018E+02	0.1732953E+01	=0.1647195E+02
0.1656166E+01	=0.1647414E+02	0.1606739E+01	=0.1647408E+02
0.1533145E+01	=0.1647979E+02	0.1479973E+01	=0.1648346E+02
0.1413186E+01	=0.1649162E+02	0.1339040E+01	=0.1649154E+02
0.1280165E+01	=0.1649930E+02	0.1177133E+01	=0.1648745E+02
0.1109794E+01	=0.1649132E+02	0.1042456E+01	=0.1649824E+02
0.9583096E+00	=0.1650267E+02	0.8868042E+00	=0.1650468E+02
0.8200176E+00	=0.1650658E+02	0.7532308E+00	=0.1650618E+02
0.6649183E+00	=0.1650491E+02	0.5834128E+00	=0.1650142E+02
0.5171784E+00	=0.1649866E+02	0.4288657E+00	=0.1649519E+02
0.3841572E+00	=0.1649435E+02	0.2879330E+00	=0.1649401E+02
0.2069798E+00	=0.1649018E+02	0.1333858E+00	=0.1648738E+02
0.7395858E-01	=0.1648706E+02	=0.1875162E-03	=0.1648727E+02
=0.5906260E-01	=0.1648502E+02	=0.1179377E+00	=0.1648581E+02
=0.1705577E+00	=0.1648746E+02	=0.2520632E+00	=0.1649298E+02
=0.3262092E+00	=0.1649458E+02	=0.4003553E+00	=0.1649642E+02
=0.4745014E+00	=0.1650150E+02	=0.5344809E+00	=0.1650799E+02
=0.6018198E+00	=0.1651110E+02	=0.6601426E+00	=0.1651662E+02
=0.7133149E+00	=0.1651746E+02	=0.7648306E+00	=0.1652543E+02

-0.8248100E+00 -0.1652832E+02 -0.8915967E+00 -0.1653842E+02
 -0.9594877E+00 -0.1654641E+02 -0.1018915E+01 -0.1655605E+02
 -0.1078894E+01 -0.1656198E+02 -0.1130962E+01 -0.1657462E+02
 -0.1184687E+01 -0.1658725E+02 -0.1244666E+01 -0.1660393E+02
 -0.1297286E+01 -0.1661488E+02 -0.1342547E+01 -0.1662623E+02
 -0.1403079E+01 -0.1664417E+02 -0.1456251E+01 -0.1666380E+02
 -0.1509975E+01 -0.1669279E+02 -0.1549533E+01 -0.1672355E+02
 -0.1581732E+01 -0.1675108E+02 -0.1628649E+01 -0.1679364E+02
 -0.1660847E+01 -0.1682117E+02 -0.1700405E+01 -0.1687081E+02
 -0.1710525E+01 -0.1688895E+02 -0.1728557E+01 -0.1694678E+02
 -0.1739782E+01 -0.1697382E+02 -0.1765173E+01 -0.1704951E+02
 -0.1768486E+01 -0.1707465E+02 -0.1771799E+01 -0.1710065E+02
 -0.1789279E+01 -0.1715367E+02 -0.1815222E+01 -0.1722298E+02
 -0.1818536E+01 -0.1723089E+02 -0.1836567E+01 -0.1729899E+02
 -0.1847240E+01 -0.1732774E+02 -0.1865272E+01 -0.1737617E+02
 -0.1892751E+01 -0.1740830E+02 -0.1915502E+01 -0.1745711E+02
 -0.1940341E+01 -0.1748588E+02 -0.1971987E+01 -0.1751823E+02
 -0.2011545E+01 -0.1755478E+02 -0.2043744E+01 -0.1757856E+02
 -0.2089557E+01 -0.1760946E+02 -0.2128562E+01 -0.1762619E+02
 -0.2189094E+01 -0.1765136E+02 -0.2257537E+01 -0.1766224E+02
 -0.2323219E+01 -0.1767350E+02 -0.2406381E+01 -0.1767132E+02
 -0.2471511E+01 -0.1766782E+02 -0.2529834E+01 -0.1765149E+02
 -0.2587605E+01 -0.1763233E+02 -0.2644824E+01 -0.1760462E+02
 -0.2694131E+01 -0.1757347E+02 -0.2736078E+01 -0.1754230E+02
 -0.2778026E+01 -0.1750694E+02 -0.2819421E+01 -0.1754966E+02

1.5
0068
0 0

0.1506077E+01	0.6557813E+01
0.1500020E+01	0.6578593E+01
0.1490935E+01	0.6634485E+01
0.1488762E+01	0.6656404E+01
0.1486447E+01	0.6678204E+01
0.1473478E+01	0.6731257E+01
0.1464108E+01	0.6761106E+01
0.1454452E+01	0.6797377E+01
0.1448396E+01	0.6820712E+01
0.1442196E+01	0.6836851E+01
0.1426923E+01	0.6861816E+01
0.1367481E+01	0.6870808E+01
0.1313501E+01	0.6879155E+01
0.1260092E+01	0.6887437E+01
0.1209854E+01	0.6896540E+01
0.1163215E+01	0.6901584E+01
0.1102181E+01	0.6907925E+01
0.1041147E+01	0.6914180E+01
0.9909090E+00	0.6921088E+01
0.9193640E+00	0.6930240E+01
0.8669840E+00	0.6936432E+01
0.8223440E+00	0.6939390E+01
0.7719640E+00	0.6943836E+01
0.7217250E+00	0.6946827E+01
0.6497530E+00	0.6952409E+01

0.5923180E+00	0.6954556E+01
0.5309990E+00	0.6958132E+01
0.4951550E+00	0.6958427E+01
0.4446320E+00	0.6961606E+01
0.3907950E+00	0.6963700E+01
0.3332170E+00	0.6966094E+01
0.2683000E+00	0.6968592E+01
0.2000680E+00	0.6970100E+01
0.1423480E+00	0.6971020E+01
0.9182501E-01	0.6971973E+01
0.3079098E-01	0.6975749E+01
-0.2304599E-01	0.6978940E+01
-0.8796400E-01	0.6982699E+01
-0.1418000E+00	0.6984702E+01
-0.2101740E+00	0.6987414E+01
-0.2642960E+00	0.6987439E+01
-0.3256150E+00	0.6984694E+01
-0.3798790E+00	0.6983723E+01
-0.4482530E+00	0.6980797E+01
-0.4881230E+00	0.6980071E+01
-0.5494421E+00	0.6976810E+01
-0.6035639E+00	0.6974906E+01
-0.6794200E+00	0.6970653E+01
-0.7372830E+00	0.6965367E+01
-0.7988872E+00	0.6959202E+01
-0.8603488E+00	0.6951859E+01
-0.9183544E+00	0.6943260E+01
-0.9729039E+00	0.6932135E+01
-0.1023855E+01	0.6920392E+01
-0.1078404E+01	0.6906254E+01
-0.1120498E+01	0.6889937E+01
-0.1184475E+01	0.6867587E+01
-0.1254274E+01	0.6834633E+01
-0.1305795E+01	0.6804682E+01
-0.1339323E+01	0.6778874E+01
-0.1376878E+01	0.6735724E+01
-0.1411546E+01	0.6676659E+01
-0.1427937E+01	0.6630489E+01
-0.1441014E+01	0.6557952E+01
-0.1467418E+01	0.6360455E+01
-0.1477181E+01	0.6268246E+01
-0.1478965E+01	0.6076671E+01
-0.1481389E+01	0.6046499E+01

RAIL CANT FOR RIGHT RAIL .025
 RAIL CANT FOR LEFT RAIL .025
 RAIL GAGE 57.5 (IN)
 WHEEL GAUGE 53.0 (IN)

PRINTER OUTPUT - ASYMMETRIC PROBLEM

THE ASYMMETRIC WHEEL/RAIL CONTACT CHARACTERIZATION PROGRAM

RUN OPTIONS SELECTED

XWIND= 0.0200

ISYM= 0 IPLACT= 1

IPLCT= 1 ICURV= 0

IFLANG = 1

NUMB= 61 IAC= 6

WHEEL GAUGE (IN), RAIL GAUGE (IN), RIGHT RAIL CANT (RAD), LEFT RAIL CANT (RAD).

E3.00000 57.50000 G.02500 C.C2500

RIGHT WHEEL PROFILE INPUT DATA *****

Moderately worn wheel data C20

3.C6250

96

1	C.24261390+01	C.16361335C+C2
2	O.23507960+J1	O.16370520C+C2
3	O.23103790+01	O.16378000C+C2
4	O.22551870+J1	O.16384660C+C2
5	O.21949320+01	O.16392710C+C2
6	O.21312190+01	O.16401570C+C2
7	C.20695170+01	C.16412740C+C2
8	O.20148920+01	C.16413350C+C2
9	C.19619650+01	C.16416890C+C2
10	O.18996970+01	C.16417660C+C2
11	J.18379960+J1	O.16424660C+C2
12	O.17093800+01	O.16432440C+C2
13	O.16249240+01	O.16432010C+C2
14	C.15911910+01	C.16433050C+C2
15	O.15224140+01	C.16430660C+C2
16	C.14689210+01	C.16426690C+C2
17	O.14077860+01	C.16427240C+C2
18	C.13455180+01	C.16425460C+C2
19	O.12925910+01	C.16427650C+C2
20	O.12407400+01	O.16417920C+C2
21	C.11850040+01	C.16413390C+C2
22	O.11244690+J1	O.16408860C+C2
23	C.10404080+01	C.16408480C+C2
24	C.97014110+J1	O.16405670C+C2
25	C.90993010+00	C.16405760C+C2
26	C.85587060+00	C.16401620C+C2
27	C.79972540+00	O.16397100C+C2
28	C.68010000+00	C.16391320C+C2
29	C.61132990+00	O.16386220C+C2
30	C.54255290+00	C.16383420C+C2
31	O.45792590+J1	C.16383340C+C2
32	C.39022470+00	C.16385530C+C2
33	O.32688150+J1	O.16385650C+C2
34	O.25810450+00	C.16382230C+C2
35	O.17347350+J1	O.16382230C+C2
36	C.10470040+00	C.16382130C+C2
37	O.42999150-J1	O.16383260C+C2
38	-C.34102670-J2	C.16383440C+C2
39	-C.10276300+00	C.16382530C+C2
40	-C.16446420+00	C.16380170C+C2
41	-C.21795760+00	C.16381100C+C2
42	-C.27416900+00	O.16385950C+C2
43	-O.33315210+00	C.16380130C+C2
44	-O.42449520+J1	C.16377590C+C2
45	-C.47891420+00	C.16377440C+C2
46	-O.54301540+J1	O.16380260C+C2
47	-O.60286270+00	C.16382640C+C2
48	-C.68695370+00	O.16380710C+C2
49	-C.76392870+00	C.16387170C+C2
50	-O.83383790+00	C.16391900C+C2
51	-C.90314100+00	C.16399950C+C2
52	-O.96544840+00	C.16407730C+C2
53	-O.10277160+J1	O.16417900C+C2
54	-O.10976250+01	C.16425530C+C2
55	-O.11522530+01	J.16424950C+C2
56	-O.12074420+01	C.16452210C+C2
57	-O.12044270+J1	O.16468350C+C2
58	-C.13319770+01	C.16480470C+C2
59	-O.13795260+01	C.16495060C+C2
60	-C.14494350+01	C.16514240C+C2
61	-O.15046270+01	C.16525150C+C2
62	-C.15598180+01	O.16555450C+C2
63	-O.16107080+01	C.16587030C+C2
64	-O.16648240+J1	O.16629380C+C2
65	-C.16993540+01	C.16658510C+C2
66	-O.17398270+J1	O.16709330C+C2
67	-C.17067160+01	C.16741170C+C2
68	-O.17919080+01	O.16781370C+C2
69	-O.18182280+01	C.16820960C+C2
70	-O.18432300+01	C.16820280C+C2
71	-C.18632300+01	C.16905510C+C2
72	-O.18807780+01	C.16945650C+C2
73	-O.19332400+01	O.16995470C+C2
74	-O.19104960+01	C.17025430C+C2
75	-O.19297430+J1	O.17102270C+C2
76	-C.19337050+01	C.17112700C+C2
77	-O.19514190+J1	O.17181420C+C2
78	-C.19626580+01	C.17215670C+C2
79	-C.19733300+01	C.17258680C+C2
80	-C.19849540+01	C.17304520C+C2
81	-O.19954060+01	C.17301290C+C2
82	-C.19980030+01	O.17372670C+C2
83	-C.20169170+01	C.17407600C+C2
84	-O.20355970+J1	O.17476010C+C2
85	-C.20455030+01	C.17505270C+C2
86	-O.20559760+J1	O.17531980C+C2
87	-C.20822980+01	C.17574510C+C2
88	-O.21309790+J1	O.17615850C+C2
89	-O.21467370+01	C.17640060C+C2
90	-O.22490040+01	C.17655830C+C2
91	-C.23118380+01	C.17668740C+C2
92	-O.24041060+01	C.17676790C+C2
93	-O.24887330+01	C.17675430C+C2
94	-O.25727940+01	C.17658010C+C2
95	-O.26310990+J1	O.17645130C+C2
96	-O.26034660+01	C.17652490C+C2

RIGHT RAIL PROFILE INPUT DATA *****

NEW AAR RAIL DATA 025

1.50000

72

0	0	0
1	0.14329410+J1	0.6106113C+01
2	0.14291980+01	C.61597160+C1
3	0.14256830+J1	0.6202402C+C1
4	0.14221670+01	C.6255852C+C1
5	0.14188780+01	0.6299916C+C1
6	0.14115450+01	C.6407996C+C1
7	0.14084830+01	C.6459593C+C1
8	C.14052700+01	0.6502649C+01
9	0.13848190+01	C.6620405C+C1
10	0.13772590+01	0.6648965C+01
11	0.13565820+01	C.672C3300+C1
12	0.13270590+J1	0.6776739C+01
13	0.12887660+01	C.68278590+C1
14	0.1246J5JD+J1	0.6872249C+01
15	0.12031830+01	0.6906820C+01
16	0.11558180+01	C.69354830+C1
17	C.11040300+01	0.6958672C+01
18	0.10392000+01	C.69851670+C1
19	C.97879400+00	C.70C9135C+C1
20	C.93127700+00	C.70256050+C1
21	0.88361JJD+JJ	0.7038C43C+01
22	C.83594200+00	C.70459280+C1
23	0.78385200+JJ	0.7052503C+01
24	C.71872000+00	C.7059757C+C1
25	0.65366300+00	0.7068334C+C1
26	C.59295400+00	C.7075C92C+01
27	0.53644100+00	C.70799550+C1
28	C.44957300+00	0.7083493C+01
29	0.38436600+00	C.70858620+C1
30	0.31915800+00	0.70883990+C1
31	C.24967900+00	C.70912570+C1
32	0.19316600+JJ	0.7093536C+01
33	0.14534700+00	0.70957540+C1
34	C.93256980-01	0.70967250+01
35	0.36668000-01	0.70966410+01
36	-0.3731JJD-01	0.7092516C+01
37	-0.98246010-01	0.70913560+C1
38	-0.15910600+JJ	0.70909650+01
39	-0.21561900+00	C.7093344C+C1
40	-0.27640400+00	C.7093C600+01
41	-0.34176300+00	C.7090148C+C1
42	-0.38096300+00	C.70872740+C1
43	-0.47667600+00	0.7078416C+01
44	-0.51602750+00	C.7077331C+C1
45	-0.57246510+JJ	0.70720110+01
46	-0.62478230+00	C.70704020+C1
47	-0.68571830+00	0.7061516C+01
48	-0.72941680+00	C.70554230+C1
49	-0.78608120+00	0.70413460+01
50	-0.82985530+00	C.7034605C+01
51	-0.89948560+00	0.70233440+C1
52	-0.94745560+00	0.70174310+C1
53	-0.99107850+00	C.70067760+C1
54	-0.10479700+J1	0.6988162C+01
55	-0.11092840+01	C.69678310+C1
56	-0.1166J240+01	0.69445910+C1
57	-0.12143720+01	C.69243820+C1
58	-0.12582220+J1	0.68990890+C1
59	-0.12978000+01	C.68715200+C1
60	-0.13331820+01	C.68444620+C1
61	-0.13728350+01	0.68047690+C1
62	-0.14040220+01	C.67669180+C1
63	-0.14308610+01	0.6711246C+01
64	-0.14403870+01	C.6688C750+C1
65	-0.14586J70+J1	0.66212080+01
66	-0.14681330+01	C.65845440+C1
67	-0.14775830+J1	0.6514143C+01
68	-0.14785660+01	C.6507C630+C1
69	-0.14835940+J1	0.64519760+01
70	-0.14929690+01	0.6385316C+C1
71	-0.14937250+01	C.63817730+C1
72	-0.15031750+01	0.6323723C+C1

LEFT WHEEL PROFILE INPUT DATA *****

SLIGHTLY WORN WHEEL DATA C19
3.C6250

96
TO EQUATE TOP OF WHEEL FLANGES ON LEFT AND RIGHT, LEFT WHEEL ROLLING RACII DATA HAVE BEEN ADJUSTED BY 0.018990 INCH

1 C.25314510+01
2 0.24409290+01
3 0.23577670+01
4 0.22604390+01
5 0.21712220+01
6 C.20900690+01
7 0.19774690+01
8 0.18959640+01
9 0.18144580+01
10 0.17329530+01
11 0.16661660+01
12 C.16067390+01
13 0.15331450+01
14 0.14799730+01
15 0.14131860+01
16 0.13393490+01
17 0.12801650+01
18 0.11771330+01
19 0.11097940+01
20 0.10424560+01
21 C.96830960+00
22 0.88680420+00
23 C.82001760+00
24 0.75223080+00
25 0.66491830+00
26 0.58341280+00
27 0.51717840+00
28 0.42886570+00
29 0.38415720+00
30 C.20793300+00
31 0.20697980+00
32 C.13338580+00
33 0.73358580-01
34 -0.18751620-03
35 -0.59002600-01
36 -0.11793770+00
37 -0.17055770+00
38 -0.25206320+00
39 -0.32620920+00
40 -0.40035530+00
41 -0.47450140+00
42 -0.53448090+00
43 -0.60181980+00
44 -0.66014260+00
45 -0.71331490+00
46 -0.76483060+00
47 -0.82481000+00
48 -0.89159670+00
49 -0.95948770+00
50 -0.10189150+01
51 -0.10788940+01
52 -0.11309620+01
53 -0.11846870+01
54 -0.12446660+01
55 -0.12972860+01
56 -0.13425470+01
57 -0.14030790+01
58 -0.14525100+01
59 -0.15099750+01
60 -0.15495330+01
61 -0.15817320+01
62 -0.16286490+01
63 -0.16608470+01
64 -0.17004050+01
65 -0.17105250+01
66 -0.17285570+01
67 -0.17397820+01
68 -0.17517300+01
69 -0.17684800+01
70 -0.17717980+01
71 -0.17892790+01
72 -0.18152220+01
73 -0.18105360+01
74 -0.18365670+01
75 -0.18472400+01
76 -0.18652720+01
77 -0.18027510+01
78 -0.19155320+01
79 -0.19403410+01
80 -0.19719870+01
81 -0.20115450+01
82 -0.20337440+01
83 -0.20895570+01
84 -0.21245620+01
85 -0.21890940+01
86 -0.22575370+01
87 -0.23232190+01
88 -0.24063810+01
89 -0.24715110+01
90 -0.25298340+01
91 -0.25876350+01
92 -0.26448200+01
93 -0.26941310+01
94 -0.27360780+01
95 -0.27780260+01
96 -0.28194210+01

C.16352860+C2
C.16422000+C2
C.16444710+C2
C.16461480+C2
C.16466830+C2
C.16473620+C2
C.16481220+C2
C.16487880+C2
C.16485170+C2
C.16490940+C2
C.16493130+C2
C.16493070+C2
C.16498780+C2
C.16502650+C2
C.16510610+C2
C.16510530+C2
C.16510530+C2
C.16506440+C2
C.16510310+C2
C.16511230+C2
C.16521660+C2
C.16523670+C2
C.16525570+C2
C.16525170+C2
C.16523900+C2
C.16520410+C2
C.16517650+C2
C.16514180+C2
C.16513340+C2
C.16513000+C2
C.16505170+C2
C.16506370+C2
C.16506050+C2
C.16506260+C2
C.16504010+C2
C.16504800+C2
C.16506450+C2
C.16511970+C2
C.16515540+C2
C.16520490+C2
C.16524980+C2
C.16530090+C2
C.16535610+C2
C.16536450+C2
C.16544420+C2
C.16547310+C2
C.16547710+C2
C.16565400+C2
C.16575040+C2
C.16580970+C2
C.16593610+C2
C.16606240+C2
C.16622920+C2
C.16633870+C2
C.16645220+C2
C.16663160+C2
C.16682750+C2
C.16711780+C2
C.16742540+C2
C.16770070+C2
C.16812630+C2
C.16840160+C2
C.16885800+C2
C.16907940+C2
C.16965770+C2
C.16992810+C2
C.17066500+C2
C.17093640+C2
C.17115860+C2
C.17172660+C2
C.17241970+C2
C.17245880+C2
C.17317980+C2
C.17346730+C2
C.17395160+C2
C.17427250+C2
C.17476100+C2
C.17504870+C2
C.17537220+C2
C.17573770+C2
C.17597550+C2
C.17628450+C2
C.17645180+C2
C.17670350+C2
C.17681230+C2
C.17692490+C2
C.17696310+C2
C.17686810+C2
C.17670480+C2
C.17651320+C2
C.17623610+C2
C.17592460+C2
C.17561290+C2
C.17525930+C2
C.17568650+C2

LEFT RAIL PROFILE INPUT DATA *****

WORN LEFT RAIL DATA 013
1.5000C

68

	0	0
1	C.15060770+01	C.65578130+C1
2	C.15000200+01	C.65785930+C1
3	O.14909350+01	C.66344850+C1
4	C.14887620+01	O.66564040+C1
5	O.14884470+01	C.66782040+C1
6	O.14734780+01	O.67312570+C1
7	O.14641080+01	C.67611060+C1
8	O.14544520+01	O.67973770+C1
9	O.14483960+01	C.68207120+C1
10	O.14421960+01	O.68368510+C1
11	C.14069230+01	C.68618160+C1
12	O.13874810+01	C.68708080+C1
13	C.13135010+01	O.68791550+C1
14	O.12600920+01	C.68874370+C1
15	O.12098540+01	C.68965400+C1
16	O.11632150+01	C.69015840+C1
17	O.11021810+01	O.69075250+C1
18	C.10411470+01	C.69141800+C1
19	O.99090900+00	O.69210880+C1
20	C.91936400+00	C.69302400+C1
21	C.86898400+00	C.69364320+C1
22	C.82234400+00	C.69393900+C1
23	O.77196400+00	C.69438360+C1
24	C.72172500+00	O.69468270+C1
25	C.64975300+00	C.69524090+C1
26	O.59231800+00	O.69545560+C1
27	C.53099900+00	C.69581320+C1
28	O.49515500+00	O.69584270+C1
29	C.44463200+00	C.69561600+C1
30	O.39079500+00	O.69637000+C1
31	C.33321700+00	C.69660940+C1
32	O.26830000+00	C.69685920+C1
33	C.20006800+00	O.69701000+C1
34	O.14234800+00	C.69710200+C1
35	O.91825010-01	O.69719730+C1
36	C.30790580-01	C.69757490+C1
37	-O.23045990-01	O.69789400+C1
38	-O.87964000-01	C.69826990+C1
39	-O.14180000+00	O.69847020+C1
40	-C.21017400+00	C.69874140+C1
41	-O.26429600+00	O.69874390+C1
42	-O.32561500+00	C.69846940+C1
43	-O.37987900+00	O.69837230+C1
44	-C.44825300+00	C.69807970+C1
45	-O.48812300+00	C.69800710+C1
46	-C.54944210+00	C.69768100+C1
47	-O.60356390+00	C.69745060+C1
48	-O.67942000+00	O.69706530+C1
49	-O.73728300+00	C.69653670+C1
50	-O.79888720+00	O.69592020+C1
51	-C.86034880+00	C.69518590+C1
52	-O.91835440+00	O.69432600+C1
53	-C.97290390+00	C.69321350+C1
54	-O.10238550+01	C.69203920+C1
55	-C.10784040+01	C.69062540+C1
56	-O.11294980+01	C.68895370+C1
57	-O.11844750+01	O.68867580+C1
58	-O.12542740+01	O.68346330+C1
59	-O.13057950+01	O.68046820+C1
60	-C.13393230+01	C.67788740+C1
61	-O.13768780+01	O.67357240+C1
62	-C.14115460+01	C.66766590+C1
63	-O.14279370+01	O.66304890+C1
64	-C.14410140+01	C.65579520+C1
65	-O.14674180+01	C.62604550+C1
66	-O.14771810+01	O.62682460+C1
67	-O.14789650+01	C.60766710+C1
68	-O.14813890+01	C.60464990+C1

RAIL CANT FOR LEFT RAIL .C25
RAIL CANT FOR RIGHT RAIL .J25
RAIL GAGE 57.5 (IN)
WHEEL GAUGE 53.0 (IN)

C.740	1.0165	J.1996	-0.5435	-0.5016	16.43279	7.09421	16.52666	6.57523	-0.015165	0.062993	0.060847	0.060388
C.760	1.0205	J.1891	-0.5435	-0.4813	16.43279	7.09459	16.52669	6.98001	-0.013042	0.062993	0.060848	0.060388
C.780	1.0405	J.1891	-0.7635	-0.6811	16.43314	7.09460	16.54261	6.97030	-0.008108	0.094884	0.060851	0.060178
C.800	1.0605	J.1765	-0.8235	-0.7205	16.43321	7.09494	16.54882	6.96718	-0.005265	0.110977	0.060852	0.060056
C.820	1.0805	J.1679	-0.8835	-0.7595	16.43325	7.09525	16.55554	6.96354	-0.002152	0.124676	0.060852	0.059932
C.840	1.0705	J.1572	-0.8835	-0.7392	16.43325	7.09551	16.55554	6.96552	0.001247	0.124676	0.060852	0.059932
C.860	1.0805	J.1465	-0.8835	-0.7185	16.43322	7.09574	16.55554	6.96735	0.004947	0.124676	0.060852	0.059932
C.880	1.0905	J.1357	-1.1235	-0.9377	16.43315	7.09592	16.59259	6.95555	0.008964	0.264081	0.060850	0.059017
C.900	1.0905	J.1144	-1.1835	-0.9764	16.43315	7.09614	16.60577	6.93172	0.008964	0.227917	0.060850	0.058663
C.920	1.0905	J.0922	-1.2535	-1.0241	16.43315	7.09618	16.62431	6.92187	0.008964	0.193715	0.060850	0.059028
C.940	1.0905	J.0707	-1.2535	-1.0027	16.43315	7.09605	16.62431	6.92559	0.008964	0.193715	0.060850	0.059028
C.960	1.0905	J.0447	-1.2535	-1.3065	16.43315	7.09567	16.71226	6.88724	0.008964	0.675385	0.060850	0.063386
C.980	1.0905	J.0184	-1.2135	-1.3111	16.43315	7.09510	16.75569	6.80448	0.008964	0.694370	0.060850	0.065753
1.00J	1.0905	J.0099	-1.6635	-1.3315	16.43315	7.09431	16.84331	6.78522	0.008964	0.854983	0.060850	0.038961
1.02C	1.0905	J.0146	-1.8335	-1.3600	16.43315	7.09283	17.30333	6.77279	0.008964	1.245794	0.060850	0.038454
1.040	1.0905	J.2177	-1.9435	-1.3558	16.43315	7.09268	17.56824	6.76573	0.008964	0.858931	0.060850	0.037311
1.06C	1.0905	J.2517	-1.9135	-1.3319	16.43315	7.09224	17.47900	6.78526	0.008964	0.918055	0.060850	0.034748
1.08J	1.7205	J.2456	-2.2035	-1.3588	16.43393	7.09234	17.56806	6.76878	0.054594	0.704144	0.060770	0.043384
1.10C	1.7405	J.2803	-1.6735	-1.3321	16.42859	7.09207	17.54049	6.78519	0.058637	0.782018	0.060760	0.040449
1.120	1.7605	J.2684	-1.9935	-1.3235	16.42879	7.09190	17.55534	6.75310	0.061410	0.730082	0.060755	0.042434
1.14C	1.7865	J.2758	-2.0135	-1.3158	16.42734	7.09172	17.57633	6.75719	0.063056	0.678325	0.060753	0.044259
1.160	1.8165	J.2723	-2.0235	-1.2550	16.42543	7.09181	17.54418	6.78520	J.063986	0.652709	0.060757	0.045175
1.18C	1.8465	J.2684	-2.0435	-1.2928	16.42351	7.09196	17.52665	6.81715	0.063454	0.607325	0.060766	0.046823
1.200	1.8765	J.2634	-2.0635	-1.2872	16.42162	7.09201	17.61175	6.82084	0.062112	0.555471	0.060778	0.048333

(RL-RR)/2A = NORMALIZED DIFFERENCE IN ROLLING RADII (IN/IN)
 (ML-MR)/2 = NORMALIZED DIFFERENCE IN CONTACT ANGLE (RAD)
 WR = WHEELSET ROLL ANGLE W.R.T. HORIZONTAL, POSITIVE UP ON LEFT (RAD)
 YCC = VERTICAL DISPLACEMENT OF WHEELSET CENTROID FROM NOMINAL PCS. (IN)
 CWR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CML = PRINCIPAL TRANSVERSE CURVATURE OF LEFT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)

Δh (IN)	(RL-RR)/2A (IN/IN)	(ML-MR)/2 (RAD)	WR (RAD)	YCC (IN)	CWR (1/IN)	CYR (1/IN)	CML (1/IN)	CYL (1/IN)
-1.200	-0.018648	-0.310151	-0.016420	0.441802	7.669333	3.908910	0.095868	0.147355
-1.180	-0.018142	-0.418128	-0.015904	0.428021	3.575986	3.906563	0.092457	0.142524
-1.160	-0.018478	-0.351010	-0.015329	0.412069	6.089517	2.816145	0.089642	0.137054
-1.140	-0.018303	-0.388601	-0.014812	0.357875	4.704428	2.171300	0.085622	0.132214
-1.120	-0.014149	-0.645066	-0.013864	0.285079	0.080805	2.819222	0.075341	0.117324
-1.100	-0.009892	-0.600078	-0.013050	0.071570	-0.434157	0.565455	0.020180	0.214783
-1.080	-0.005397	-0.484279	-0.012311	0.011870	-0.938502	1.668832	0.020180	0.183667
-1.060	-0.004354	-0.460006	-0.011589	-0.015839	-1.259093	1.750292	0.016723	0.176398
-1.040	0.002059	-0.293306	-0.010666	-0.023007	0.032306	0.051549	0.013266	0.171846
-1.020	0.002065	0.527268	-0.009076	-0.000076	0.000076	0.090499	0.011537	0.166175
-1.000	0.002069	J.024757	-0.008090	-0.021891	0.044501	0.090465	0.012393	0.160518
-0.980	0.002074	J.022646	-0.007101	-0.021408	0.052566	0.089017	0.014554	0.154862
-0.960	J.002078	J.021112	-0.006111	-0.020567	0.054993	0.088972	0.016715	0.149128
-0.940	0.002081	J.017619	-0.005120	-0.020582	0.044280	0.088952	0.018877	0.143453
-0.920	J.002086	J.015523	-0.004125	-0.020249	0.044968	0.087508	0.021038	0.137679
-0.900	0.002084	J.013203	-0.003136	-0.019962	0.038343	0.087492	0.023200	0.132249
-0.880	0.002092	J.011002	-0.002143	-0.019725	0.031715	0.087479	0.025361	0.126640
-0.860	J.002095	J.008977	-0.001149	-0.019534	0.025095	0.087467	0.027523	0.121040
-0.840	0.002100	J.006958	-0.000154	-0.019388	0.018470	0.087458	0.031847	0.121004
-0.820	0.002102	J.004939	-0.000158	-0.019275	0.011844	0.087462	0.034010	0.115443
-0.800	0.002090	J.002920	-0.000156	-0.019057	-0.011346	0.087495	0.036172	0.109942
-0.780	J.002089	J.000901	0.000153	-0.018860	-0.014653	0.087482	0.038335	0.104427
-0.760	0.002085	J.000926	0.000145	-0.018699	-0.021277	0.087493	0.039319	0.104488
-0.740	J.002082	J.000865	0.000144	-0.018563	-0.024599	0.087480	0.044826	0.104488
-0.720	0.002078	J.000873	0.000139	-0.018425	-0.031214	0.087498	0.046826	0.098353
-0.700	J.002074	J.000871	0.000146	-0.018274	-0.037838	0.087457	0.051757	0.219919

PROFILE PRINCIPAL TRANSVERSE CURVATURES (1/IN)

XWR= LOCATION ON RIGHT WHEEL, POSITIVE CUT FROM TAPELINE (IN)
 XRR= LOCATION ON RIGHT RAIL, POSITIVE CUT FROM CENTERLINE (IN)
 XWL= LOCATION ON LEFT WHEEL, POSITIVE OUT FROM CENTERLINE (IN)
 XRL= LOCATION ON LEFT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 CWR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CWL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)

XWR (IN)	CWR (1/IN)	XRR (IN)	CYR (1/IN)	XWL (IN)	CWL (1/IN)	XRL (IN)	CYL (1/IN)
-2.68346	-4.916701	-1.45861	C.743191	-2.32322	5.666380	-1.41155	1.444368
-2.65000	-6.002773	-1.45000	C.855714	-2.30000	5.278864	-1.40000	1.630697
-2.60000	-5.373230	-1.40000	L.966661	-2.25000	3.776591	-1.35000	2.537836
-2.55000	-2.948425	-1.35000	3.552658	-2.20000	2.265416	-1.30000	3.112927
-2.50000	-J.452113	-1.30000	3.326706	-2.15000	0.178332	-1.25000	2.585058
-2.40000	4.394793	-1.20000	C.664651	-2.05000	-0.703257	-1.15000	C.983376
-2.35000	1.102941	-1.15000	C.792467	-2.00000	3.400762	-1.10000	C.452925
-2.30000	-1.757321	-1.10000	C.524600	-1.95000	4.192184	-1.05000	0.571573
-2.25000	-4.701198	-1.05000	L.089575	-1.90000	2.097722	-1.00000	0.698856
-2.20000	5.136013	-1.00000	C.917455	-1.85000	0.515306	-0.95000	C.833884
-2.15000	11.069228	-0.95000	C.701745	-1.80000	0.034678	-0.90000	0.834370
-2.10000	4.232259	-0.90000	C.467058	-1.75000	-0.359781	-0.85000	0.656146
-2.05000	0.767846	-0.85000	C.221990	-1.70000	-1.043544	-0.80000	0.466473
-2.00000	0.14022	-0.80000	C.138205	-1.65000	-2.033803	-0.75000	0.270460
-1.95000	-J.203125	-0.75000	0.165548	-1.60000	-3.554763	-0.70000	0.260842
-1.90000	-0.489008	-0.70000	C.153954	-1.55000	-4.596130	-0.65000	C.255310
-1.85000	-J.754823	-0.65000	0.222238	-1.50000	-3.660505	-0.60000	0.249592
-1.80000	-1.122113	-0.60000	C.250791	-1.45000	-1.249804	-0.55000	C.243707
-1.75000	-1.503463	-0.55000	C.459587	-1.40000	0.193702	-0.50000	0.237471
-1.70000	-1.787231	-0.50000	C.308974	-1.35000	0.932218	-0.45000	0.225214
-1.65000	-1.749000	-0.45000	C.303465	-1.30000	0.596050	-0.40000	0.218825
-1.60000	-1.674478	-0.40000	C.268655	-1.25000	0.280208	-0.35000	C.199573
-1.55000	-1.574612	-0.35000	C.232257	-1.20000	-0.024724	-0.30000	0.171920
-1.50000	-1.431803	-0.30000	C.156159	-1.15000	-0.330652	-0.25000	C.144140
-1.45000	-0.957592	-0.25000	C.155578	-1.10000	-0.649277	-0.20000	0.116362
-1.40000	-J.357152	-0.20000	C.123664	-1.05000	-0.193702	-0.15000	0.078601
-1.35000	-1.180804	-0.15000	C.687901	-1.00000	-0.667054	-0.10000	0.060863
-1.30000	-J.223831	-0.10000	C.650516	-0.95000	-0.579438	-0.05000	C.053345
-1.25000	-0.267867	-0.05000	C.056537	-0.90000	-0.486795	0.00000	0.005440
-1.20000	-J.313314	C.00000	0.063884	-0.85000	-0.390814	0.05000	-0.008961
-1.15000	-0.359318	C.05000	C.070830	-0.80000	-0.292766	C.10000	-0.002040
-1.10000	-0.406753	0.10000	C.077572	-0.75000	-0.193702	C.15000	0.001882
-1.05000	-0.391463	0.15000	C.085110	-0.70000	-0.093388	C.20000	0.001864
-1.00000	-0.373964	0.20000	C.092241	-0.65000	0.006410	0.25000	0.018724
-0.95000	-0.351550	0.25000	C.099361	-0.60000	0.101555	C.30000	C.025642
-0.90000	-0.330367	0.30000	C.106466	-0.55000	0.066112	C.35000	C.032557
-0.85000	-0.308549	0.35000	0.137055	-0.50000	-0.030725	C.40000	C.039466
-0.80000	-0.286219	0.40000	C.182143	-0.45000	-0.004625	0.45000	0.047996
-0.75000	-J.263487	0.45000	0.227643	-0.40000	-0.035933	0.50000	0.064990
-0.70000	-0.240949	0.50000	C.271630	-0.35000	-0.075339	0.55000	0.091952
-0.65000	-0.217171	0.55000	0.315732	-0.30000	-0.110841	0.60000	C.113865
-0.60000	-0.193439	0.60000	0.359116	-0.25000	-0.146387	0.65000	C.135707
-0.55000	-0.168448	0.65000	0.401486	-0.20000	-0.182015	0.70000	0.157452
-0.50000	-0.143184	0.70000	C.442484	-0.15000	-0.217717	0.75000	0.176065
-0.45000	-0.117881	0.75000	C.481663	-0.10000	-0.231431	0.80000	0.200504
-0.40000	-0.092559	0.80000	C.521860	-0.05000	-0.253720	0.85000	0.221716
-0.35000	-0.067332	0.85000	C.562100	0.00000	-0.179954	0.90000	0.242474
-0.30000	-0.041997	0.90000	C.583447	0.05000	-0.154094	C.95000	0.263211
-0.25000	-0.016584	0.95000	C.610264	0.10000	-0.128254	1.00000	0.283341
-0.20000	J.008737	1.00000	0.632627	0.15000	-0.102422	1.041155	C.299513
-0.15000	0.034059	1.03920	C.646735	0.20000	-0.076616	0.0	0.0
-0.10000	J.057369	0.0	0.0	0.25000	-0.050822	0.0	0.0
-0.05000	0.040510	0.0	0.0	0.30000	-0.025054	0.0	0.0
0.00000	0.023949	0.0	0.0	0.35000	0.000792	0.0	0.0
0.05000	0.007347	0.0	0.0	0.40000	0.021658	0.0	0.0
0.10000	-0.009174	0.0	0.0	0.45000	0.032248	0.0	0.0
0.15000	-0.025736	0.0	0.0	0.50000	0.042846	0.0	0.0
0.20000	-0.042296	0.0	0.0	0.55000	0.053449	0.0	0.0
0.25000	-0.058855	0.0	0.0	0.60000	0.064058	0.0	0.0
0.30000	-0.075409	0.0	0.0	0.65000	0.074674	0.0	0.0
0.35000	-J.091955	0.0	0.0	0.70000	0.085293	0.0	0.0
0.40000	-J.108473	0.0	0.0	0.75000	0.095918	0.0	0.0
0.45000	-J.124927	0.0	0.0	0.80000	0.106537	0.0	0.0
0.50000	-0.091741	0.0	0.0	0.85000	0.117155	0.0	0.0
0.55000	-J.084279	0.0	0.0	0.90000	0.122102	0.0	0.0
0.60000	-0.070821	0.0	0.0	0.95000	0.111266	0.0	0.0
0.65000	-0.069370	0.0	0.0	1.00000	0.100418	0.0	0.0
0.70000	-0.061425	0.0	0.0	1.05000	0.089577	0.0	0.0
0.75000	-0.054488	0.0	0.0	1.10000	0.078731	0.0	0.0
0.80000	-0.047195	0.0	0.0	1.15000	0.071894	0.0	0.0
0.85000	-0.039636	0.0	0.0	1.20000	0.057064	0.0	0.0
0.90000	-J.032219	0.0	0.0	1.25000	0.046241	0.0	0.0
0.95000	-0.012659	0.0	0.0	1.30000	0.035424	0.0	0.0
1.00000	J.009916	0.0	0.0	1.35000	0.024613	0.0	0.0
1.05000	0.032477	0.0	0.0	1.40000	0.013807	0.0	0.0
1.10000	0.055365	0.0	0.0	1.45000	0.013321	0.0	0.0
1.15000	-0.077691	0.0	0.0	1.50000	0.025325	0.0	0.0
1.20000	0.100332	0.0	0.0	1.55000	0.034558	0.0	0.0
1.25000	0.123019	0.0	0.0	1.60000	0.043230	0.0	0.0
1.30000	0.145740	0.0	0.0	1.65000	0.051853	0.0	0.0
1.35000	0.168484	0.0	0.0	1.70000	0.060466	0.0	0.0
1.40000	0.191233	0.0	0.0	1.75000	0.069066	0.0	0.0
1.45000	J.179346	0.0	0.0	1.80000	0.077655	0.0	0.0
1.50000	0.160371	0.0	0.0	1.85000	0.086244	0.0	0.0
1.55000	J.141669	0.0	0.0	1.90000	0.094833	0.0	0.0
1.60000	0.122957	0.0	0.0	1.95000	0.103422	0.0	0.0
1.65000	0.104249	0.0	0.0	2.00000	0.112011	0.0	0.0
1.70000	0.085552	0.0	0.0	2.05000	0.120600	0.0	0.0
1.75000	0.066870	0.0	0.0	2.09900	0.128888	0.0	0.0
1.80000	0.048203	0.0	0.0	0.0	0.0	0.0	0.0
1.85000	0.029549	0.0	0.0	0.0	0.0	0.0	0.0
1.90000	J.010903	0.0	0.0	0.0	0.0	0.0	0.0
1.95000	-0.007739	0.0	0.0	0.0	0.0	0.0	0.0
2.00000	-J.026383	0.0	0.0	0.0	0.0	0.0	0.0
2.01489	-0.031937	C.C	C.O	0.0	0.0	0.0	0.0

CALCOMP PLOTTER OUTPUT - ASYMMETRIC PROBLEM

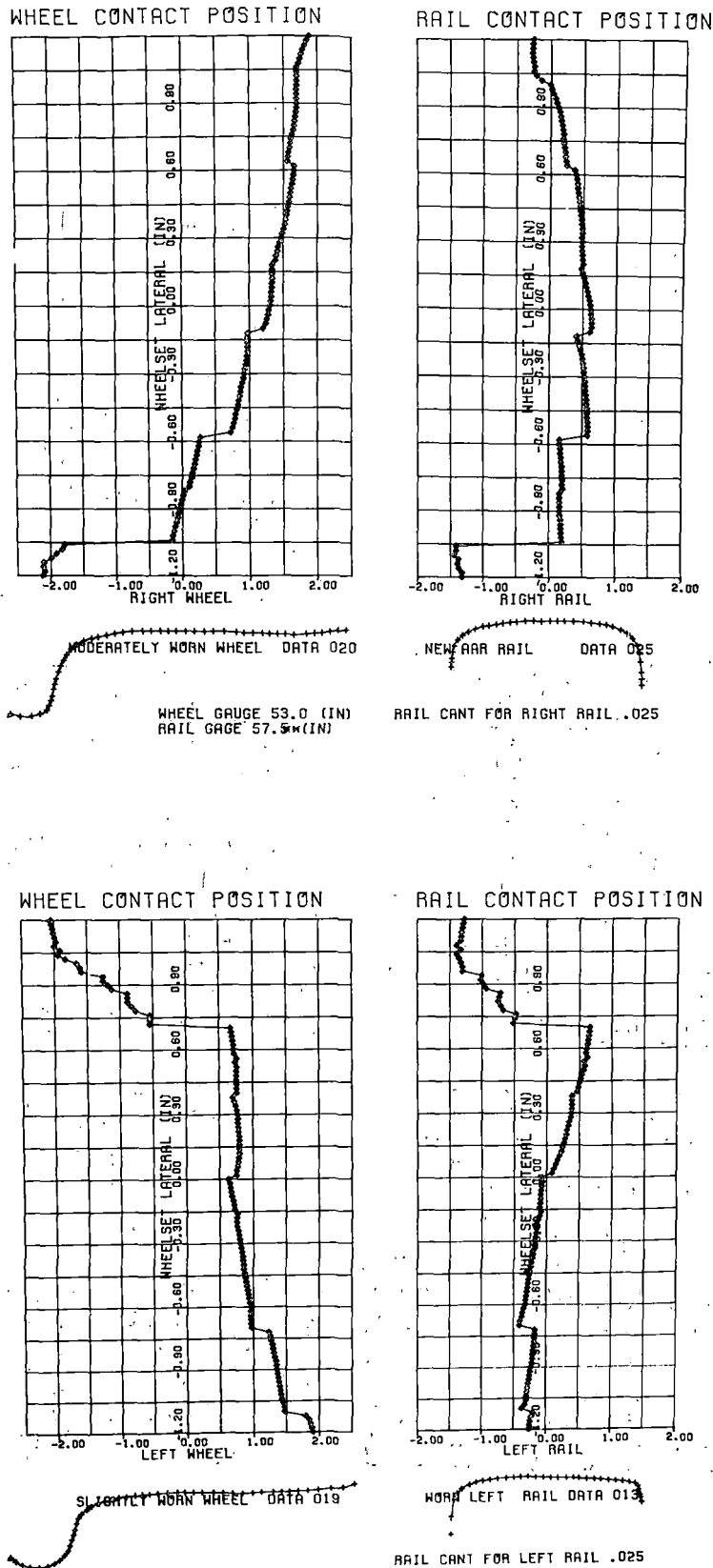
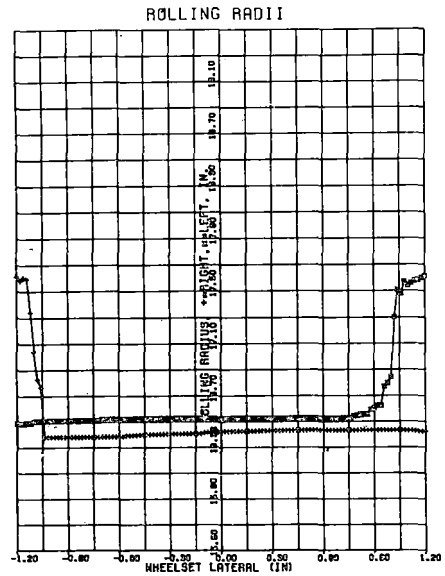
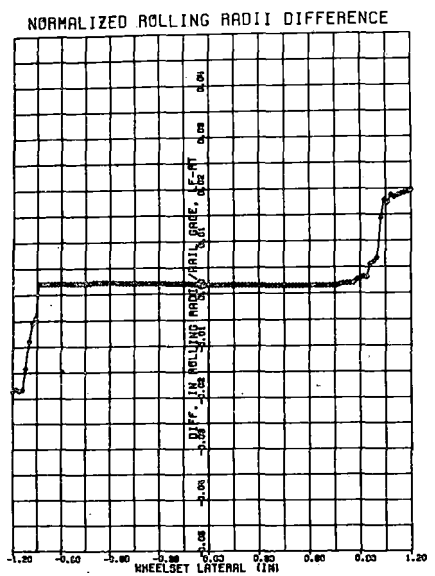


FIGURE 4A. CALCOMP PLOTTER OUTPUT - ASYMMETRIC PROBLEM, WHEEL/RAIL PROFILES AND LOCATION OF CONTACT POINTS.



RIGHT SIDE

MODERATELY WORN WHEEL DATA 020
 NEW RAR RAIL DATA 025
 RAIL CANT FOR RIGHT RAIL .025

LEFT SIDE

SLIGHTLY WORN WHEEL DATA 019
 WORN LEFT RAIL DATA 013
 RAIL CANT FOR LEFT RAIL .025

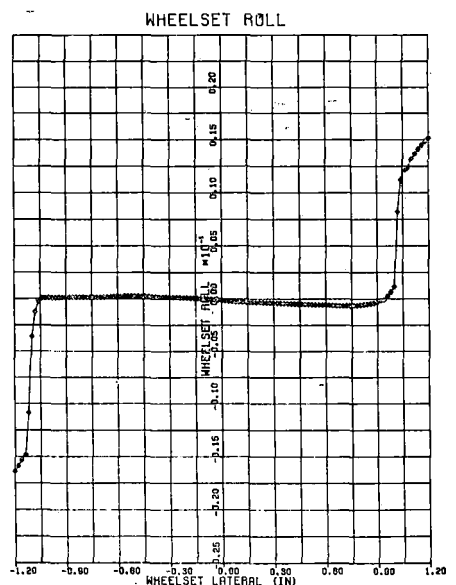
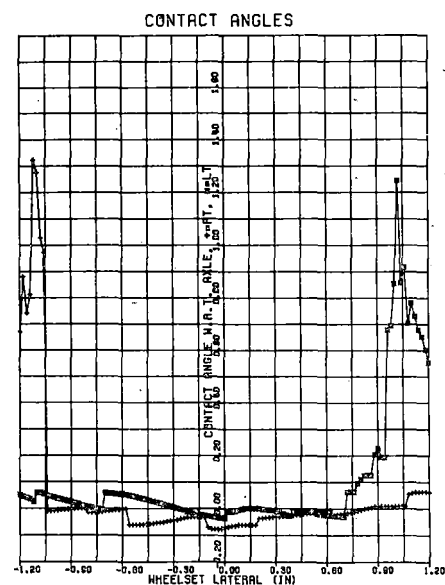
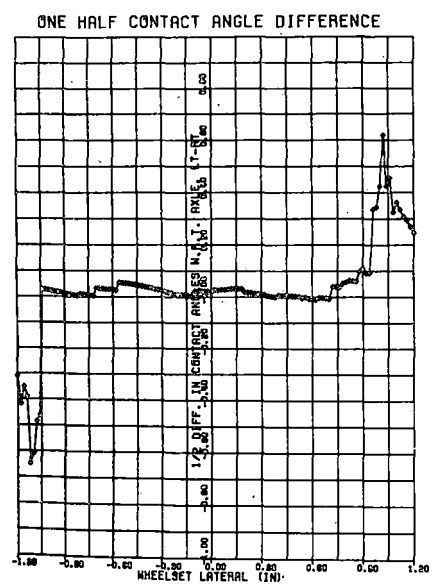


FIGURE 4B. CALCOMP PLOTTER OUTPUT - ASYMMETRIC PROBLEM, GEOMETRIC CONSTRAINTS.

PARTIAL LISTING OF PUNCHED CARD OUTPUT - ASYMMETRIC PROBLEM

0.530000D+02 0.295630D+02 0.575000D+02 0.302500D+02 0.250000D-01 0.250000D-01

COEFFICIENTS FOR PROFILE CURVE FITS

MODERATELY WORN WHEEL DATA 020

16

1-0.1567150+01 0.3046710D+02-0.1914860D+02 0.5300640D+01-0.5476390D+00
 0.2000000D+03 0.2131220D+01
 2 0.4614050+01 0.2532350D+02-0.2024060D+02 0.7163360D+01-0.9494600D+00
 0.2131220D+01 0.1706390D+01
 3 0.1325180D+02 0.8410710D+01-0.8434090D+01 0.3785320D+01-0.6393210D+00
 0.1706390D+01 0.1345520D+01
 4 0.1472030D+02 0.6319830D+01-0.8817440D+01 0.5402190D+01-0.1218670D+01
 0.1345520D+01 0.9781410D+00
 5 0.1645330D+02-0.3766790D+00 0.6402810D+00-0.3569710D+00 0.4796030D-01
 0.9781410D+00 0.5425530D+00
 6 0.1638200D+02 0.5211540D-02 0.1045730D+00-0.4354210D+00 0.4396860D+00
 0.5425530D+00 0.1047000D+00
 7 0.1638260D+02 0.1255620D-03-0.1611280D-01 0.1362370D+00 0.2605590D+00
 0.1047000D+00-0.2720170D+00
 8 0.1638300D+02 0.2021760D-01 0.1438990D-01 0.6627310D-03 0.3380390D-01
 -0.2720170D+00-0.6869440D+00
 9 0.1614670D+02-0.1217650D+01-0.2327960D+01-0.1905850D+01-0.5292470D+00
 -0.6869440D+00-0.1097630D+01
 10 0.1898160D+02 0.8932110D+01 0.1130060D+02 0.6231240D+01 0.1293940D+01
 -0.1097630D+01-0.1449440D+01
 11-0.7741510D+01-0.5909980D+02-0.5316820D+02-0.2070120D+02-0.2887360D+01
 -0.1449440D+01-0.1739830D+01
 12 0.1356100D+04 0.3025830D+04 0.2562340D+04 0.9644170D+03 0.1361910D+03
 -0.1739830D+01-0.1880780D+01
 13 0.8426730D+04 0.1741600D+05 0.1352510D+05 0.4669060D+04 0.6046630D+03
 -0.1880780D+01-0.1962860D+01
 14 0.2300530D+05 0.4557840D+05 0.3386470D+05 0.1117580D+05 0.1382270D+04
 -0.1962860D+01-0.2035600D+01
 15-0.8339370D+03-0.1475080D+04-0.9579250D+03-0.2763910D+03-0.2989260D+02
 -0.2035600D+01-0.2249000D+01
 16 0.4659080D+03 0.7679960D+03 0.4916130D+03 0.1393620D+03 0.1476350D+02
 -0.2249000D+01-0.2683460D+01

NEW AAR RAIL DATA 025

12

1-0.7179740D+06 0.2023150D+07-0.2137740D+07 0.1003870D+07-0.1767740D+06
 0.2000000D+03 0.1411550D+01
 2-0.4713270D+04 0.1467010D+05-0.1708560D+05 0.8838250D+04-0.1713550D+04
 0.1411550D+01 0.1327060D+01
 3-0.1727650D+02 0.9303840D+02-0.1324270D+03 0.8329030D+02-0.1962230D+02
 0.1327060D+01 0.1039200D+01
 4 0.7832700D+01-0.3683280D+01 0.6619600D+01-0.5151990D+01 0.1384700D+01
 0.1039200D+01 0.7187200D+00
 5 0.7117870D+01-0.2373390D+00 0.7596440D+00-0.1112080D+01 0.5018010D+00
 0.7187200D+00 0.3191580D+00

6 0.709460D+01 0.287286D-01-0.803595D-01-0.595744D+00 0.114622D+01
 0.319158D+00-0.373100D-01
 7 0.709319D+01 0.215640D-01 0.235734D+00 0.808897D+00 0.608104D+00
 -0.373100D-01-0.380963D+00
 8 0.718524D+01 0.674892D+00 0.176116D+01 0.207601D+01 0.809856D+00
 -0.380963D+00-0.729417D+00
 9 0.757947D+01 0.186464D+01 0.248642D+01 0.142973D+01 0.230883D+00
 -0.729417D+00-0.104797D+01
 10 -0.925237D+01-0.590273D+02-0.796795D+02-0.475942D+02-0.106845D+02
 -0.104797D+01-0.133318D+01
 11 -0.217416D+04-0.650945D+04-0.728106D+04-0.361792D+04-0.673933D+03
 -0.133318D+01-0.146813D+01
 12 0.312714D+06 0.852386D+06 0.871187D+06 0.395682D+06 0.673831D+05
 -0.146813D+01-0.150317D+01

SLIGHTLY WORN WHEEL DATA 019

16

1 0.128266D+01 0.297367D+02-0.217413D+02 0.705471D+01-0.859258D+00
 0.200000D+03 0.209007D+01
 2 0.224666D+02-0.128168D+02 0.102578D+02-0.362104D+01 0.474031D+00
 0.209007D+01 0.160674D+01
 3 0.200192D+02-0.105257D+02 0.117192D+02-0.573018D+01 0.103558D+01
 0.160674D+01 0.117713D+01
 4 0.166938D+02-0.106922D+01 0.226674D+01-0.196264D+01 0.590000D+00
 0.117713D+01 0.753231D+00
 5 0.165013D+02 0.707760D-01-0.228450D+00 0.434430D+00-0.264626D+00
 0.753231D+00 0.287933D+00
 6 0.165047D+02 0.523937D-02 0.113306D+00-0.617850D-01-0.267297D+00
 0.287933D+00-0.117938D+00
 7 0.165054D+02 0.134114D-01 0.132511D+00 0.545437D-01-0.236652D-01
 -0.117938D+00-0.534481D+00
 8 0.163438D+02-0.949982D+00-0.192276D+01-0.177162D+01-0.571225D+00
 -0.534481D+00-0.891597D+00
 9 0.160470D+02-0.194034D+01-0.292016D+01-0.196159D+01-0.458314D+00
 -0.891597D+00-0.124467D+01
 10 0.206284D+01-0.402814D+02-0.413435D+02-0.185038D+02-0.300320D+01
 -0.124467D+01-0.154953D+01
 11 0.686777D+03 0.171190D+04 0.163843D+04 0.696507D+03 0.111018D+03
 -0.154953D+01-0.172856D+01
 12 0.114368D+05 0.256190D+05 0.215434D+05 0.804836D+04 0.112723D+04
 -0.172856D+01-0.181522D+01
 13 0.436321D+04 0.926468D+04 0.739158D+04 0.261622D+04 0.346694D+03
 -0.181522D+01-0.191550D+01
 14 -0.814421D+02-0.171680D+03-0.112573D+03-0.331004D+02-0.367898D+01
 -0.191550D+01-0.212856D+01
 15 -0.419957D+02-0.975061D+02-0.603910D+02-0.168212D+02-0.177863D+01
 -0.212856D+01-0.252983D+01
 16 0.231189D+04 0.356985D+04 0.208054D+04 0.538212D+03 0.521373D+02
 -0.252983D+01-0.281942D+01

WORN LEFT RAIL DATA 013

11

1 0.400507D+06-0.108454D+07 0.110124D+07-0.496933D+06 0.840817D+05
 0.200000D+03 0.147348D+01

2-0.9116840+03 0.2810610+04-0.3220800+04 0.1638360+04-0.3121620+03
 0.1473480+01 0.1367480+01
 3 0.2913670+01 0.1537210+02-0.2163390+02 0.1332010+02-0.3051660+01
 0.1367480+01 0.1041150+01
 4 0.7218940+01-0.1336090+01 0.2578770+01-0.2218470+01 0.6768870+00
 0.1041150+01 0.7217250+00
 5 0.6966570+01 0.7017330-01-0.3460950+00 0.4794100+00-0.2570140+00
 0.7217250+00 0.3907950+00
 6 0.6977340+01-0.5171950-01 0.4893040-01 0.1467710+00-0.3887350+00
 0.3907950+00 0.3079100-01
 7 0.6977370+01-0.6589210-01 0.2125850-01 0.7642810+00 0.9560310+00
 0.3079100-01-0.3256150+00
 8 0.6985170+01-0.5137110-01-0.2543940+00-0.3708360+00-0.2292080+00
 -0.3256150+00-0.6794200+00
 9 0.6852120+01-0.6792460+00-0.1309650+01-0.1105540+01-0.4006640+00
 -0.6794200+00-0.1023850+01
 10-0.1636860+02-0.8513130+02-0.1157670+03-0.6961500+02-0.1568150+02
 -0.1023850+01-0.1339320+01
 11-0.7242550+04-0.2158360+05-0.2408100+05-0.1193340+05-0.2216320+04
 -0.1339320+01-0.1481390+01

THE DATA IS ORDERED AS FOLLOWS:

CONTACT POINTS, GEOMETRIC CONSTRAINTS, AND PROFILE CURVATURES
AS A FUNCTION OF WHEELSET LATERAL DISPLACEMENT

XW = WHEELSET LATERAL, POSITIVE TO THE LEFT (IN)
 X1 = CONTACT LOCATION ON RIGHT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
 X2 = CONTACT LOCATION ON RIGHT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 X3 = CONTACT LOCATION ON LEFT WHEEL, POSITIVE OUT FROM TAPELINE (IN)
 X4 = CONTACT LOCATION ON LEFT RAIL, POSITIVE OUT FROM CENTERLINE (IN)
 RR = ROLLING RADII, RIGHT WHEEL (IN)
 YR = RAIL HEAD PROFILE HEIGHT, RIGHT RAIL (IN)
 RL = ROLLING RADII, LEFT WHEEL (IN)
 YL = RAIL HEAD PROFILE HEIGHT, LEFT RAIL (IN)
 MR = CONTACT ANGLE W.R.T. AXLE, RIGHT WHEEL (RAD)
 ML = CONTACT ANGLE W.R.T. AXLE, LEFT WHEEL (RAD)
 1/(RL-RR)/2A = NORMALIZED DIFFERENCE IN ROLLING RADII (IN/IN)
 (ML-MR)/2 = NORMALIZED DIFFERENCE IN CONTACT ANGLES (RAD)
 WR = WHEELSET ROLL ANGLE W.R.T. HORIZONTAL, POSITIVE UP ON LEFT (RAD)
 YCG = VERTICAL DISPLACEMENT OF WHEELSET CENTROID FROM NOMINAL POS. (IN)
 RR CRV = PRINCIPAL ROLLING CURVATURE OF RIGHT WHEEL PROFILE (1/IN)
 RL CRV = PRINCIPAL ROLLING CURVATURE OF LEFT WHEEL PROFILE (1/IN)
 CWR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYR = PRINCIPAL TRANSVERSE CURVATURE OF RIGHT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CWL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT WHEEL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)
 CYL = PRINCIPAL TRANSVERSE CURVATURE OF LEFT RAIL PROFILE,
 POSITIVE FOR CURVATURE CENTER IN BODY (1/IN)

122 6

-0.1200000+01-0.2123460+01-0.1325540+01 0.1906540+01-0.2557940+00 0.1761420+02
 0.6852820+01 0.1648590+02 0.6986910+01 0.6693620+00 0.4905880-01-0.1864850-01
 -0.3101510+00-0.1642040-01 0.4418020+00
 0.4452200-01 0.6058480-01 0.7669330+01 0.3908910+01 0.9586780-01 0.1473590+00
 -0.1180000+01-0.2093460+01-0.1324820+01 0.1886540+01-0.2470920+00 0.1758440+02
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ETC.

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